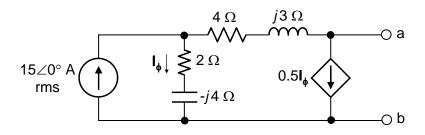
#### Problem (12 pts)

Consider the circuit shown



a. Determine the open-circuit voltage at terminals a and b. (3 pts)

$$15 = 1.5 \mathbf{I}_{\phi}$$
;  $\mathbf{I}_{\phi} = 10 \text{ A}$ ;  $\mathbf{V}_{Th} = 10(2 - j4) - 5(4 + j3) = -j55 \text{ V}$ .

b. Determine the current flowing in the short circuit when there is a short between terminals a and b. (3 pts)

$$15 = 1.5 \mathbf{I}_{\phi} + \mathbf{I}_{SC};$$

$$\mathbf{I}_{\phi}(2 - j4) = (0.5 \mathbf{I}_{\phi} + \mathbf{I}_{SC})(4 + j3);$$
solving these two equations gives 
$$15 \angle 0^{\circ} \text{ A}$$

$$\mathbf{I}_{SC} = \frac{165}{74}(1 - j6) \text{ A}$$

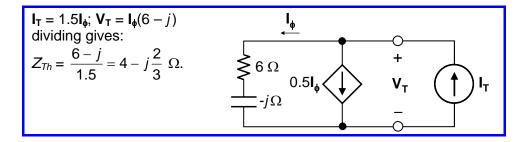
$$15 = 1.5 \mathbf{I}_{\phi} + \mathbf{I}_{SC};$$

$$15 \angle 0^{\circ} \text{ A}$$

c. Determine the equivalent impedance  $Z_{Th}$  as seen by the terminals a and b. (2 pts)

$$Z_{Th} = \frac{|\mathbf{V}_{Th}|/|\mathbf{I}_{SC}|}{165(1-j6)} = 4-j\frac{2}{3}\Omega$$

d. Evaluate  $Z_{Th}$  again using a different method then that employed in part (c). (4 pts)



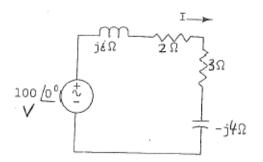
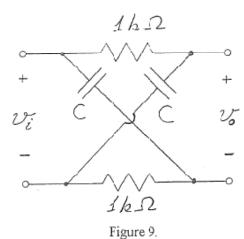


Figure 4.

- Find the current in the circuit shown in figure 4.
- \_\_\_A. 18.6 /<u>-21.8°</u> A
  - B. 22.5 /<u>-35.6°</u> A
  - C. 12.3 /-18.9° A
  - D. 34.7 /-29.7° A
  - E. None of the above



Hint: redraw lattice circuit as a bridge

- 9. Determine C in the circuit shown in figure 9 so that the output voltage  $v_o$  has the same magnitude as the input voltage  $v_i$  but lags it by 90°, assuming  $\omega = 200$  rad/s.
- A. 5 μF
  - B. 2 μF
  - C. 6 µF
  - D. 8 µF
  - E. None of the above

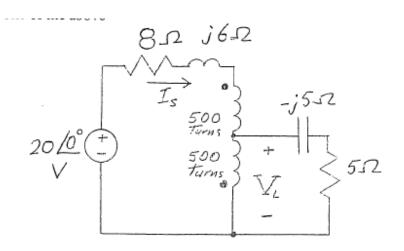


Figure 12.

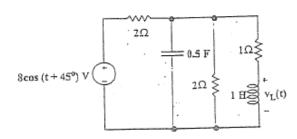
- 12. Determine Is and VL in the circuit shown in figure 12.
  - A. 1.4∠-45.0° A, 0 V
  - B. 0.7∠-45.0° A, 0.3∠45.0° V
  - C. 1.4∠-36.3° A, 0.3∠14.4° V

Hint: determine current in (5 - j5) ohms, assuming autotransformer is ideal

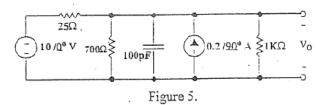
- C. 1.4 \( -36.3 \) A, V.S \( \)

  D. 1.1 \( \times -45.0^\circ \text{A}, 0.4 \times 45.0^\circ \text{V} \)

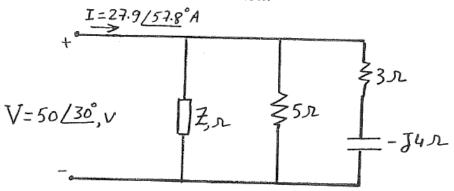
  2 \( \frac{1.4 \( \times -36.3 \) A, OV
- Find the expression of v<sub>L</sub>(t) in 4. the circuit shown in Fig. 3.
  - A.  $v_L(t) = 1.89\cos(t + 90^\circ) V$ 
    - B.  $v_L(t) = 1.24\cos(t 90^\circ) \text{ V}$
    - C.  $v_L(t) = 2.58\cos(t + 45^\circ) \text{ V}$
    - D.  $v_L(t) = 0.96\cos(t 45^\circ) \text{ V}$
    - E. None of the above



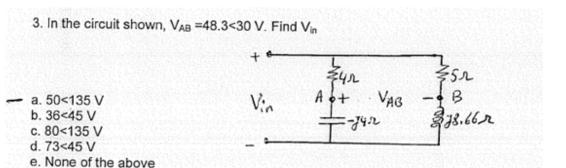
- Find  $v_0$  in the circuit shown in Fig. 5 if  $\omega = 5 \times 10^6$  rad/s.
  - A. 14.7 /<u>21.8</u>° V
  - B. 11.6/<u>15.6</u>° V
  - C. 12.8 /35.2° V
  - →D. 10.5 /<u>25.9</u>° V
    - E. None of the above



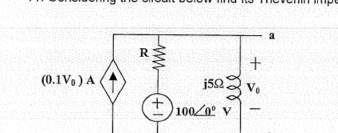
12. Determine Z in the circuit shown below:



- A.  $0.2 < 29.9^{\circ}\Omega$
- Β. 5Ω
- →C. 5<-29.9 Ω
  - D. 1.8<-27.8Ω
  - E. None of the above.



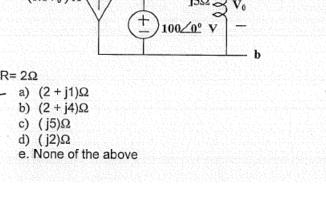
11. Considering the circuit below find its Thevenin impedance between a and b.



 $R = 2\Omega$ 

a)  $(2 + j1)\Omega$ b)  $(2 + j4)\Omega$ 

c) (j5)Ω d) (j2)Ω e. None of the above



19. Determine Thevenin's impedance looking into terminals ab, given the reactance of C is -j 10  $\Omega$ .  $2V_x$ -j 20 Ω +j 20 Ω -j 40 Ω  $+j40\Omega$ j 20 Ω None of the above

6. Determine 
$$L$$
 so that the bridge is balanced ( $v_0 = 0$ ) at  $\omega = 10^6$  rad/s.

A. 1 mH

B. 2  $\mu$ H

C. 4  $\mu$ H

D. 1 H

E. None of the above

$$1 k\Omega$$

 $1 \text{ k}\Omega$ 

ttion:: At balance, 
$$\frac{Z_1}{Z_2} = \frac{Z_3}{Z_4}$$
;

$$Z_2 = \frac{R/j\omega C}{R+1/j\omega C} = \frac{R}{1+j\omega CR}; \Omega.$$

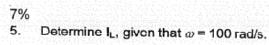
$$\frac{Z_1}{Z_2} = 1+j\omega CR. \text{ Hence. } \frac{R+j\omega L}{R} = \frac{R}{R}$$

$$= \frac{11 j\omega C}{R + 1/j\omega C} =$$
$$= 1 + j\omega CR \cdot H$$

 $1 + \frac{j\omega L}{R} = 1 + j\omega CR$ , or

 $L = CR^2 = 10^{-9} \times 10^6 \equiv 1 \text{ mH}.$ 

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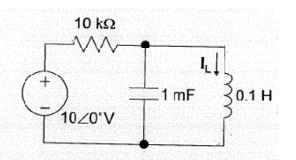


A. zero

8%

B. infinite

- D. 1∠-90° A E. None of the above



4 mH

0.25 mF

1 mH

2. Determine 
$$I_C$$
, given that  $\omega = 2 \text{ krad/s}$ 

C. 5∠-45° A D. 10∠90°

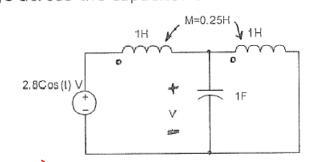
E. None of the above

**Solution:** 
$$j\omega L = j2 \times 10^{-3} \times 10^{-3} = j2 \Omega$$
;  $\frac{1}{j\omega C} = \frac{1}{j2 \times 10^3 \times 0.25 \times 10^{-3}} = -j2 \Omega$ .

10∠45° 1

The parallel impedance of  $j2 \Omega$  and  $-j2 \Omega$  is infinite, so that no current flows in the 4 mH inductor. The voltage across the capacitor is  $10\angle 45^{\circ}$  V, and  $I_C = \frac{10\angle 45^{\circ}}{-i2} = 5\angle 135^{\circ}$  A.

-7- Find the voltage across the capacitor of the circuit shown.



a. Cos(2.26t) b. 0 c. 2.26Cos(t) d. 0.25Cos(t) f. None of the above

7.Find the equivalent inductance for the following connection , such that: L=60mH, L'=80mH and M=100mH.

a)34.2mH b)86.6mH c)-15.3mH d)134.2mH e)NOA

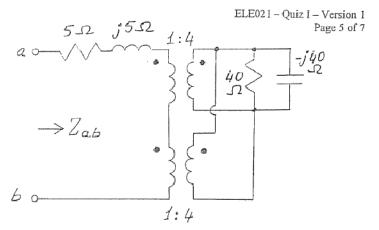
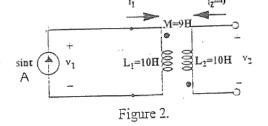


Figure 7.

- 7. Two identical transformers are connected as shown in figure 7. Determine the impedance  $Z_{ab}$ .
- -- A. 10 Ω
  - B. 15 Ω
  - C.  $10 + j10 \Omega$
  - D.  $10 j10 \Omega$
  - E. None of the above
- 3. Calculate the voltages  $v_1$  and  $v_2$  in the circuit of Fig. 2.
  - A.  $v_1 = -10 \cos V$ ;  $v_2 = -9 \cos V$
  - B.  $v_1 = 10 \cos V$ ;  $v_2 = 9 \cos V$
  - C.  $v_1 = 10 \cos V$ ;  $v_2 = -9 \cos V$ 
    - D.  $v_1 = 9 \cos V$ ;  $v_2 = -10 \cos V$
    - E. None of the above



- 8. Find the turns ratio for the ideal transformer shown in Fig. 7 required to match the 200 ohms source impedance to the 8 ohms load.
  - A. n = 3
  - B. n = 4
  - C. n = 5
    - D. n = 6
    - E. None of the above

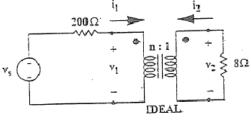


Figure 7.

15. Determine the Thevenin equivalent circuit between terminals a and b in Fig. 13 if

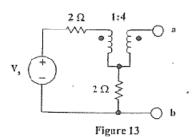
$$V_s = 10 \angle 0^{\circ} V$$
.

