## DO NOT OPEN THIS EXAM BEFORE YOU ARE TOLD TO BEGIN

NAME
ID Number $\qquad$

Useful information
$\varepsilon_{0}=8.85 \times 10^{-12} \mathrm{C}^{2} / \mathrm{N} . \mathrm{m}^{2}$.

| Grading |  |
| :---: | :--- |
| Problem 1 |  |
| Problem 2 |  |
|  |  |
| TOTAL |  |

## Problem 1 ( $65 \%$ )

## 1. Gauss's Law and Capacitance

A solid, insulating sphere of radius $a$ has a uniform charge density $\rho$ and a total charge $Q$. Concentric with this sphere is an uncharged, conducting hollow sphere whose inner and outer radii are $b$ and $c$, as shown in the Figure below.

(a) (10) Find the magnitude of the electric field in the region $r<a$
(b) (10) Show that the magnitude of the electric field in the region $a<r<b$ is $E=\rho a^{3} / 3 \varepsilon_{0} r^{2}$
(c) (5) Find the magnitude of the electric field in the region $b<r<c$
(d) (10) Find the magnitude of the electric field in the region $r>c$
(e) (15) Determine the induced charge per unit area on the inner and outer surfaces of the hollow sphere.
(f) (10) Determine the potential difference between $a$ and a position $r$ such that $a<r<b$
(g) (5) Compare the electric field inside this capacitor to the one produced by two parallel plates.
2. (35) Electrostatic acceleration

We want to accelerate a particle, with charge $Q$ and mass $M$, just by putting it close to a ring biased to $Q$ and held fixed. The charge is initially put at the center of the ring.

(a) (10) Determine the expression of the electric potential at a point on the axis of the ring at a position $x$ from the center.
(b) (5) Deduce the electric potential at the center of the ring.
(c) (5) Find the potential energy of the particle at the initial and final positions.
(d) (10) Assume that the charge has a mass $M$, show that the ultimate speed of the point charge is

$$
v=\left(\frac{2 k_{e} Q^{2}}{M R}\right)^{1 / 2}
$$

(e) (5) the ring is now put horizontally, determine the $Q$ needed so as the charge will remain in equilibrium at an elevation equal to $x_{0}$

## SCRATCH PAPER

Nothing on this page will be gradedCheck if solution is continued on the back.

