Name: $\qquad$
Student ID:

## Instructions:

1. You must show correct work to receive credit. Correct answers with inconsistent work will not be given credit.
2. Books and notes are not allowed.
3. You may use a simple calculator.
4. Turn off and put away all cell phones.

| Page | Points | Points Possible |
| :---: | :---: | :---: |
| 2 |  | 12 |
| 3 |  | 14 |
| 4 |  | 11 |
| 5 |  | 13 |
| Total |  | 50 |

Name: $\qquad$

1. The augmented matrix of a linear system is $A=\left[\begin{array}{lll|l}2 & 2 & -2 & a \\ 3 & 2 & -2 & b \\ 2 & 1 & -1 & c\end{array}\right]$.
(a) ( 8 pts ) Determine the values of $a, b, c$ for which the system is consistent.
(b) (4 pts) If $a=4, b=1$ and $c=-1$, how many solutions does the system have?

Name:
2. ( 6 pts ) If $A$ is a $4 \times 4$ matrix with $\operatorname{det}(A)=3$, find $\operatorname{det}\left(4 A^{3} A^{t}(2 A)^{-1}\right)$.
3. (8 pts) Let $A=\left[\begin{array}{rrr}2 & 6 & 2 \\ 3 & 5 & 1 \\ -1 & 3 & 2 \\ 2 & 2 & 0\end{array}\right]$. Prove or disprove: The linear system $A \mathbf{x}=\mathbf{b}$ has a unique solution for every vector $\mathbf{b}$ in $\mathbb{R}^{4}$.

Name:
4. (3 pts) Prove or disprove: If $\mathbf{v}$ is any vector in a vector space $V$ then $\{\mathbf{v}\}$ is linearly independent.
5. (8 pts) For which values of $a$ is the set $S=\left\{a x^{3}, x^{3}+(2 a-1) x^{2}, a^{2} x^{2}+(a-4) x\right\}$ linearly independent?

## Name:

6. (5 pts) Let $A$ and $B$ be two $n \times n$ matrices with $\operatorname{det}(A)=\operatorname{det}(B) \neq 0$. Find a matrix $C$ such that $\operatorname{det}(C)=1$ and $A=C B$.
7. ( 8 pts ) Let $V$ and $W$ be subspaces of the Euclidean space $\mathbb{R}^{5}$. Determine whether the set $S=\{\mathbf{v}-\mathbf{w} \mid \mathbf{v} \in V, \mathbf{w} \in W\}$ is a subspace of $\mathbb{R}^{5}$.