A. 
$$V_{Th} = 40 \text{ V}$$
;  $R_{Th} = 25 \Omega$ 

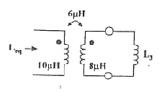
B. 
$$V_{Th} = 20 \text{ V}$$
;  $R_{Th} = 25 \Omega$ 

B. 
$$V_{Th} = 20 \text{ V}$$
;  $R_{Th} = 25 \Omega$   
C.  $V_{Th} = 40 \text{ V}$ ;  $R_{Th} = 50 \Omega$   
D.  $V_{Th} = 20 \text{ V}$ ;  $R_{Th} = 50 \Omega$   
E. Nohe of the above

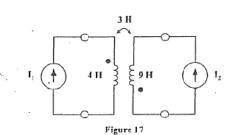
D. 
$$V_{Th} = 20 \text{ V}$$
;  $R_{Th} = 50 \Omega$ 



19. Determine  $L_{eq}$  in Fig. 16 if  $L_3 = 1 \mu H$ .



- Figure 16
- If  $I_1 = 2$  A in Fig. 17, find the value of 20. I2 that will minimize the stored energy.



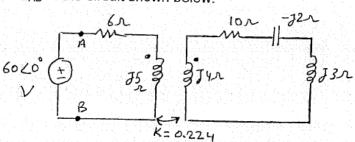
2. Find the input impedance ZAB in the circuit shown below.

A. 
$$6 + j 5.896 \Omega$$

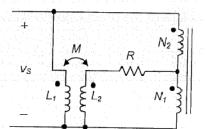
B. 
$$8.3 + j 4.7 \Omega$$

D. 
$$3.8 + j 9.2 \Omega$$

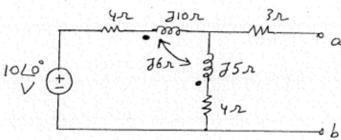
E. None of the above



5. In the figure shown,  $v_S = 10\cos 100\pi t \text{ V}$ ,  $L_1 = 120 \text{ mH}$ ,  $L_2 = 30 \text{ mH}$ , R = 100 ohms,  $N_1 = 400 \text{ turns}$ , and  $N_2 = 1600 \text{ turns}$ . Determine the coupling coefficient so that no current flows in the 100 ohm resistor.



- $\rightarrow$  A. 0.4
  - B. 0.5
  - C. 0.6
  - D. 0.8
  - E. None of the above
    - 9. In the circuit shown below, find the Thevenin equivalent circuit as seen from terminals a-b.



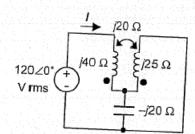
- $\rightarrow$  A. V<sub>Thev</sub>= 4.82<-34.60, V, Z<sub>Thev</sub>= 8.62<48.79 Ω
  - B.  $V_{Thev}$ = 4.82< 34.60, V,  $Z_{Thev}$ = 8.62<40.38  $\Omega$
  - C. V<sub>Thev</sub>= 48.2<-34.60, V, Z<sub>Thev</sub>= 86.2<48.79 Ω</p>
  - D. V<sub>Thev</sub>= 5<-34.60, V, Z<sub>Thev</sub>= 8.1<48.79 Ω
  - E. None of the above
- 12. Consider a source Vs supplying the primary of a transformer. The secondary is connected to a purely capacitive load Zc. The primary impedance is Z1, the secondary impedance is Z2, and the mutual impedance between primary and secondary is Zm. Calculate the currents I1 at primary and I2 at secondary.

Given:  $Vs = 150 < 0^{\circ} V$ ,  $Z1 = j3600 \Omega$ ,  $Z2 = j2500 \Omega$ ,  $Zm = j1200 \Omega$ , Zc = -j2400

- →A. 11= 13.9 <-90° mA, 12=166.6<+90° mA
  - B. I1= 13.9 <0° mA, I2=166.6<+180° mA
  - C. I1= 33.5 <-90° mA, I2=356.5 <+90° mA
  - D. I1= 33.5 <0° mA, I2=356.5<+180° mA
  - E. None of the above

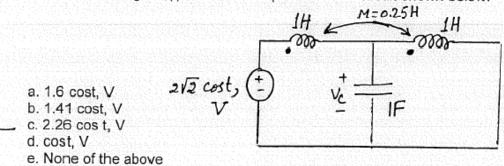
Assume dot markings are both up

- 1. Two magnetically coupled coils have a coefficient of coupling K=0.5. When they are connected in series, their total inductance is 80 mH. When connection of one of the coils is reversed, the total inductance becomes 40 mH. Specify which of the following represents the self-inductance of one of the coils L.
- A. 60 mH
- →B. 52.36 mH
  - C. 40 mH
  - D. 5.64 mH
  - E. None of the above
    - Determine I.
  - A. +j4 A rms
  - B. –*j*6 A rms
    - C. -j4.8 A rms
    - D. –j8 A rms
    - E. None of the above

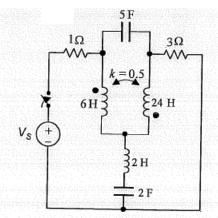


11. Determine  $I_2$  in the circuit shown.  $I_3 \circ 40^{\circ} \circ 1$   $I_4 \circ 40^{\circ} \circ 1$   $I_4 \circ 40^{\circ} \circ 1$   $I_5 \circ 40^{\circ} \circ 1$   $I_7 \circ 10^{\circ} \circ 10^{\circ} \circ 10^{\circ}$   $I_7 \circ 10^{\circ} \circ 10^$ 

- A. 25.61 <166.85 A</p>
- B. 3.56<-166.85 A
- C. 16.42<-13.15 A
- D. 9.33 <-193.15 A
  - E. None of the above
  - Find the voltage V<sub>c</sub>(t) across the capacitor of the circuit shown below.

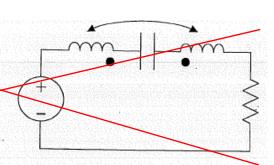


- Determine the total energy stored in the capacitors and inductors after the switch has been closed for a long time, 3. assuming  $V_S = 8$  V.
  - 12 J 30 J
  - B.
  - C. 120 J
    - D. 148 J
    - None of the above



7%

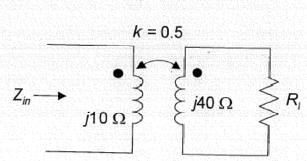
- If the dot marking on one of the coils is reversed, the damping coefficient &
  - A. increases
  - B. decreases
    - C. remains the same



7%

- Determine the minimum value of  $Z_{in}$  as  $R_L$  is varied between zero and infinity.
  - A. j5 Ω
  - B. j7.5 Ω C. j10 Ω D. 0

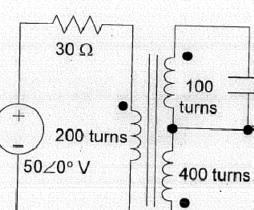
  - E. None of the above



9. Determine Thevenin's equivalent circuit between terminals ab, assuming the transformer is ideal.

$$V_{7h} = -64 + j48 V$$

$$Z_{7h} = \frac{96}{5} (4 - j3) - 2$$



-j10 Ω

The sinusoidal current source i(t) is given by:

$$i(t) = 10\sin(120\pi t)(Amps)$$

$$t \ge 0$$

t ≥ 0

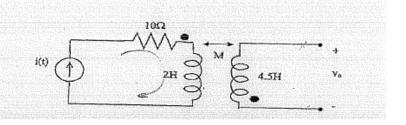
This current is applied to the primary coil of a transformer, as shown below. The primary coil (self-inductan 2H) is 100%-coupled to the secondary coil (self-inductance 4.5H).

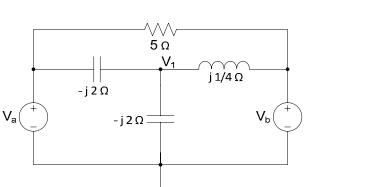
Find the value of the voltage  $v_s$  at t = 0.

(a) 15.75 kV (b) -11.31 kV

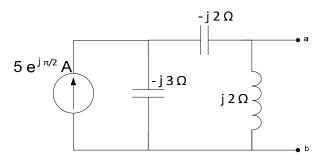


(d) 11.31kV (c) None of these

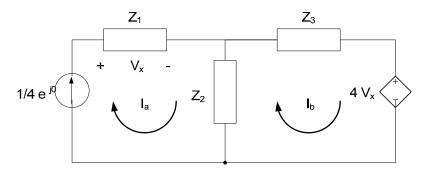




- 1. Find the correct node-equation for the voltage  $V_1$ .
- $\rightarrow$ a)  $6V_1 + V_a 8V_b = 0$ 
  - b)  $2V_1 + V_a 4V_b = 0$ c)  $V_1 - V_a + V_b = 0$
- d)  $3V_1 2V_a + V_b = 0$ 
  - e)  $7V_1 4V_a + V_b = 0$



- 4. Find the Thevenin equivalent circuit with respect to the terminals a-b. What are the values of  $V_{Th}$  in V and  $Z_{Th}$  in  $\Omega$ ?
- $\rightarrow$ a) V<sub>Th</sub> =-10 V, Z<sub>Th</sub> = j10/3 Ω
  - b)  $V_{Th} = -8 \text{ V}, Z_{Th} = j3 \Omega$
  - c)  $V_{Th} = -6 \text{ V}, Z_{Th} = j14/5 \Omega$
  - d)  $V_{Th} = -4 V$ ,  $Z_{Th} = j8/3 \Omega$
  - e)  $V_{Th} = -2 \text{ V}, Z_{Th} = j5/2 \Omega$



- 5. What is the expression for  $V_x$ ?
- a)  $(Z_1 + Z_2)$
- b) 5 Z<sub>1</sub>
- $\rightarrow$  c)  $Z_1/4$ 
  - d)  $2 Z_1$
  - e)  $Z_1/2$
  - 6. What is the correct set of equations for the mesh currents I<sub>a</sub> and I<sub>b</sub>?

a) 
$$I_a(-Z_1+4Z_2)-I_b(4Z_2+4Z_3)=0, I_a-5=0$$

b) 
$$I_a(-Z_1+2Z_2)-I_b(2Z_2+2Z_3)=0, I_a-2=0$$

c) 
$$I_a(-Z_1+Z_2)-I_b(Z_2+Z_3)=0, I_a-1=0$$

d) 
$$I_a(-2Z_1+Z_2)-I_b(Z_2+Z_3)=0, I_a-1/2=0$$

$$\rightarrow$$
e)  $I_a(-4Z_1+Z_2)-I_b(Z_2+Z_3)=0, I_a-1/4=0$ 

- 17. If a capacitor with impedance  $Z_2$  is connected in parallel to a load  $Z_1 = 300 + j450 \Omega$ . What should be  $\mathbb{Z}_2$  in ohms so that the equivalent load is purely resistive?

- $\rightarrow$ c) -650 i

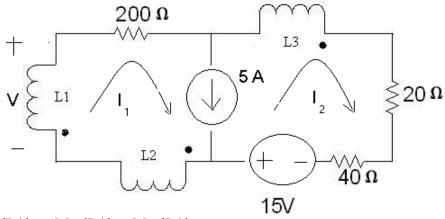
a) -928.6 j b) -1112.5 i

d) -750 j

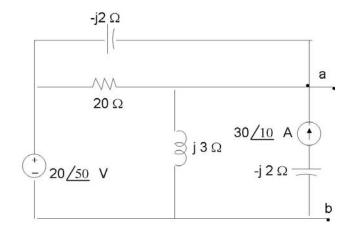
e) None of the above

- 22. Assuming that the voltage V across inductance L1 is as shown in figure below and that the mutual inductance between
  - L1 and L2 is M12
  - L1 and L3 is M13
  - L2 and L3 is M23

Use the mesh technique to find the expression of the voltage V.



