# FACULTY OF ENGINEERING AND ARCHITECTURE <br> AMERICAN UNIVERSITY OF BEIRUT <br> FALL 2011-2012 <br> FINAL EXAM <br> DIGITAL SYTEMS DESIGN (EECE320)- Dr. Youssef Nasser 

January 16, 2011

NAME: $\qquad$ ID: $\qquad$

## CLOSED BOOK (2 HOURS)

WRITE YOUR NAME AND ID NUMBER IN THE SPACE PROVIDED ABOVE.

CALCULATORS ARE NOT ALLOWED.

PROVIDE YOUR ANSWERS IN THE SPACE PROVIDED ON THE QUESTION SHEET.
THE SCRATCH BOOKLET WILL NOT BE CONSIDERED IN GRADING.

| Problem | Total Points | Earned Points |
| :---: | :---: | :---: |
| 1 | 13 |  |
| 2 | 10 |  |
| 3 | 10 |  |
| 4 | 4 |  |
| 5 | 22 |  |
| 6 | 7 |  |
| 7 | 8 |  |
| 8 | 8 |  |
| 9 | 6 |  |
| 10 | 12 |  |
| Total | 100 |  |

## Problem 1 [13 points]

Given $F=\Sigma_{A, B, C, D}(0,2,4,5,6,7,8,10,13,15)$ and $G=\Pi_{A, B, C, D}(0,2,4,5,6,7,8,10,13,15)$
A. Fill in the corresponding Karnaugh maps of function F and G


Function F


Function G
B. Indicate the Essential Prime Implicants of F
$\qquad$
C. Indicate all other Prime Implicants of F
$\qquad$
D. Write the Minimal Sum of Products of F
$\qquad$
E. Deduce from G the Minimal Maximum of Products of G.
$\qquad$

## Problem 2 [10 points]

A circuit designer has optimized his design for the use of $\mathrm{J}-\mathrm{K}$ flip flop while $\mathrm{J}=\mathrm{XW}+\mathrm{W}$ ' and $K=X^{\prime} W^{\prime}+W Y X ; X, Y$ and $W$ are three inputs of the circuit. While trying to implement his circuit, the designer finds that he was restricted to the use of a T Flip-Flop with enable and a 3-to-8 decoder only.
Write down the expression of E and complete the following diagram to achieve this purpose.
$\mathrm{E}=$ $\qquad$


## Problem 3 [10 points]

1. We would like to analyze the following clocked synchronous state machine.

A. Write the next state equations for $\mathrm{z}_{1}$ and $\mathrm{z}_{2}$.

$$
\begin{aligned}
& \mathrm{z}_{1} *= \\
& \mathrm{z}_{2} *= \\
& \hline
\end{aligned}
$$

B. Draw the transition/output table.

|  | XY |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{z}_{\mathbf{2}} \mathbf{z}_{\mathbf{1}}$ | $\mathbf{0 0}$ | $\mathbf{0 1}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ | $\mathbf{Z T}$ |
| 00 |  |  |  |  |  |
| 01 |  |  |  |  |  |
| 11 |  |  |  |  |  |
| 10 |  |  |  |  |  |
|  | $\mathbf{z}_{\mathbf{2}}{ }^{*} \mathbf{z}_{\mathbf{1}}{ }^{*}$ |  |  |  |  |

C. Draw the state diagram

## Problem 4 [4 points]

It is required to design a combinational network that converts from the (2421) code to the BCD code written in the reverse order as given in the truth table below. Unused code words should be considered as don't cares to simplify your design.

| Digit | A | B | C | D | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| 2 | 0 | 0 | 1 | 0 | 1 | 0 | 1 |
| 3 | 0 | 0 | 1 | 1 | 1 | 0 | 0 |
| 4 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| 5 | 1 | 0 | 1 | 1 | 0 | 1 | 0 |
| 6 | 1 | 1 | 0 | 0 | 0 | 0 | 1 |
| 7 | 1 | 1 | 0 | 1 | 0 | 0 | 0 |

A. Plot the outputs of the network on the following Karnaugh maps.

B. The expressions for $\mathrm{X}, \mathrm{Y}$ and Z are:

$$
\mathrm{X}=
$$

$\qquad$
$Y=$ $\qquad$

$$
\mathrm{Z}=
$$

$\qquad$

## Problem 5[22 points]

Design a sequential circuit with 2 JK flip-flops A and B and 3 inputs $\mathrm{E}, \mathrm{F}$ and G . If $\mathrm{E}=0$ or $\mathrm{F}=0$, the circuit remains in the same state regardless of G . When $\mathrm{E}=1, \mathrm{~F}=1$ and $\mathrm{G}=0$, the circuit goes through the transitions from 00 to 11 , to 01,10 , back to 00 , and repeats. When $\mathrm{E}=1, \mathrm{~F}=1$ and $\mathrm{G}=1$ the circuit goes through the transitions from 00 to 10 , to 00 and repeats while the next state of 01 is 01 and that of 11 is 11 .
A. Fill the transition and excitation tables below when $\mathrm{G}=0$ and then when $\mathrm{G}=1$.
$\underline{\mathrm{G}=0}$

