

1. A 100 V/m plane wave of frequency 300 MHz travels in the +z-direction in an infinite, lossless medium having  $\epsilon_r=9$ ,  $\mu_r=1$ , and  $\sigma=0$ . Determine the time domain expression for H field vector knowing that the direction of the vector E is along x-axis.

- a.  $(5/2\pi) \cos(600\pi \cdot 10^6 t - 6\pi z) a_x$  (A/m)
- b.  $(5/2\pi) \cos(600\pi \cdot 10^6 t - 6\pi z) a_y$  (A/m)
- c.  $(5/\pi) \cos(600\pi \cdot 10^6 t - 6\pi z) a_x$  (A/m)
- d.  $(2\pi/5) \cos(600\pi \cdot 10^6 t - 6\pi z) a_y$  (A/m)
- e. None of the above

2. A plane wave is traveling in the x-direction in a lossless medium, with a 100 V/m electric field in the z-direction. Given that the wavelength is 25 cm and the velocity of propagation is  $2 \cdot 10^8$  m/s, determine the relative permittivity of the medium. Assume  $\mu_r=1$ .

- a. 11/4
- b. 7/4
- c. 15/4
- d. 9/4
- e. None of the above

3. In problem 2, express the electric field vector in the time domain

- a.  $(100) \cos(1.6\pi \cdot 10^9 t - 8\pi x) a_z$  (V/m)
- b.  $(100) \cos(1.6\pi \cdot 10^9 t - 8\pi z) a_x$  (V/m)
- c.  $(100) \cos(1.6\pi \cdot 10^3 t - 8\pi x) a_z$  (V/m)
- d.  $(100) \cos(1.6\pi \cdot 10^3 t - 8\pi z) a_x$  (V/m)
- e. None of the above

4. Determine the polarization of the following plane wave:

$$E = 1 \cos(\omega t + \beta z) a_x - 1 \sin(\omega t + \beta z) a_y$$

- a. left-circular
- b. right-circular
- c. left-elliptical
- d. right-elliptical
- e. None of the above

5. For a plane wave propagating in the z-direction in air:

$$E(z) = (30 - j40)e^{-j\pi z} a_x + (20 + j10)e^{-j\pi z} a_y$$

Calculate  $E(1/3 \text{ m}, 5 \text{ ns})$

- a.  $E = 75.4a_x - 33.12a_y$
- b.  $E = -46a_x - 12.32a_y$
- c.  $E = -53a_x - 27.45a_y$
- d.  $E = -23a_x + 6.16a_y$
- e. None of the above

6. In a medium characterized by  $\sigma = 0$ ,  $\mu = \mu_0$ ,  $\epsilon = 4\epsilon_0$ , and

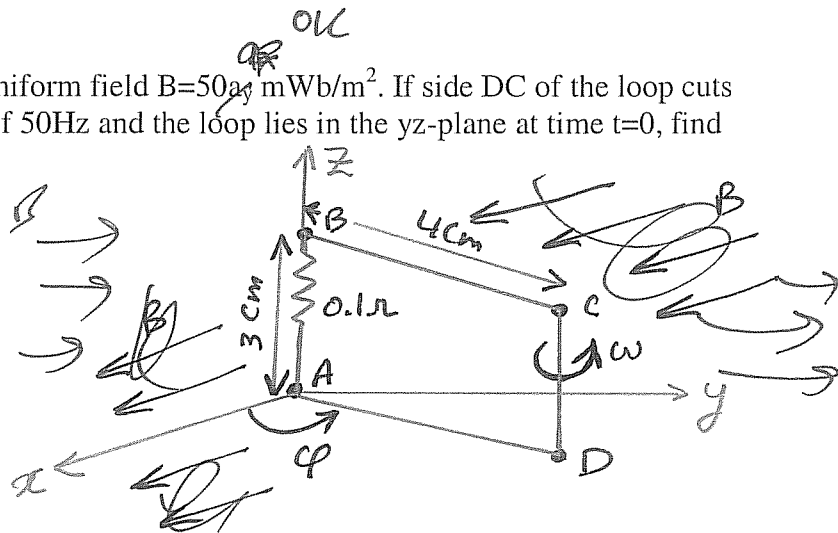
$$E = 20 \sin(10^8 t - \beta z) a_y \text{ (V/m)}$$

calculate  $H$ .

- a.  $\pm (5/3\pi) \sin [10^8 t \pm (7/3)z] a_y \text{ A/m}$
- b.  $\pm (2/3\pi) \sin [10^8 t \pm (2/3)z] a_x \text{ A/m}$
- c.  $\pm (1/3\pi) \sin [10^8 t \pm (2/3)z] a_x \text{ A/m}$
- d.  $\pm (7/3\pi) \sin [10^8 t \pm (5/3)z] a_x \text{ A/m}$
- e. None of the above

7. The loop shown is inside a uniform field  $B = 50 a_y \text{ mWb/m}^2$ . If side DC of the loop cuts the flux lines at the frequency of 50Hz and the loop lies in the yz-plane at time  $t=0$ , find the induced current at  $t=3 \text{ ms}$ .