- $\rightarrow$  a) V=- L<sub>1</sub>dI<sub>1</sub>/dt M<sub>12</sub>dI<sub>1</sub>/dt + M<sub>13</sub>dI<sub>2</sub>/dt
  - b) V=-  $L_1 dI_1/dt + M_{12} dI_1/dt + M_{13} dI_2/dt$
  - c) V=-  $L_1dI_1/dt + M_{12}dI_1/dt M_{13}dI_2/dt$
  - d) V=-  $L_1dI_1/dt + M_{12}dI_1/dt + M_{13}dI_2/dt$
  - e) None of the above

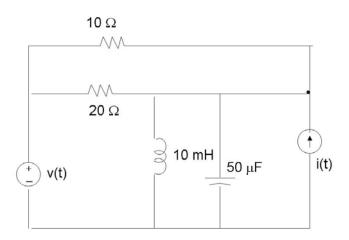


Find Zth across a and b

- A)  $Z_{th} = 3.85 j 0.77 \Omega$
- →B)  $Z_{th} = 1.65 j 5.50 Ω$ 
  - C)  $Z_{th} = 5.29 j 8.82 \Omega$
  - D)  $Z_{th}$  = 6.50- j 1.65 Ω
  - E) None of the above

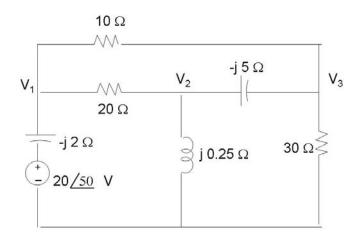
## Problem 2

What are the impedances in this circuit if  $v(t)=20\cos(10t+50^{\circ})$  Volts and  $i(t)=50\cos(10t+20^{\circ})$  Amperes.



- A)  $10 \Omega$ ,  $20 \Omega$ ,  $-j 0.1 \Omega$ ,  $j 0.05 \Omega$
- B)  $10 \Omega$ ,  $20 \Omega$ ,  $-j1.0 \Omega$ ,  $j0.05 \Omega$
- $\rightarrow$ C) 10  $\Omega$ , 20  $\Omega$ , j 0.1  $\Omega$ , -j 2000  $\Omega$ 
  - D)  $10 \Omega$ ,  $20 \Omega$ ,  $j 10 \Omega$ ,  $-j 20 \Omega$
  - E) None of the above

Find the node equations for the following circuit



$$(0.15 + j0.5)V_1 - 0.05V_2 - 0.1V_3 + 7.66 - j6.43 = 0$$

$$\rightarrow A) -0.05V_1 + (0.05 - j3.8)V_2 - j0.2V_3 = 0$$

$$-0.1V_1 - j0.2V_2 + (0.133 + j0.2)V_3 = 0$$

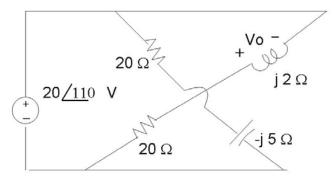
$$\begin{aligned} & \big(0.15+j0.5\big)V_1-0.1\,V_2-0.05\,V_3+7.66-j6.43=0 \\ & \text{B)} \quad -0.1\,V_1+\big(0.1-j3.8\big)V_2-j0.2V_3=0 \\ & \quad -0.05\,V_1-j0.2\,V_2+\big(0.0833+j0.2\big)V_3=0 \end{aligned}$$

$$(0.15 + j0.2)V_1 - 0.05 V_2 - 0.1 V_3 - 12.85 - j15.32 = 0$$
C)  $-0.05 V_1 + (0.05 - j3.8)V_2 - j0.2V_3 = 0$ 
 $-0.1 V_1 - j0.2 V_2 + (0.133 + j0.2)V_3 = 0$ 

$$\begin{aligned} & \big(0.15+j0.2\big)V_1-0.1\,V_2-0.05\,V_3-12.85-j15.32=0 \\ & \mathrm{D}\big) & -0.1\,V_1+\big(0.1-j3.8\big)V_2-j0.2V_3=0 \\ & -0.05\,V_1-j0.2\,V_2+\big(0.0833+j0.2\big)V_3=0 \end{aligned}$$

E) None of the above

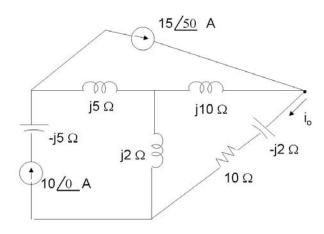
Find  $V_0$  (t) given  $\omega$ =120 rad/sec.



- A)  $V_0 = -0.99 \cos(120t + 94.29.^{\circ}) \text{ Volts}$ B)  $V_0 = -1.99 \cos(120t + 194.29^{\circ}) \text{ Volts}$ 
  - C)  $V_0 = -1.99 \cos(120t -25.7^{\circ}) \text{ Volts}$ D)  $V_0 = -0.99 \cos(120t -115.71^{\circ}) \text{ Volts}$

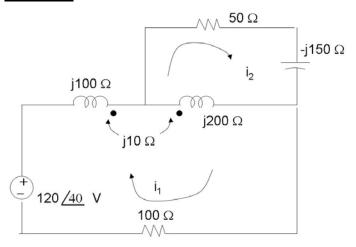
  - E) None of the above

### Problem 5



Find io in the circuit above.

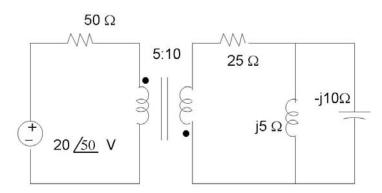
- A) 8.178\(\angle 104.62^0\)
- B) 23.14∠89.62°
- C) 16.36\(\angle 104.62^0\)
- →D) 11.57∠89.62°
  - E) None of the above



Given the circuit above, what are the two mesh equations?

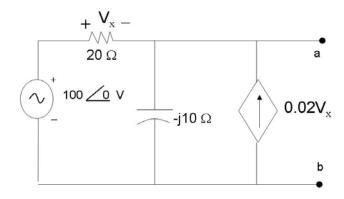
A) 
$$-120\angle 40^{\circ} + (100 + j280)i_{1} - 190i_{2} = 0;$$
  $-j190i_{1} + (50 + j50)i_{2} = 0$   
B)  $-120\angle 40^{\circ} + (100 + j400)i_{1} - 250i_{2} = 0;$   $-j250i_{1} + (50 + j50)i_{2} = 0$   
C)  $-120\angle 40^{\circ} + (100 + j200)i_{1} - 150i_{2} = 0;$   $-j150i_{1} + (50 + j50)i_{2} = 0$   
D)  $-120\angle 40^{\circ} + (100 + j320)i_{1} - 210i_{2} = 0;$   $-j210i_{1} + (50 + j50)i_{2} = 0$   
E) None of the above

## **Problem 7**



In the circuit shown above, what is the value of the reflected impedance of the 50 ohms resistor from the primary to the secondary side?

- A) 100 Ω
- B) 12.5 Ω
- C) 25 Ω
- $\rightarrow$ D) 200  $\Omega$ 
  - E) None of the above



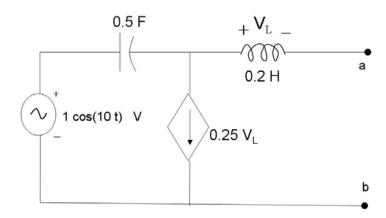
In the circuit shown above, find the Thevenin voltage across a,b

- A)  $76.82\angle -39.80^{\circ}$  V
- $\rightarrow$ B) 57.3∠ 55.0° V
  - C)  $28.6 \angle -63.0^{\circ}$  V
  - D)  $65.99 \angle -48.3^{\circ} V$
  - E) None of the above

## Problem 9

For the same circuit of previous problem, find Zth across a,b

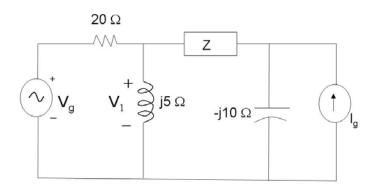
- A)  $Zth = 4.9 j4.1 \Omega$
- B) Zth=  $1.08 j2.12 \Omega$
- $\rightarrow$ C) Zth= 4.7- j6.71  $\Omega$ 
  - D) Zth=  $3.7 j5.1 \Omega$
  - E) None of the above



Find the Thevenin equivalent resistance and capacitance/inductance with respect to the terminals a,b in the circuit shown above

- $\rightarrow$  A) R = 0.1Ω; L=0.18 Ω
  - B)  $R = 0.2\Omega$ ;  $L=0.38 \Omega$
  - C)  $R = 0.25\Omega$ ;  $L=0.43 \Omega$
  - D)  $R = 0.15\Omega$ ; L=0.36  $\Omega$
  - E) None of the above

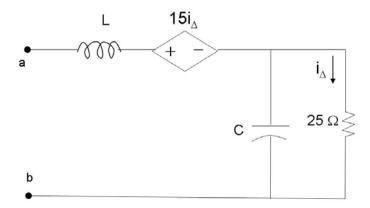
## Problem 11



In the circuit shown above, find the value of the impedance Z if

. 
$$V_1 = 40 + j30$$
 V,  $V_g = 100 - j50$  V, and  $I_g = 20 + j30$  A

- A)  $10-j5 \Omega$
- B)  $58+j14 \Omega$
- $\rightarrow$ C) 68+j24  $\Omega$ 
  - D)  $5+j20 \Omega$
  - E) None of the above



Find the input impedance Zi at the terminals a,b in the circuit shown above

$$\rightarrow$$
 A)  $Z_i = jL\omega + \frac{40}{1 + j25C\omega}$   $\Omega$ 

B) 
$$Z_i = jL\omega + \frac{25}{1 + i40C\omega}$$

C) 
$$Z_i = jL\omega + \frac{15}{1 + j40C\omega}$$
  $\Omega$ 

D) 
$$Z_i = jL\omega + \frac{40}{1 + j15C\omega}$$
  $\Omega$ 

E) None of the above

#### **Problem 13**

In the circuit of the previous problem, find the frequency  $\omega$  such that the input impedance Zi is purely resistive.

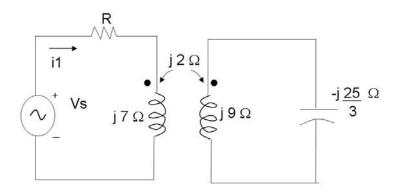
A) 
$$\omega = \frac{1}{40C} \sqrt{1000 \frac{C}{L} - 1}$$
 rad/s

$$\rightarrow$$
B)  $\omega = \frac{1}{25C} \sqrt{1000 \frac{C}{L} - 1}$  rad/s

C) 
$$\omega = \frac{1}{40C} \sqrt{600 \frac{C}{L} - 1}$$
 rad/s

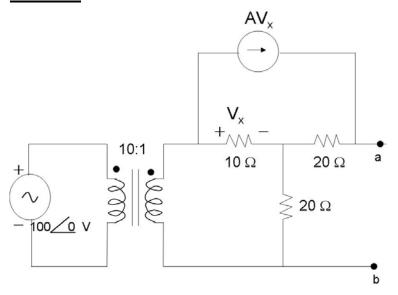
D) 
$$\omega = \frac{1}{15C} \sqrt{600 \frac{C}{L} - 1}$$
 rad/s

E) None of the above



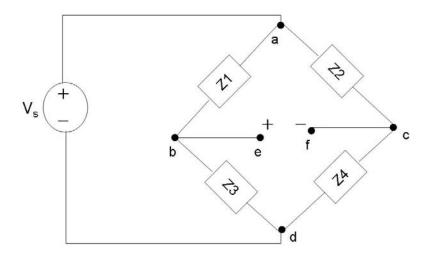
In the circuit shown above, it is given that  $\mathbf{R}=\mathbf{1} \Omega$ , and  $\mathbf{V}=\mathbf{10} \mathbf{0}$  volts. Find the current i1 as indicated.

- A)  $8\angle -53.13^{\circ}$  A
- B)  $7.07 \angle -53.13^{\circ} \text{ A}$   $\rightarrow$  C)  $7.07 \angle -45^{\circ} \text{ A}$ 
  - D)  $8 \angle -45^{\circ} \text{ A}$
  - E) None of the above



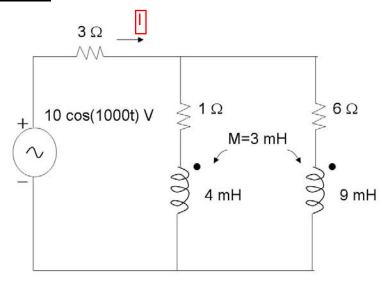
Find the magnitude of the Thevenin Voltage  $V_{th}$  across terminals a,b in the circuit above. Given A=1/4.

