American University of Beirut Faculty of Engineering and Architecture Department of Electrical and Computer Engineering

EECE 290 – Analog System Processing – Spring 2009 **EXAM 1 – Friday March 27, 2009** Lama Hamandi

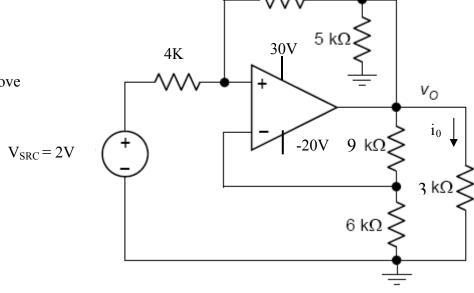
Name:	ID Number:

## **Read the following instructions carefully:**

- The duration of the exam is **90 minutes**.
- The exam consists of 10 pages and 15 questions. You can use the question sheets for scratch.
- All questions have the same weight. Total achievable points: **100**.
- **No questions** will be answered during the exam.
- Programmable calculators are not allowed.
- Provide your answers on the computer card only using a pencil.
- Return the computer card attached to the question sheet.
- Mark with a pencil your last name.
- Mark with a pencil your ID number.
- You don't need to fill the field "Test ID".
- When using an eraser, make sure you erased well.
- When you finish the exam bring all of your belongings to the front of the room and hand in the exam. Then leave the room immediately.
- Enjoy and Good Luck!

$f(t) \ (t > 0 -)$	F(s)	$f(t) \ (t > 0 - )$	F(s)
$\delta(t)$	1 .	df(t)	aF(a) f(0=)
u(t)	<u>1</u>	-dt	$sF(s) - f(0^-)$
	<i>S</i>	$\int_{-\infty}^{t}$	F(s)
t	$\frac{1}{s^2}$	$\int_0^t f(x)  dx$	$\frac{1}{s}$
$e^{-at}$	1	f(t-a)u(t-a), a>0	$e^{-as}F(s)$
Ü	s + a	$e^{-at}f(t)$	F(s+a)
$\sin \omega t$	$\frac{\omega}{s^2 + \omega^2}$	f(at), a > 0	$\frac{1}{a}F\left(\frac{s}{a}\right)$
$\cos \omega t$	$\frac{s}{s^2 + \omega^2}$	tf(t)	$-\frac{dF(s)}{ds}$

- 1. Determine the current  $i_0$  in mA.
- A. 4
- B. 2.5
- C. 6.7
- D. 5
- E. None of the above



 $8~\text{k}\Omega$ 

2. In the previous problem, what is the range of the  $V_{SRC}$  to keep the op amp working in the linear region.

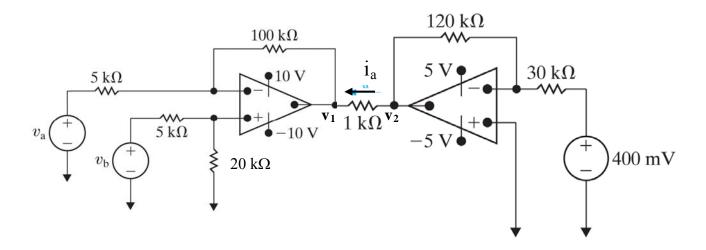
A. 
$$-4V \le V_{SRC} \le 3V$$

$$B.~-2V \le V_{SRC} \le 3V$$

$$C. -3V \le V_{SRC} \le 2V$$

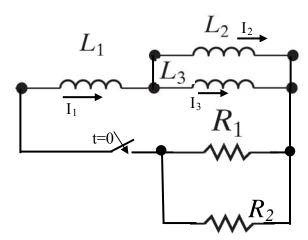
$$D. \quad \text{-}3V \leq V_{SRC} \leq 4V$$

- 3. Determine the voltage  $v_1$  in Volts given that  $v_a$  = 0.1V and  $v_b$  = 0.2V .
  - A. 1.36 V
  - B. 3.4 V
  - C. 2.2 V
  - D. 4.1 V
  - E. None of the above



- 4. Determine the current  $i_a$  in mA in the previous problem. Hint: start by finding  $v_2$ 
  - A. 3.8mA
  - B. -3.8mA
  - C. 2.96mA
  - D. -2.96 mA
  - E. None of the above

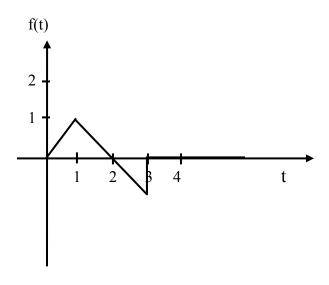
5.



The switch closes at time t = 0, with initial currents in the inductors  $I_1(0^-)=5A$ ,  $I_2(0^-)=3A$ ,  $I_3(0^-)=2A$ . Given that  $L_1 = 3mH$ ,  $L_2 = 4mH$ ,  $L_3 = 4mH$ ,  $R_1 = 5K\Omega$ ,  $R_2 = 20K\Omega$ . Find the total energy dissipated in  $R_1$  and  $R_2$ .