|  | EF |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{A B}$ | $\mathbf{0 0}$ | $\mathbf{0 1}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |
|  | $\mathbf{A}^{*} \mathbf{B}^{*}$ |  |  |  |


|  | EF |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{A B}$ | $\mathbf{0 0}$ | $\mathbf{0 1}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |
|  | $\mathbf{J}_{\mathbf{A}} * \mathbf{K}_{\mathbf{A}}{ }^{*} \mathbf{J}_{\mathbf{B}} * \mathbf{K}_{\mathbf{B}} *$ |  |  |  |

$\mathrm{G}=1$

|  | EF |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{A B}$ | $\mathbf{0 0}$ | $\mathbf{0 1}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 | $\mathbf{A}^{*} \mathbf{B}^{*}$ |  |  |  |
|  |  |  |  |  |


|  | EF |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{A B}$ | $\mathbf{0 0}$ | $\mathbf{0 1}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |
|  | $\mathbf{J}_{\mathbf{A}} * \mathbf{K}_{\mathbf{A}}{ }^{*} \mathbf{J}_{\mathbf{B}} * \mathbf{K}_{\mathbf{B}} *$ |  |  |  |

B. Fill the Karnaugh maps below corresponding to $\mathrm{J}_{\mathrm{A}}, \mathrm{K}_{\mathrm{A}}$ and $\mathrm{J}_{\mathrm{A}}, \mathrm{K}_{\mathrm{B}}$ and find their expressions.


$$
\mathrm{J}_{\mathrm{A}}=
$$

$\qquad$


$\mathrm{K}_{\mathrm{A}}=$ $\qquad$

$\mathrm{G}=0$

$\mathrm{G}=1$
$\mathrm{J}_{\mathrm{B}}=$ $\qquad$

$\underline{\mathrm{G}=0}$

$\mathrm{G}=1$
$\mathrm{K}_{\mathrm{B}}=$ $\qquad$
C. Draw the circuit design of this Finite State Machine. We assume that the output is set to 1 when E, F and G are ON and both Flips Flops are set to 1.

## Problem 6 [7 points]

A memory is usually specified by the number of words times the number of bits per word. If we have a memory of 128 Kx 32 , how many address lines does the memory have: $\qquad$ how many data lines does it have: $\qquad$ , and how many bits in total does it have (as a power of 2): $\qquad$
A $256 \mathrm{~K} \times 64$ RAM chip is designed in such a way that its cell array is square, i.e., it contains an equal number of bits per row and column. A row decoder is used to select a row, and a column decoder is used to select the appropriate word within a column. What is the number of address bits needed to access a row: $\qquad$ and what is the number of address bits needed to access 64 bits within a column: $\qquad$

## Problem 7 [8 points]

For the following circuit, complete the corresponding timing diagram shown below. Assume all flip-flops are initialized to zero.


X


A $\qquad$

B $\qquad$

C

## Problem 8 [8 points]

Using T flip-flops with Enable, design a counter that counts as follows: $0,3,1,4,2,5,8,6,9,7,0$, etc. In case of an illegal state like $10,11,12,13,14$, and 15 we should use minimum risk and move the counter to the initial state of 0 .
A. Fill the next state table and excitation tables.

| A | B | C | D | A* | B* | C* | D* | E1 | E2 | E3 | E4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |
| 0 | 0 | 0 | 1 |  |  |  |  |  |  |  |  |
| 0 | 0 | 1 | 0 |  |  |  |  |  |  |  |  |
| 0 | 0 | 1 | 1 |  |  |  |  |  |  |  |  |
| 0 | 1 | 0 | 0 |  |  |  |  |  |  |  |  |
| 0 | 1 | 0 | 1 |  |  |  |  |  |  |  |  |
| 0 | 1 | 1 | 0 |  |  |  |  |  |  |  |  |
| 0 | 1 | 1 | 1 |  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |
| 1 | 0 | 0 | 1 |  |  |  |  |  |  |  |  |

B. Derive the excitation equations for E1, and E4.


E1


E4
E1 = $\qquad$
E4 = $\qquad$

## Problem 9 [6 points]

Using a Moore machine, design a sequence detector with one input X and one output Z where the output is asserted whenever the input sequence 010 has been observed as long as the sequence 100 has never been seen. Draw the state diagram in the space below.

## Problem 10 ( 12 points)

Write a VHDL code to implement a 3-bits Gray counter (equivalent to Gray decoder).