- → A) 15.0 V
  - B) 37.5 V
  - C) 14.29 V
  - D) 7.15 V
  - E) None of the above



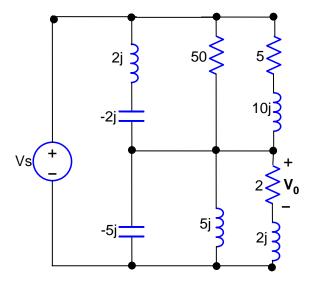
In the circuit shown above, given  $V_s = 48 \angle 90^\circ$  V,  $Z_1 = 3 + j4 \Omega$ ,  $Z_2 = 8 - j6 \Omega$ ,  $Z_3 = 3 - j4 \Omega$  and  $Z_4 = 8 + j6 \Omega$ . The Thevenin equivalent circuit values for the voltage souce and the internal impedance across terminals e and f are:

- A)  $14\angle 0^{0}$  V,  $3.5 j3.5 \Omega$
- B)  $50 \angle 0^0$  V,  $2.5 + j2.5 \Omega$ ,
- C)  $14 \angle 0^{0}$  V,  $7.29 \Omega$
- →D)  $50 \angle 0^0$  V, 10.42 Ω
  - E) None of the above



In the circuit shown above, the phasor form of the current I in amperes is:

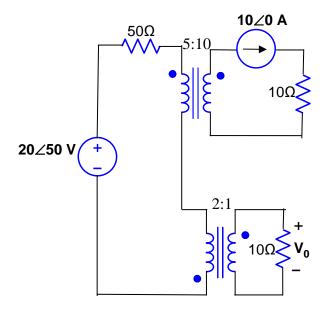
- $\rightarrow$  A) 1.833 $\angle -45.0^{\circ}$  V
  - B)  $0.917 \angle -45.0^{\circ}$  V
  - C)  $1.5\angle -53.13^{\circ}$  V
  - D)  $3.0 \angle -53.13^{\circ}$  V
  - E) None of the above



Find  $V_0$  if the source voltage is  $Vs = 20 \angle 60^{\circ}$  Volts.

- $\rightarrow$ A) 14.14 ∠ 15° V
  - B)  $7.07 \angle 15^{\circ} \text{ V}$
  - $\stackrel{\cdot}{\text{C}}$  20 $\stackrel{\prime}{\text{C}}$  60 $^{\circ}$  V
  - D)  $10 \angle 60^{\circ}$  V
  - E) None of the above

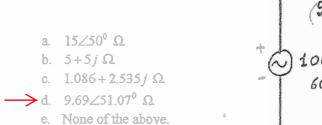
# Problem 13

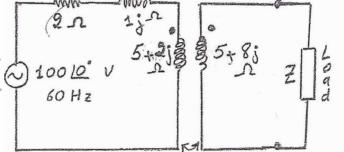


Find V<sub>0</sub>.

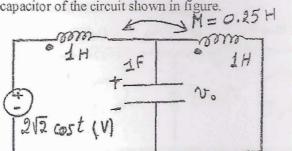
- A) 400 ∠ 0 V
- →B) 400 ∠ 0 V
  - C) 100 ∠ 0 V
  - D) 100 ∠ 0 V
  - E) None of the above

3. Determine the Thevenin impedance to the left of the terminals T1-T2 of the circuit shown in figure.



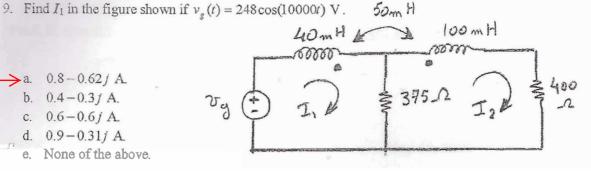


5. Find the voltage  $v_0(t)$  across the capacitor of the circuit shown in figure.

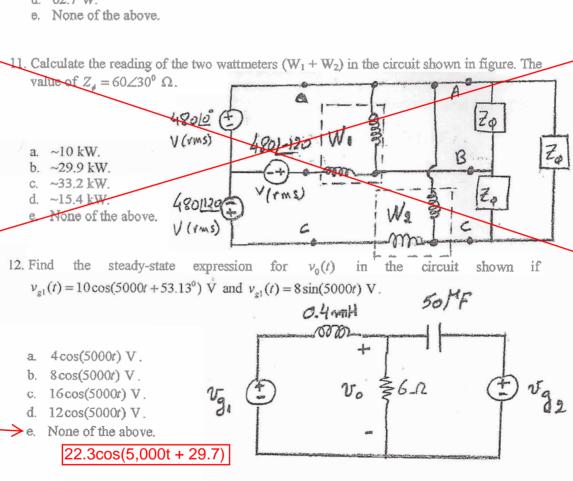


- a. 1.60 cos(2t) V.
- b. 1.60 sin(t) V.
- c. 3.2 cos(t) V.
- d. 2.26 cos(t) V.
   None of the above.

a. 0.8-0.62 j A. b. 0.4 - 0.3 j A. c. 0.6-0.6 j A. d. 0.9-0.31j A None of the above.

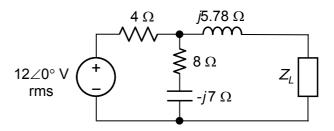


- 10. In problem 9, find the average power delivered to the 375  $\Omega$  resistor.
  - a. 99.2 W.
  - b. 50.3 W.
- >c. 49.2 W.
  - d. 62.7 W.



#### Problem 8 (14 pts)

Consider the circuit shown



a. For  $Z_L = 3 - j5.2 \Omega$ , determine the average power developed by the voltage source and the average power absorbed by the load. (4 pts)

$$V_{Th} = 12 \frac{8 - j7}{12 - j7} = 9 - j1.74 \text{ V};$$

$$|V_{Th}| = 9.18 \text{ V};$$

$$I_L = V_{Th}/6 = 1.5 - j0.29 \text{ A};$$

$$V_1 = (3 - j0.58)I_L = 4.68 + j0 \text{ V} \text{ rms}$$

$$I_{SRC} = \frac{12 - 4.68}{4} = 1.83 + j0 \text{ A}$$

$$P_{SRC} = V_1 I_{SRC} = 12 \times 1.83 \cong 22 \text{ W}; P_L = \frac{(9.18)^2}{4 \times 3} \cong 7 \text{ W}.$$

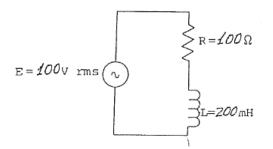


Figure 3.

- 3. Determine the power dissipated in the load in the circuit shown in figure 3. f = 60 Hz.
  - A. 38.8 W
- B. 63.8 W
  - C. 52.5 W
  - D. 45.3 W E. None of the above

A coil (R and L) has a resistance of 10Ω and draws a current of 5A (RMS)
when connected across a 100V (RMS), 60 Hz source. Determine the inductance
of the coil.

- c. 45.94 mH d. 102.73 mH

e. None of the above

a. 17.32 mH b. 32.48 mH 1. If M = 5 mH, determine the ratio  $v_1/v$ .

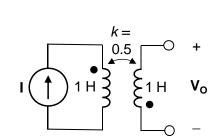
**Solution:** 
$$L_{eq} = L_1 + L_2 - 2M$$
;  $v = L_{eq} \frac{di}{dt}$ ;  $v_1 = L_1 \frac{di}{dt} - M \frac{di}{dt}$ ;

hence,  $\frac{v_1}{v} = \frac{L_1 - M}{L_1 + L_2 - 2M} = \frac{60 - M}{100 - 2M}$ 

2. Determine  $V_0$ , given that  $I = 1 \angle 0^\circ$  A and  $\omega = 10$  rad/s.

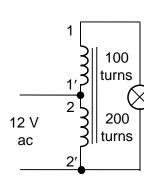
**Solution:**  $M = k\sqrt{L_1L_2} = 0.5 \, \text{H}$ ; secondary voltage is  $j\omega M \text{I}$ , with the dotted terminal positive with respect to the undotted terminal. Hence,  $\mathbf{V_0} = -j\omega M \text{I} = -j10\times0.5 \, \text{I} = -j5 \, \text{I}$ .

3. The lamp glows brighter when the dots are at coil terminals **Solution:** The lamp glows brighter when the voltage across it is largest. This occurs when the voltages across the windings are additive, that is, when the dots are at terminals 1 and 2 or 1' and 2'.



60 mH

40 mH



6. Derive the time-domain expression for  $v_C$ , given that  $v_{SRC} = 10\sin(2,000t)$  V.

**Solution:** 
$$\omega L = 2 \times 10^{3} \times 2 \times 10^{-3} = 4 \Omega$$
;

$$\frac{1}{\omega C} = \frac{1}{2 \times 10^3 \times 100 \times 10^{-6}} = 5 \ \Omega; \ \mathbf{V}_{SRC} = 10 \angle 0^{\circ}.$$

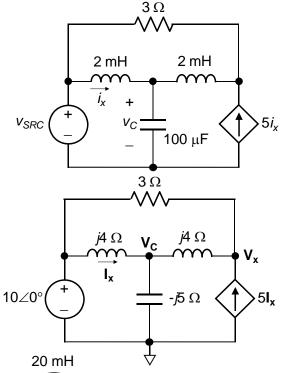
The node-voltage method can be applied, the circuit being as shown. At the middle node:

$$V_{c}/-j5 + (V_{c} - V_{x})/j4 + (V_{c} - 10)/j4 = 0$$

At the right-hand node:

$$(\mathbf{V_x} - \mathbf{V_c})/j4 + (\mathbf{V_x} - 10)/3 = 5\mathbf{I_x} = 5(10 - \mathbf{V_c})/j4$$
  
Solving,  $\mathbf{V_c} = 11.98 + j1.44 = 12.1 \angle 6.86^\circ$ , so that

 $v_C = 12.1\sin(2,000t + 6.86^{\circ}) \text{ V}.$ 



7. Derive  $V_{Th}$  and  $Z_{Th}$  as seen between terminals ab, given that  $v_{SRC}$  =  $10\cos(1,000t + 45^{\circ})$  V.

Solution:  $\omega L_1 =$ 

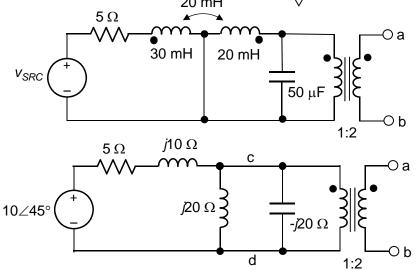
$$10^3 \times 30 \times 10^{-3} = 30 \ \Omega; \ \omega L_2$$

$$= \omega M = 10^3 \times 20 \times 10^{-3} = 20$$

$$\Omega; \ \frac{1}{\omega C} = \frac{1}{10^3 \times 50 \times 10^{-6}}$$

= 20 Ω; 
$$V_{SRC}$$
 = 10∠45°.

The circuit in the



frequency domain will be as shown, where  $\omega(L_1-M)=10~\Omega$ ;  $\omega(L_2-M)=0~\Omega$  and is omitted. The  $j20~\Omega$  in parallel with  $-j20~\Omega$  is effectively an open circuit. The current in the  $(5+j10)~\Omega$  impedance is zero,  $\mathbf{V}_{cd}=10\angle45^\circ$ , and  $\mathbf{V}_{ab}=\mathbf{V}_{Th}=20\angle45^\circ$ .

If the independent voltage source is replaced by a short circuit, the impedance on the primary side is  $(5 + j10) \Omega$  and  $Z_{Th} = 4(5 + j10) = 20 + j40 \Omega$ .

Determine the impedance seen by the source, assuming a = 2.