- a.  $-0.1108 \text{ A}$
- b.  $-0.173 \text{ A}$
- c.  $-0.223 \text{ A}$
- d.  $-0.087 \text{ A}$
- e. None of the above



8. A spherical capacitor consists of an inner conducting sphere of radius  $R_i$  and an outer conductor with a spherical inner wall of radius  $R_o$ . The space in between is filled with a dielectric of permittivity  $\epsilon$ . Determine the capacitance.

- a.  $(2\pi\epsilon)/(1/R_o - 1/R_i)$
- b.  $(6\pi\epsilon)/(1/R_i - 1/R_o)$
- c.  $(4\pi\epsilon)/(1/R_i - 1/R_o)$
- d.  $(3\pi\epsilon)/(1/R_o - 1/R_i)$
- e. None of the above

9. If  $E_s = 10e^{j4x} a_y$ , which of these is not a correct representation of  $E$ ?

- a.  $\text{Im}(E_s e^{j\omega t})$
- b.  $10 \cos(\omega t + j4x) a_y$
- c.  $10 \sin(\omega t + 4x) a_y$
- d.  $\text{Re}(E_s e^{j\omega t})$
- e. None of the above

10. A section of lossless coaxial cable having  $R_c = 50 \Omega$  and  $u = 200 \text{ m}/\mu\text{s}$  is terminated in a short circuit and operated at a frequency of 10 MHz. Determine the shortest length of the lines such that, at the input terminals, the line appears to be 100-pF capacitor.

- a. 8.23 m
- b. 2.44 m
- c. 8.65 m
- d. 5.97 m
- e. None of the above

11. An antenna having an input impedance at 100 MHz of  $(72 + j40) \Omega$  is connected to a 100-MHz generator via a section of 300- $\Omega$  air filled line of length 1.75 m. Determine the voltage reflection coefficient at the line input terminals.

- a.  $0.87 \angle -75.3^\circ$
- b.  $0.43 \angle -175.4^\circ$
- c.  $0.73 \angle -245.8^\circ$
- d.  $0.62 \angle -256.09^\circ$
- e. None of the above

12. In problem 11, calculate the average incident power delivered to the antenna at the sending end of the line by a generator with source voltage of 10V and a source impedance of 50  $\Omega$ .

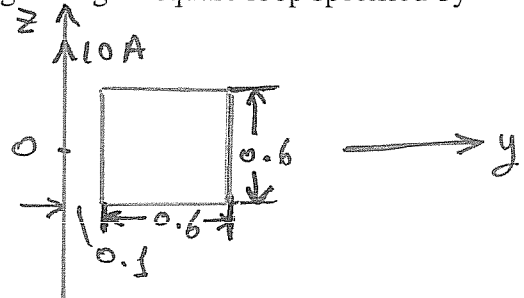
- a. 89.22 mW
- b. 47.67 mW
- c. 76.58 mW
- d. 65.28 mW
- e. None of the above

13. Determine the work done in carrying a  $+5(\mu C)$  charge from  $P_1(1,2,-4)$  to  $P_2(-2,8,-4)$  in the field  $E=a_x y + a_y x$  along the straight line joining  $P_1$  and  $P_2$ .

- a.  $120 \mu J$
- b.  $90 \mu J$
- c.  $70 \mu J$
- d.  $61 \mu J$
- e. None of the above

14. A direct current  $I=10A$  flows in an infinitely long wire of radius 2 mm along the z-axis. Determine the total magnetic flux passing through a square loop specified by  $z=\pm 0.3$  m and  $y=0.1$  m and  $0.7$  m in air.

- a.  $3.12 \mu Wb$
- b.  $5.22 \mu Wb$
- c.  $1.78 \mu Wb$
- d.  $2.34 \mu Wb$
- e. None of the above



15. Find the magnetic flux density  $B$  at the center of a semi-circular loop ( $0 < \varphi < \pi$ ) of radius 8cm carrying a dc current of 4A

- a.  $3\pi (\mu T)$
- b.  $5\pi (\mu T)$
- c.  $7\pi (\mu T)$
- d.  $9\pi (\mu T)$
- e. None of the above

16. The open-circuit and short-circuit impedances measured at the input terminals of a lossless transmission line of length 1.5m, which is less than a quarter wavelength are  $-j54.6 \Omega$  and  $j103 \Omega$  respectively. Find  $\beta$  of the line.

- a. 0.416
- b. 0.241
- c. 0.852
- d. 0.628
- e. None of the above

17. In problem 16, how long should the short-circuited line be in order for it to appear as an open circuit at the input terminals?

- a.  $l = 4 + (2n-1) m, n=1,2,3,\dots$
- b.  $l = 1.3 + (5n-1) m, n=1,3,5,\dots$
- c.  $l = 2.5 + 5(n-1) m, n=1,2,3,\dots$
- d.  $l = 3 + 7(n-1) m, n=1,2,3,\dots$
- e. None of the above