- A. 87.5 mW
- B. 43.75 mW
- C. 31.25 mW
- D. 62.5 mW
- E. None of the above
- 6. What is the energy trapped in the system of problem 5 as  $t \rightarrow \infty$ .
  - A. 1 mW
  - B. 1.5 mW
  - $C. \quad 2 \ mW$
  - D. 2.5 mW
  - E. None of the above

7. Find the Laplace transform of **df/dt**.



$$A. \ \frac{1 - 2e^{-2s} + (s-1)e^{-3s}}{s}$$

$$B. \ \frac{1 - 2e^{-s} + (1 + s)e^{-3s}}{s}$$

$$C. \quad \frac{0.5 - 1.5e^{-2s} + (1+s)e^{-4s}}{s}$$

$$D. \quad \frac{0.5 - 2.5e^{-3s} + (s-1)e^{-4s}}{s}$$

*E.* None of the above

8. Given that the hyperbolic sine is:  $\sinh at = \frac{e^{at} - e^{-at}}{2}$ . Find  $\mathcal{L}\{e^{-3t} \sinh 2t\}$ .

A. 
$$3/(s^2+4s-5)$$

B. 
$$s/(s^2+6s-5)$$

C. 
$$2/(s^2+6s+5)$$

D. 
$$s / (s^2 + 4s + 5)$$

9. Find the Laplace transform of  $f(t) = (2t + 3t^2)^2$ 

A. 
$$(8s^2 + 72s + 216)/s^5$$

B. 
$$(24s^2 + 6s + 2)/s^5$$

C. 
$$(18s^2 + 72s + 96)/s^5$$

D. 
$$(24s^2 + 12s + 8)/s^5$$

E. None of the above

10. Given that 
$$F(s) = \frac{8s^2 + 4s + 6}{(2s+3)(s+4)}$$
, find f(t), the inverse Laplace of F(s).

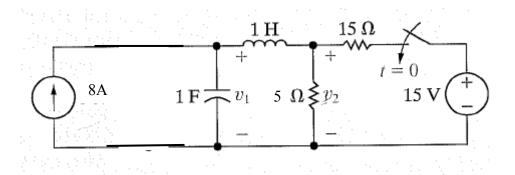
A. 
$$4t + (3.4 e^{-1.5t} - 22.4 e^{-4t})u(t)$$

B. 
$$4\delta(t) + (3.6 e^{-1.5t} - 23.6 e^{-4t})u(t)$$

C. 
$$(7.2 e^{-1.5t} - 23.6 e^{-4t})u(t)$$

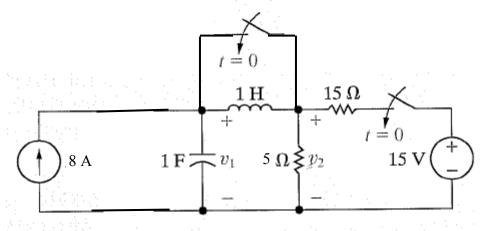
D. 
$$4\delta(t) + (3.4 e^{-1.5t} - 22.4 e^{-4t})u(t)$$

11. The switch has been open for a long time. It closes at t=0. Find  $v_2(0^+)$ .



- A. 22.5V
- B. 15 V
- C. 40 V
- D. 33.75V
- E. None of the above

12. The switches have been open for a long time. They close at t=0. Find  $V_1(s)$ .



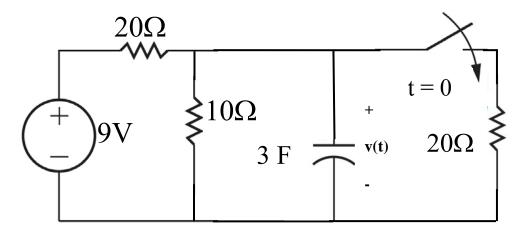
A. 
$$(40s + 5) / (s^2 + 3.75 s)$$

B. 
$$(25s + 6) / (s^2 + 0.27 s)$$

C. 
$$(40s + 6) / (s^2 + 0.27 s)$$

D. 
$$(25s + 5) / (s^2 + 3.75 s)$$

13. The switch closes at t=0. Find v(t) in volts for  $t \ge 0$ , t is in seconds..



A. 
$$2.25 + 0.75e^{-0.067t}$$

B. 
$$2.75 + 0.5e^{-0.033t}$$

C. 
$$2.5 + 1.5 e^{-0.05t}$$

D. 
$$3 + 2 e^{-0.1t}$$

E. None of the above

14. The switch opens again at t = 10sec. Find v(t) for  $t \ge 10$ sec.

$$A.\ 2-0.63\ e^{\text{-0.067(t-10)}}$$

B. 
$$4 - 0.6 e^{-0.038(t-10)}$$

$$C.\ 2.5-0.5\ e^{\text{-}0.067(t-10)}$$

D. 
$$3 - 0.37 e^{-0.05(t-10)}$$

- 15. For the following circuit, L = 8H, C = 2F,  $R = 10\Omega$ . Choose the right answer:
- A. The response is overdamped
- B. The response is critically damped.
- C. The response is underdamped.
- D. This is the natural response of parallel RLC circuit.
- E. None of the above.