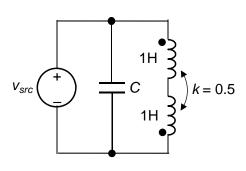
 $4 \angle 0^{\circ} \lor \begin{matrix} + \\ - \\ - \\ 1:a \end{matrix}$ 

**Solution:** Reflection of the  $(5 - j5) \Omega$ 

through the RH transformer gives  $(20 - j20) \Omega$ . The impedance on the secondary side of the LH transformer is  $(25 - j10) \Omega$ . Reflected to the primary side, this becomes  $(25 - j10)/a^2 \Omega$ .

4. If  $v_{src} = 10\cos(1,000t)$  V, determine the energy stored in the circuit in the sinusoidal steady state at t = 0, assuming  $C = 1 \mu F$ .

**Solution:** At t = 0, the voltage across C is 10 V and the current through the inductors is zero, being proportional to the integral of  $v_{src}$ . The energy stored is  $W = \frac{1}{2}Cv^2 = 50C$ .



5. Determine  $R_x$  given that I = 0 and  $R = 2 \Omega$ .

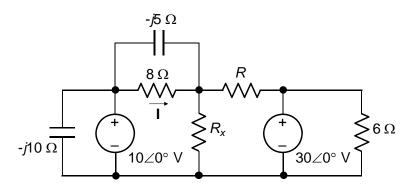
**Solution:** Since I = 0, the voltage across  $R_x$  is 10 V, and the same current  $\frac{30\angle 0^\circ - 10\angle 0^\circ}{R}$  flows

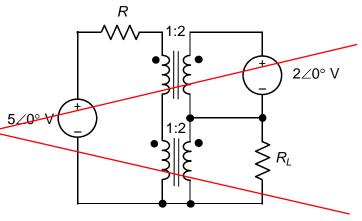
through R and  $R_x$ . It follows that

$$\frac{20}{R}R_x = 10$$
, or  $R_x = \frac{R}{2}$ .

7. Determine the maximum power that can be delivered to  $R_L$ , assuming  $R = 0.5 \Omega$ .

**Solution**: The primary voltage of the upper transformer is always 1 V. On





9. Two identical coils, each having an inductance of 10 mH, are connected in series. When the connections to one of the coils are reversed, the total inductance is multiplied by a factor *a*. Determine the coupling coefficient of the coils.

**Solution:** 
$$(10 + 10 + 2M) = a(10 + 10 - 10)$$

$$2M$$
);  $2M(a + 1) = 20(a - 1)$ ;

$$M = \frac{10(a-1)}{a+1}$$
;  $k = \frac{M}{10} = \frac{(a-1)}{a+1}$ 

10. Determine  $I_x$ , assuming  $R = 4 \Omega$ .

**Solution:** The voltage across all

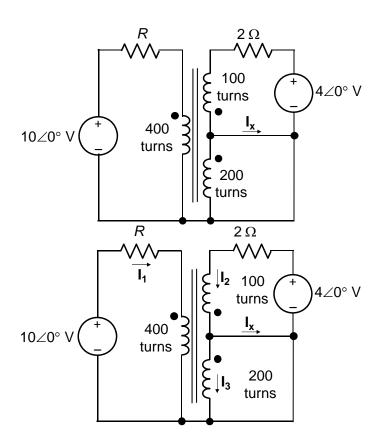
windings is zero. Hence, 
$$I_1 = \frac{10}{R} A$$
, and

$$I_2 = \frac{4}{2} = 2 \text{ A}$$
. Setting the net mmf to

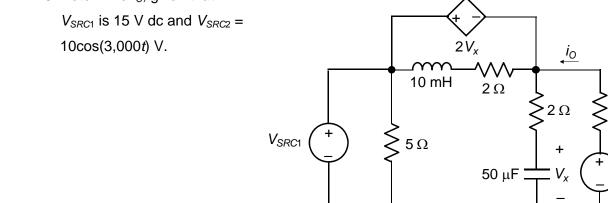
zero, 
$$400\mathbf{I}_1 - 100\mathbf{I}_2 + 200\mathbf{I}_3 = 0$$
, or

$$\frac{4 \times 10}{R} - 2 + 2 I_3 = 0$$
, which gives  $I_3 =$ 

$$1 - \frac{20}{R}; \, \mathbf{I_X} = \mathbf{I_2} - \mathbf{I_3} = 1 + \frac{20}{R}.$$

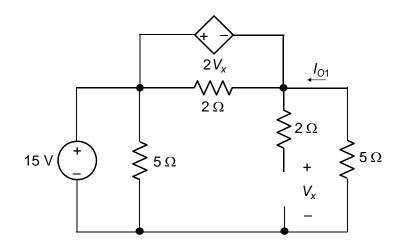


16. Determine  $i_0$ , given that



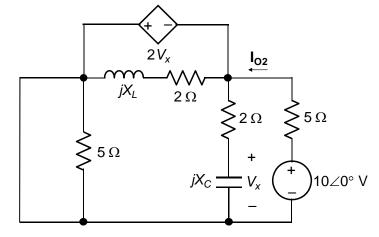
 $V_{SRC2}$ 

**Solution:** With  $V_{SRC1}$  applied and  $V_{SRC2}$  set to zero, the circuit becomes as shown.  $15 = 3V_x$ , so that  $V_x = 5$  V and  $I_{O1} = \frac{-V_x}{5} = -1$  A.



With  $V_{SRC2}$  applied and  $V_{SRC1}$  set to zero, the circuit becomes as shown. It follows that:  $-2V_x = V_x + \frac{2V_x}{jX_C}$ , or  $V_x \left(3 + \frac{2}{jX_C}\right) = 0$ , which gives  $V_x = 0$ . Hence,  $I_{02} = \frac{10\angle 0^{\circ}}{5} = 2\angle 0^{\circ}$  A. Thus,

 $i_0 = -1 + 2\cos(3,000t)$  A.



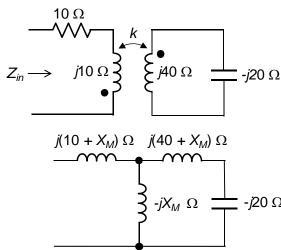
17. Determine *k* so that the input resistance is purely resistive.

**Solution:** Disregarding the 10  $\Omega$  resistance and replacing the linear transformer by its T-equivalent circuit, the circuit becomes as shown. The input reactance is

$$j10 + jX_M - \frac{jX_M(j20 + jX_M)}{j20} = 0$$
, or

$$10 + X_M - X_M - \frac{X_M^2}{20} = 0$$
, which gives

$$X_M = \sqrt{200} = 10\sqrt{2}$$
. Hence,  $k = \frac{10\sqrt{2}}{\sqrt{400}} = \frac{1}{\sqrt{2}} = 0.71$ .



Given 3 elements  $R = 10K\Omega$ , L = 10mH and C = 625nF powered by a source  $v = 90sin(10,000t + \frac{\pi}{4})$  (V). Find the impedance of each element  $Z_R$ ,  $Z_L$  and  $Z_C$ .

$$\longrightarrow$$
 A)  $Z_R = 10K\Omega, Z_L = 100j\Omega, Z_C = -160j\Omega$ 

B) 
$$Z_R = 10K\Omega, Z_L = 10j\Omega, Z_C = -16j\Omega$$

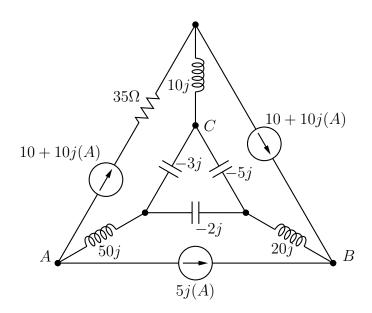
C) 
$$Z_R = 10jK\Omega, Z_L = 10j\Omega, Z_C = -1600j\Omega$$

D) 
$$Z_R = 10K\Omega, Z_L = 10j\Omega, Z_C = -160j\Omega$$

E) None of the above

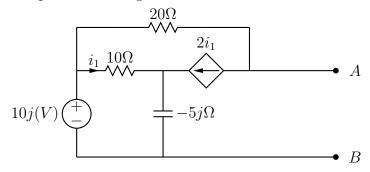
#### Problem 2

Find the Thevenin equivalent voltage between A and C. (Impedances are in  $\Omega$ )



- A) 285-190j V
- →B) -741+494j V
  - C) -741-494j V
  - D) 285+190j V
  - E) None of the above

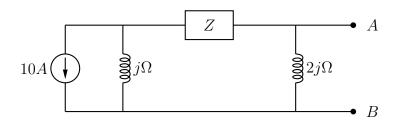
Find the Thevenin equivalent voltage between A and B.



- A)  $39.7V \angle 21.6^{\circ}$
- B)  $18.6V \angle 7.1^{\circ}$
- →C)  $18.6V \angle -7.1^{\circ}$ 
  - D)  $39.7V\angle 21.6^{\circ}$
  - E) None of the above

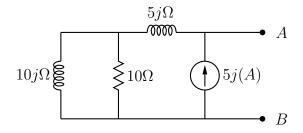
# Problem 4

Find the nature of Z such that the Thevenin equivalent impedance between A and B is  $1\Omega$ .



- $\longrightarrow$  A)  $0.8 1.4j\Omega$ 
  - B)  $0.8 + 1.4j\Omega$
  - C)  $0.5 2.5j\Omega$
  - D)  $0.5 + 2.5j\Omega$
  - E) None of the above

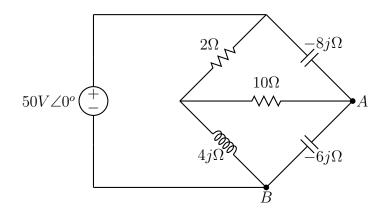
Find the Thevenin voltage between A and B.



- A) 50+25j V
- B) -100+50j V
- C) 100+50j V
- →D) -50+25j V
  - E) None of the above

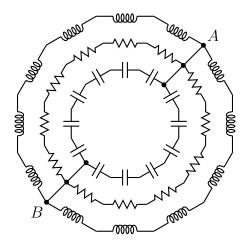
# Problem 6

Find the Thevenin impedance between A and B.



- A) 1.49-0.55j Ω
- B)  $0.96+3.21j \Omega$
- →C) 0.96-3.21j Ω
  - D)  $1.49+0.55j\ \Omega$
  - E) None of the above

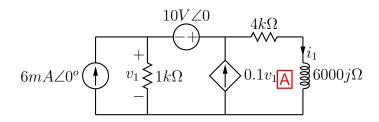
All the inductors are equal to  $5j\Omega$ , all the capacitors are equal to  $-6j\Omega$ , all the resistances are equal to  $10\Omega$ . Find  $Z_{AB}$ .



- A) 30.56+16.98j Ω
- B)  $30.56-16.98j\ \Omega$
- C) 27-9j  $\Omega$
- $\rightarrow$ D) 27+9j  $\Omega$ 
  - E) None of the above

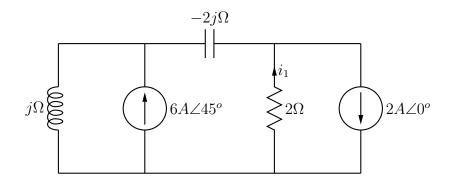
## Problem 8

Find  $i_1$ .



- →A) 0.76-1.14j mA
  - B) -0.26+1.6j mA
  - C) 0.26-1.6j mA
  - D) -0.76+1.14j mA
  - E) None of the above

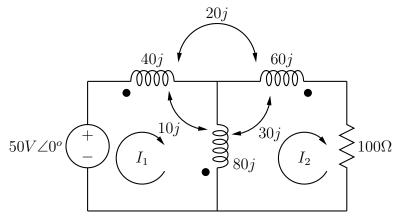
Find  $i_1$ .



- $\rightarrow$  A)  $3.38 \angle -29.2^{\circ}$  (A)
  - B)  $7.55\angle 82.4^{\circ}$  (A)
  - C)  $7.55 \angle 82.4^{\circ}$  (A)
  - D)  $3.38\angle 29.2^{\circ}$  (A)
  - E) None of the above

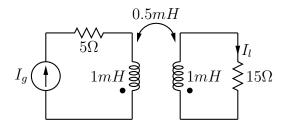
#### Problem 10

Write the two mesh current equation for  $I_1$  and  $I_2$  Don't solve. (Impedances are in  $\Omega$ ).



- A)  $100jI_1 + 60jI_2 = 50$   $60jI_1 + (100 + 80j)I_2 = 0$
- B)  $120jI_1 80jI_2 = 50$   $-80jI_1 + (100 + 80j)I_2 = 0$
- C)  $100jI_1 80jI_2 = 50$   $-80jI_1 + (100 + 80j)I_2 = 0$
- D)  $100jI_1 60jI_2 = 50$   $-60jI_1 + (100 + 80j)I_2 = 0$
- $\rightarrow$ E) None of the above

If  $I_g = 20cos(10,000t + \frac{\pi}{3})(A)$  find the energy associated with the 2 coils at the time  $t = 100\pi\mu s$ .

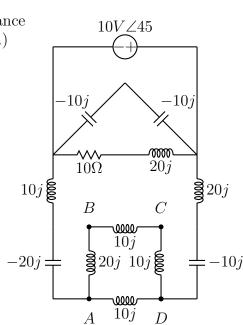


- →A) 65.3mJ
  - B) 261.3mJ
  - C) 40.7mJ
  - D) 163mJ
  - E) None of the above

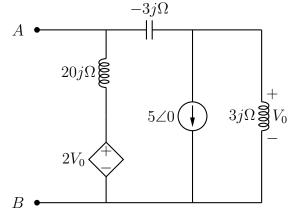
## Problem 12

Find the Thevenin equivalent impedance between A and B. (Impedances are in  $\Omega$ .)

- **→**A) 10j Ω
  - B) 8j Ω
  - C)  $7.5j \Omega$
  - D) 12j  $\Omega$
  - E) None of the above

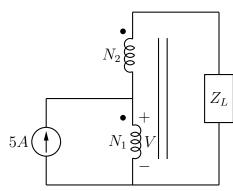


Find the Thevenin equivalent voltage between A and B  $(V_{AB})$ .



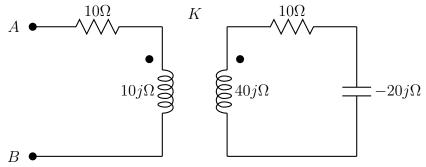
- A) 15j V
- B) -20j V
- C) 20j V
- →D) -15j V
  - E) None of the above

Given  $Z_L = 100 + 100j$ ,  $N_2 = 90$ ,  $N_1 = 10$ , find V.



- A)  $7.07V \angle 135^{\circ}$
- B)  $63.64V \angle 45^{\circ}$ C)  $63.64V \angle -135^{\circ}$
- →D)  $7.07V \angle 45^{\circ}$ 
  - E) None of the above

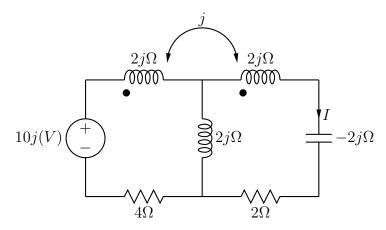
Consider the linear transformer of the figure below, given  $\omega = 1 rad/s$ , find the coupling coefficient K, such that the Thevenin impedance between A and B is purely resistive.



- $\rightarrow$ A) 0.79
  - B) 0.82
  - C) 0.85
  - D) 0.88
  - E) None of the above

#### Problem 17

Find I.



- A) 0.0389 0.6226j A
- B) -0.0778 + 1.2452j A
- $\rightarrow$ C) -0.0389 + 0.6226j A
  - D) 0.0778 1.2452j A
  - E) None of the above

6. Derive the time-domain expression for  $v_C$ , given that  $v_{SRC} = 10\sin(2,000t)$  V.

**Solution:**  $\omega L = 2 \times 10^{3} \times 2 \times 10^{-3} = 4 \Omega$ ;

$$\frac{1}{\omega C} = \frac{1}{2 \times 10^3 \times 100 \times 10^{-6}} = 5 \ \Omega; \ \mathbf{V}_{SRC} = 10 \angle 0^{\circ}.$$

The node-voltage method can be applied, the circuit being as shown. At the middle node:

$$V_{c}/-j5 + (V_{c} - V_{x})/j4 + (V_{c} - 10)/j4 = 0$$

At the right-hand node:

$$(\mathbf{V_x} - \mathbf{V_C})/j4 + (\mathbf{V_x} - 10)/3 = 5\mathbf{I_x} = 5(10 - \mathbf{V_C})/j4$$
  
Solving,  $\mathbf{V_C} = 11.98 + j1.44 = 12.1 \angle 6.86^\circ$ , so that  $\mathbf{V_C} = 12.1\sin(2,000t + 6.86^\circ)$  V.

7. Derive  $V_{Th}$  and  $Z_{Th}$  as seen between terminals ab, given that  $v_{SRC}$  =  $10\cos(1,000t + 45^{\circ}) \text{ V}.$ 

Solution:  $\omega L_1 =$ 

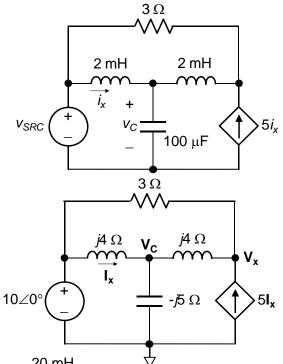
$$10^3 \times 30 \times 10^{-3} = 30 \ \Omega; \ \omega L_2$$

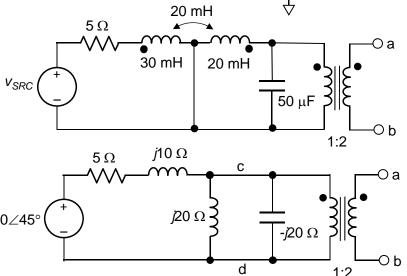
$$= \omega M = 10^3 \times 20 \times 10^{-3} = 20$$

$$\Omega; \ \frac{1}{\omega C} = \frac{1}{10^3 \times 50 \times 10^{-6}}$$

= 20 Ω; 
$$V_{SRC}$$
 = 10∠45°.

*j*10 Ω  $5\Omega$  $10^3 \times 30 \times 10^{-3} = 30 \ \Omega$ :  $\omega L_2$ С  $= \omega M = 10^3 \times 20 \times 10^{-3} = 20$ *j*20 Ω 10∠45° -j20 Ω = 20 Ω;  $V_{SRC}$  = 10∠45°. d 1:2 The circuit in the frequency domain will be as shown, where  $\omega(L_1 - M) = 10 \Omega$ ;  $\omega(L_2 - M) = 0 \Omega$  and is omitted. The j20  $\Omega$  in parallel with -j20  $\Omega$  is effectively an open circuit. The current in the (5 + j10)  $\Omega$ impedance is zero,  $V_{cd} = 10 \angle 45^{\circ}$ , and  $V_{ab} = V_{Th} = 20 \angle 45^{\circ}$ .

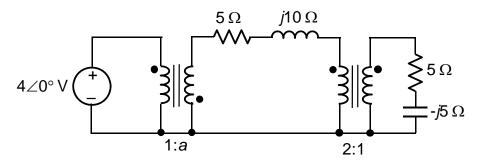




If the independent voltage source is replaced by a short circuit, the impedance on the primary side is  $(5 + j10) \Omega$  and  $Z_{Th} = 4(5 + j10) = 20 + j40 \Omega$ .

Determine the impedance seen by the source, assuming a = 2.

**Solution:** Reflection of the  $(5 - j5) \Omega$ 



through the RH transformer gives  $(20 - j20) \Omega$ . The impedance on the secondary side of the LH transformer is  $(25 - j10) \Omega$ . Reflected to the primary side, this becomes  $(25 - j10)/a^2 \Omega$ .

4. If  $v_{src} = 10\cos(1,000t)$  V, determine the energy stored in the circuit in the sinusoidal steady state at t = 0, assuming  $C = 1 \mu F$ .

**Solution:** At t = 0, the voltage across C is 10 V and the current through the inductors is zero, being proportional to the integral of  $v_{src}$ . The energy stored is  $W = \frac{1}{2}Cv^2 = 50C$ .

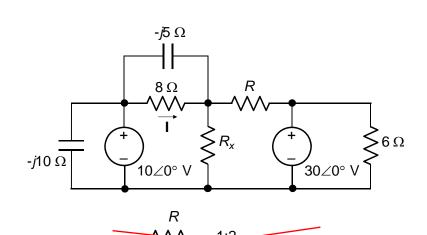
$$V_{SYC}$$
 $+$ 
 $C$ 
 $1H$ 
 $k = 0.5$ 

5. Determine 
$$R_x$$
 given that  $I = 0$  and  $R = 2 \Omega$ .

**Solution:** Since I = 0, the voltage across  $R_x$  is 10 V, and the same current  $\frac{30\angle 0^{\circ} - 10\angle 0^{\circ}}{R}$  flows

through R and  $R_x$ . It follows that

$$\frac{20}{R}R_x = 10$$
, or  $R_x = \frac{R}{2}$ .



9. Two identical coils, each having an inductance of 10 mH, are connected in series. When the connections to one of the coils are reversed, the total inductance is multiplied by a factor *a*. Determine the coupling coefficient of the coils.

**Solution:** 
$$(10 + 10 + 2M) = a(10 + 10 - 10)$$

$$2M$$
);  $2M(a + 1) = 20(a - 1)$ ;

$$M = \frac{10(a-1)}{a+1}$$
;  $k = \frac{M}{10} = \frac{(a-1)}{a+1}$ 

10. Determine  $I_x$ , assuming  $R = 4 \Omega$ .

Solution: The voltage across all

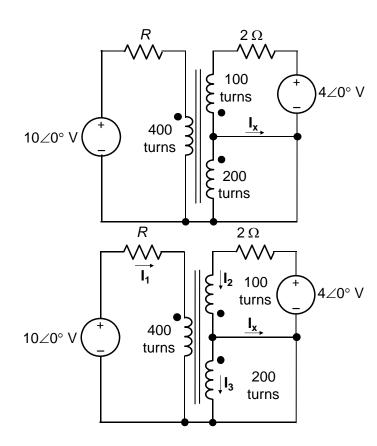
windings is zero. Hence,  $I_1 = \frac{10}{R} A$ , and

$$I_2 = \frac{4}{2} = 2 \text{ A}$$
. Setting the net mmf to

zero,  $400\mathbf{I_1} - 100\mathbf{I_2} + 200\mathbf{I_3} = 0$ , or

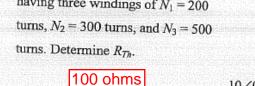
$$\frac{4 \times 10}{R}$$
 - 2 + 2  $I_3$  = 0, which gives  $I_3$  =

$$1 - \frac{20}{R}; \, \mathbf{I_X} = \mathbf{I_2} - \mathbf{I_3} = 1 + \frac{20}{R}.$$



Given an ideal autotransformer having three windings of  $N_1 = 200$ turns,  $N_2 = 300$  turns, and  $N_3 = 500$ 

18%



10∠0° V

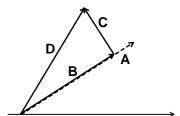




**1.** A current  $i = I_m \cos(\omega t + 30^\circ)$  flows through an impedance  $(5 - j5) \Omega$ . Determine the rms phasor voltage across the impedance if  $I_m = 2.5 \text{ A}$ .

**Solution:** The phasor current is  $I_m \angle 30^\circ$  A. The impedance is  $5\sqrt{2} \angle - 45^\circ \Omega$ . The phasor voltage is  $5I_m \sqrt{2} \angle - 15^\circ$  V peak value or  $5I_m \angle - 15^\circ = 12.5 \angle - 15^\circ$  V rms.

2. In the phasor diagram shown, phasor A is a current, the other phasors B, C, and D are voltages. To which of the following combinations of circuit elements does this phasor diagram apply?



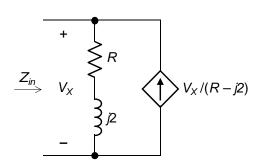
- A. R in series with L
- B. R in series with C
- C. R in parallel with C
- D. L in series with C
- E. L in parallel with C.

**Solution:** The phasor diagram represents a series RL circuit, Phasor **B** is the voltage across R. Phasor **C** is the voltage across L, leading the current by 90°, and phasor **D** is the voltage across the series combination.

3. Determine the input impedance  $Z_{in}$  assuming  $R = 2 \Omega$ .

Solution: If a test voltage source  $\mathbf{V}_{\mathsf{T}}$  is applied,  $\mathbf{I}_{\mathsf{T}}$ 

$$= \left(\frac{1}{R+j2} - \frac{1}{R-j2}\right) \mathbf{V_T}, \text{ or } Z_{in} =$$



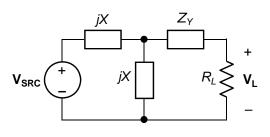
$$\frac{1}{\left(\frac{1}{R+j2} - \frac{1}{R-j2}\right)} = \frac{(R+j2)(R-j2)}{R-j2-R-j2} = \frac{R^2+4}{-j4} = j\left(1 + \frac{R^2}{4}\right)\Omega.$$
 Alternatively, the dependent

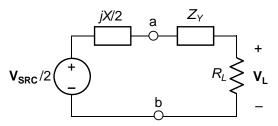
source is equivalent to an impedance -(R-j2) and  $Z_{in} = (R+j2)||[-(R-j2)]=$ 

$$-\frac{R^2 + 4}{j2} = j \left(\frac{R^2}{4} + 1\right) = j2 \Omega.$$

**4.** Determine  $Z_Y$  so that  $\mathbf{V_L}$  is in phase with  $\mathbf{V_{SRC}}$ , assuming  $X = -5 \Omega$  with  $R_L$  and  $\mathbf{V_{SRC}}$  unknown.

**Solution:** TEC as seen from terminals a and b will have  $Z_{Th} = jX/2$ . For  $V_L$  to be in phase with  $V_{SRC}$ ,  $Z_Y = -jX/2 = j2.5 \Omega$ 

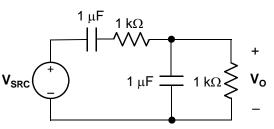




**5.** Determine  $V_0$  if  $\omega = 1$  krad/s and  $V_{SRC} = 3$  V.

**Solution:** 
$$\omega CR = 1$$
;

$$\frac{\mathbf{V_o}}{\mathbf{V_{SRC}}} = \frac{R/(1+j\omega CR)}{R/(1+j\omega CR) + R-j/\omega C} = \frac{R/(1+j)}{R/(1+j) + R-j/\omega C} = \frac{1/(1+j)}{1/(1+j) + 1-j} = \frac{1}{1+(1+j)(1-j)} = \frac{1}{1+1-j^2} = \frac{1}{3}; \mathbf{V_o} = \mathbf{V_{SRC}/3} = 1 \text{ V.}$$



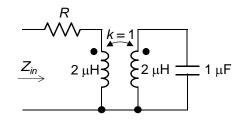
6. Two coils are wound on a core of high permeability. Coil 1 has 100 turns and coil 2 has 400 turns. A current of 1 A in coil 1, with coil 2 open circuited, produces a core flux of 0.5 mWb. Determine the magnitude of the core flux produced by a current of 0.8 A in coil 2, with coil 1 open circuited.

**Solution:** From the definition of mutual inductance,  $\frac{N_2\phi_{21}}{i_1} = \frac{N_1\phi_{12}}{i_2}$ , so that  $\phi_{12} = \frac{i_2}{i_1} \frac{N_2}{N_1} \phi_{21} = \frac{i_2}{i_1} \frac{N_2}{N_1} \phi_{21}$ 

$$\frac{0.8}{1} \frac{400}{100} \phi_{21} = 3.2 \phi_{21} = 3.2 \times 0.5 = 1.6 \text{ mWb}$$

7. Determine  $Z_{in}$ , assuming  $R = 10 \Omega$ , and  $\omega = 1 \text{ Mrad/s}$ .

**Solution:**  $M = k\sqrt{L \times L} = 2 \, \mu \text{H}$ . It follows that the series branches of the T-equivalent circuit are zero and the shunt branch is  $j\omega M = j2 \, \Omega$ ;  $-\frac{j}{\omega C} = -j$ . The parallel



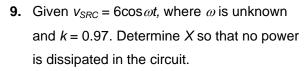
impedance of j2 and -j  $\Omega$  is  $2/(2-j) = -j2\Omega$ .  $Z_{in} = R - j2 = 10 - j2\Omega$ .

**8.** Determine the stored **magnetic energy** under dc conditions, assuming  $V_{SRC} = 1 \text{ V}$ .

**Solution:** The branch containing the capacitor carries no current under dc conditions. The current in the other two branches is  $V_{SRC}/0.5$  A and the stored magnetic energy is W =

$$\frac{1}{2} \left( L_1 I^2 + L_1 I^2 + 2M I^2 \right) =$$

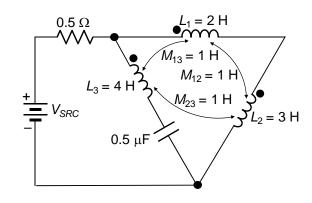
$$\frac{1}{2} \left( \frac{V_{SRC}}{0.5} \right)^2 (2 + 3 + 2 \times 1) = 14 V_{SRC}^2 = 14 \text{ J}.$$

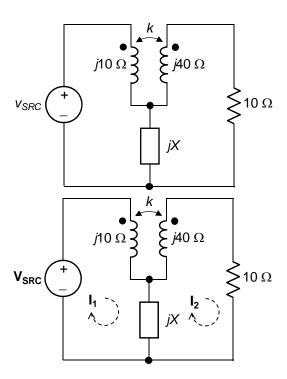


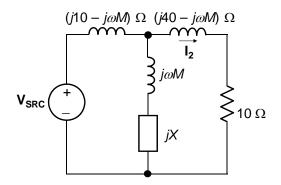
**Solution:** Considering mesh currents  $I_1$  and  $I_2$ , then for no power dissipation,  $I_2 = 0$ . The mesh-current equation for mesh 2 is:

$$-(j\omega M + jX)\mathbf{I}_{1} + (j40 + jX + 10)\mathbf{I}_{2} = 0$$
 For  $\mathbf{I}_{2}$  to be zero,  $\omega M + X = 0$ , or  $X = -\omega M = -\omega k\sqrt{L_{1}L_{2}} = -k\sqrt{(\omega L_{1})(\omega L_{2})} = -k\sqrt{400} = -20k = -0.97 \times 20 = -19.4 \ \Omega.$ 

Alternatively, it follows from the T-equivalent circuit that if  $X = -\omega M$  the shunt branch will have zero impedance so  $\mathbf{I_2} = 0$ .







**10.** Determine the input admittance  $Y_{in}$  assuming  $Z_L = 10 \angle 45^{\circ} \Omega$ .

**Solution:** It follows from the circuit shown that  $V_L = -2V_1$ , so that

 $\frac{V_L}{V_1} = -2$ . Since the ideal autotransformer does not dissipate

power, and  $V_L = -2V_1$ ,  $V_L \times I_L = V_1 \times I_1$ ,  $\frac{I_L}{I_1} = -\frac{1}{2}$ . It follows that

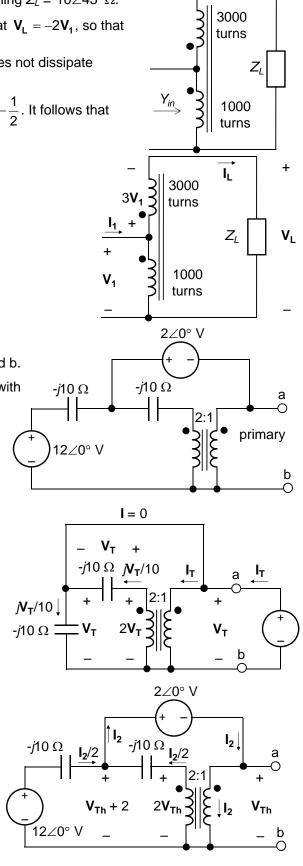
$$Y_{in} = \frac{I_1}{V_1} = \frac{4}{Z_L} = \frac{4}{10\angle 45^{\circ}} = 0.4\angle - 45^{\circ} \text{ S.}$$

**11.** Determine  $Z_{Th}$  looking into terminals a and b.

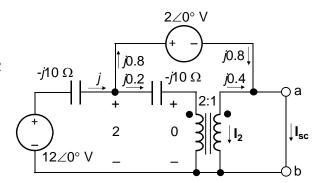
**Solution-***Method 1*: Apply a test voltage  $V_T$ , with the independent sources replaced by short circuits. The secondary voltage is  $V_T$  and the voltage is  $2V_T$ . The current through each capacitor is  $V_T/10$  as shown, so that the current in the short-circuit replacing the 2 V source is zero. For the ideal transformer,  $I_T$ 

= 
$$j2V_T/10$$
. It follows that  $\frac{V_T}{I_T} = \frac{5}{j} = -j5\Omega$ .

Method 2: Under open-circuit conditions, the currents and voltages will be as shown. The voltages across the two capacitors are of equal magnitude but opposite polarity. It follows that  $2V_{Th} = 12 \text{ V}$ , and  $V_{Th} = 6 \text{ V}$ .



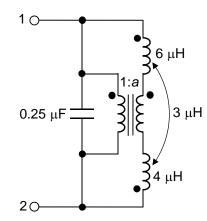
Under short circuit conditions, the currents and voltages will be as shown. It follows that  $I_{SC} = j1.2$  A. Hence,  $Z_{Th} = 6/j1.2$  = -j5  $\Omega$ .



**12.** Determine the turns ratio *a* so that Norton's admittance looking into terminals 1 and 2 is zero, assuming  $\omega = 1$  Mrad/s.

**Solution-***Method 1:* The impedances are:  $j\omega 6 = j6 \Omega$ ,  $j\omega 4 = j4 \Omega$ ,  $j\omega 3 = j3 \Omega$ , and  $1/j\omega C = 1/(j10^6 \times 0.25 \times 10^{-6}) = -j4 \Omega$ .

When a test source  $\mathbf{V}_{\mathsf{T}}$  is applied, the test current  $\mathbf{I}_{\mathsf{T}}$  should be zero. The voltages and currents in the circuit will be as shown.



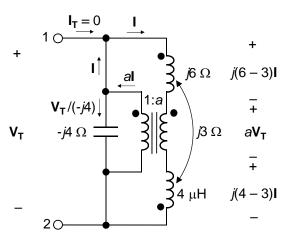
From KVL in the branch containing the coupled coils,

$$V_{T} = j(6-3)I + aV_{T} + j(4-3)I = aV_{T} + j4I \lor$$
, or  $(1-a)V_{T} = j4I$  (1)  
From KCL at node 1,  $aI = I + \frac{V_{T}}{-j4}$ , or  $\frac{V_{T}}{j4} = (1-a)I$  (2)

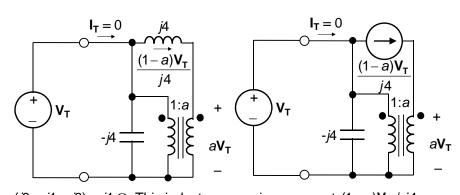
Dividing Equation 1 by Equation 2:

$$j4(1-a) = \frac{j4}{(1-a)}$$
,  $(a-1)^2 = 1$ ;  $a = 1 \pm 1$ ,

which gives a = 2.

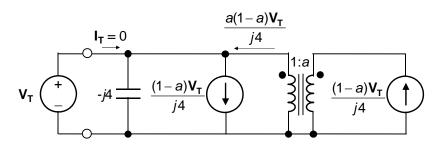


Method 2: The circuit can be redrawn as shown, where the two coupled coils in series have been replaced by the



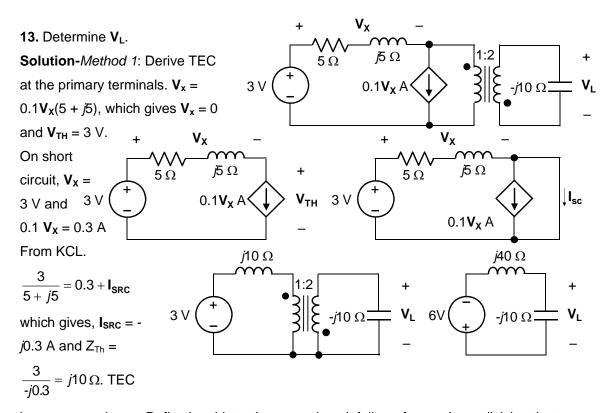
equivalent inductance (j6 + j4 - j6) =  $j4 \Omega$ . This inductance carries a current  $(1-a)\mathbf{V}_T / j4$ 

and can be replaced by a current source of this value in accordance with the substitution theorem. This source can then



be rearranged as two sources, as shown. From KCL,  $\frac{a(1-a)}{j4}\mathbf{V_T} = \frac{(1-a)}{j4}\mathbf{V_T} + \frac{\mathbf{V_T}}{-j4}$ ,  $a-a^2 = \frac{a(1-a)}{j4}\mathbf{V_T} + \frac{a(1-a)}{j$ 

1 - a - 1, which gives a = 0 or 2, so a must equal 2.



becomes as shown. Reflecting this to the secondary, it follows from voltage division that

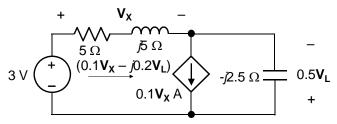
$$V_L = -\frac{j10}{j30} \times 6 = 2 \text{ V.}$$

Method 2: No reflections.

The primary voltage and current will be as shown in the figure. From KCL, the current in the  $(5 + j5) \Omega$ 

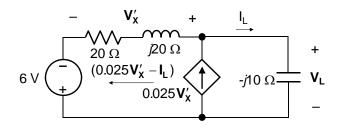
impedance is  $(0.1\mathbf{V}_{X} - 2\mathbf{I}_{L})$ , so that  $\mathbf{V}_{X} = (0.1\mathbf{V}_{X} - 2\mathbf{I}_{L})(5 + j5)$  and  $\mathbf{I}_{L} = \mathbf{V}_{L}/(-j10) = j0.1\mathbf{V}_{L}$ . Substituting for  $\mathbf{I}_{L}$ ,  $\mathbf{V}_{X} = (0.1\mathbf{V}_{X} - j0.2\mathbf{V}_{L})(5 + j5) = 0.5\mathbf{V}_{X} + j0.5\mathbf{V}_{X} - j(1 + j)\mathbf{V}_{L}$ , or,  $0.5(1 - j)\mathbf{V}_{X} = (1 - j)\mathbf{V}_{L}$ , which gives,  $\mathbf{V}_{X} = 2\mathbf{V}_{L}$ . From KVL on the primary side,  $0.5\mathbf{V}_{L} + 3 - \mathbf{V}_{X} = 0$ ; substituting for  $V_X$ , 1.5 $V_L$  = 3 and  $V_L$  = 2 V.

Method 3: The capacitive branch is reflected to the primary side together with  $\mathbf{V_L}$ . From KCL, the current through the (5 +j5)  $\Omega$ 



impedance is  $0.1 \mathbf{V}_{X} - 0.5 \mathbf{V}_{L} / -j2.5 = 0.1 \mathbf{V}_{X} - j0.2 \mathbf{V}_{L}$ , so that  $\mathbf{V}_{X} = (0.1 \mathbf{V}_{X} - j0.2 \mathbf{V}_{L})(5 + j5) = (0.5 \mathbf{V}_{X} - j\mathbf{V}_{L})(1 + j) = 0.5 \mathbf{V}_{X} + j0.5 \mathbf{V}_{X} - j\mathbf{V}_{L}(1 + j)$ , or  $0.5(1 - j)\mathbf{V}_{X} = (1 - j)\mathbf{V}_{L}$ , which gives  $\mathbf{V}_{X} = 2 \mathbf{V}_{L}$ . From KVL on the primary side,  $0.5 \mathbf{V}_{L} + 3 - \mathbf{V}_{X} = 0$ ; substituting for  $\mathbf{V}_{X}$ ,  $1.5 \mathbf{V}_{L} = 3$  and  $\mathbf{V}_{L} = 2 \mathbf{V}$ .

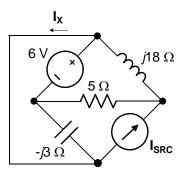
Method 4: The primary circuit is reflected to the secondary side. The  $(5 + j5) \Omega$  is multiplied by 4. The source voltage and  $\mathbf{V}_{\mathbf{X}}'$  are multiplied by 2 and reversed in sign. To maintain the same dependency relation, with the dependent source still



on the primary side, k is divided by 2 and reversed in sign. When reflected to the secondary side, this current source must be divided by 2. The overall effect is to divide k by 4 and reverse the sign of the current source as shown. It follows that  $\mathbf{V}_{\mathbf{X}}' = (0.025\,\mathbf{V}_{\mathbf{X}}' - \mathbf{I}_{\mathbf{L}})(20 + j20) = (0.5\,\mathbf{V}_{\mathbf{X}}' - j2\mathbf{V}_{\mathbf{L}})(1 + j) = 0.5\,\mathbf{V}_{\mathbf{X}}' + j0.5\,\mathbf{V}_{\mathbf{X}}' + 2\mathbf{V}_{\mathbf{L}}(1 - j)$ , or,  $0.5\,\mathbf{V}_{\mathbf{X}}'(1 - j) = 2\mathbf{V}_{\mathbf{L}}(1 - j)$ , which gives  $\mathbf{V}_{\mathbf{X}}' = 4\mathbf{V}_{\mathbf{L}}$ . From KVL,  $\mathbf{V}_{\mathbf{L}} - \mathbf{V}_{\mathbf{X}}' + 6 = 0$ . Substituting for  $\mathbf{V}_{\mathbf{X}}'$ ,  $\mathbf{V}_{\mathbf{L}} = 2\,\mathbf{V}$ .

- **3.** Determine  $I_X$  assuming  $I_{SRC} = j A$ .
  - A. *j*6 A
  - B. -*j*3 A
  - C. /3 A
  - D. -j6 A
  - E. *j*4 A

**Solution:** The voltage across the -j3  $\Omega$  capacitor is 6 V and the current through this capacitor, directed upwards is j2 A. It follows that  $I_X = I_{SRC} + j2 = j3$  A.



- **5.** Two coils are tightly coupled to a high-permeability core, so that the leakage flux is negligibly small. If coil 1 has 100 turns and an inductance of 10 mH, and the mutual inductance is 12.5 mH, determine the number of turns of coil 2.
  - A. 125
  - B. 250
  - C. 150
  - D. 175
  - E. 200

Solution: From the definitions of self and mutual inductance, with negligible leakage flux,

$$L_1 = \frac{N_1 \phi_{21}}{i_1}$$
 and  $M = \frac{N_2 \phi_{21}}{i_1}$ . It follows that  $N_2 = \frac{M}{L_1} N_1 = 10M = 125$ .

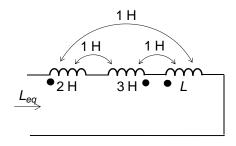
- **6.** Determine the inductance of coil 2 of the preceding problem.
  - A. 22.5 mH
  - B. 30.63 mH
  - C. 15.63 mH
  - D. 40 mH
  - E. 50.63 mH

**Solution:** Since the coils are tightly coupled to the core, k = 1, so that  $M^2 = L_1 L_2$ , or

$$L_2 = \frac{M^2}{L_1} = 0.1 M^2$$
 mH. It also follows from the solution of the preceding problem that

$$N_1 = \frac{M}{L_2} N_2$$
. Dividing,  $L_2 = L_1 \left(\frac{N_2}{N_1}\right)^2 = 0.1 M^2 = 0.1 \times (12.5)^2 = 15.625 \text{ mH}.$ 

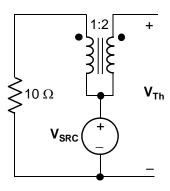
- **9.** Determine  $L_{eq}$  if L = 1 H.
  - A. 6 H
  - B. 4 H
  - C. 8 H
  - D. 7 H
  - E. 5 H

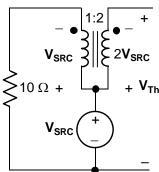


**Solution:** Consider that a voltage **V** is applied, causing a current **I** to flow.  $\mathbf{V} = j\omega \mathbf{I}[(2-1+1) + (3-1-1) + (L+1-1)]; L_{eq} = 3 + L = 4 \text{ H}.$ 

**10.** Determine  $V_{Th}$ , assuming  $V_{SRC} = 1 \angle 0^{\circ} \text{ V}$ 

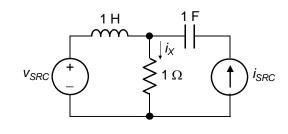
**Solution:** On open circuit, no current flows. The primary voltage is  $V_{SRC}$  as shown, and  $V_{Th} = -V_{SRC} = -1 \angle 0^{\circ} \text{ V}$ 





**17.** Given  $v_{SRC} = \cos t \, V$  and  $i_{SRC} = \sin 2t \, A$ .

- (a) Derive the expression for  $i_X$  in the time domain.
- (b) Determine the power dissipated in the resistor.



**Solution:** (a) Let the amplitude of  $v_{SRC}$  and  $i_{SRC}$  be K. With the current source replaced by an

open circuit, 
$$\mathbf{I_{x1}} = \frac{K \angle 0^{\circ}}{1} \frac{1}{1+j} = \frac{K}{2} (1-j)$$
;  $i_{X1} = \frac{K}{\sqrt{2}} \cos(t-45^{\circ})$  A. With the current source

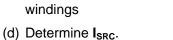
replaced by a short circuit, 
$$\mathbf{I_{x2}} = K \angle 0^{\circ} \frac{j2}{1+j2} = \frac{2K}{\sqrt{5}} \angle (90^{\circ} - \tan^{-1} 2)$$
;  $i_{X2} = \frac{2K}{\sqrt{5}} \sin(2t + 26.57^{\circ})$ 

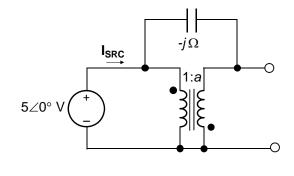
A. Hence, 
$$i_X = \frac{K}{\sqrt{2}}\cos(t - 45^\circ) + \frac{2K}{\sqrt{5}}\sin(2t + 26.57^\circ) = 0.71\cos(t - 45^\circ) +$$

 $0.89 \sin(2t + 26.57^{\circ})$  A.

(b) Power dissipated is 
$$P = \frac{1}{2} \left( \frac{K^2}{2} + \frac{4K^2}{5} \right) = 0.65 K^2 = 0.65 W.$$

- **18.** Given the circuit shown, with a = 2.
  - (a) Determine the current in the capacitor
  - (b) Replace the capacitor by a current source, in accordance with the substitution theorem
  - (c) Rearrange the current source as two current sources across the transformer windings





**Solution:** (a) The voltage across the capacitor is 5(1 + a) V. The current through the capacitor is j5(1 + a) = j15 A directed from primary to secondary.

(b) (c) |SRC| |5a(1+a)| A  $|5 \le 0^{\circ}| V | + a = 0$   $|5 \le 0^{\circ}| V | + a = 0$   $|5 \le 0^{\circ}| V | + a = 0$   $|5 \le 0^{\circ}| V | + a = 0$ 

(d) It follows that  $I_{SRC} = j5(a + 1)^2 = j45 \text{ A}.$