

Do each of the following problems. Show all your work. No work shown. No credit.

\*\*\*\*GOOD LUCK\*\*\*\*

**Problem 1. (Answer on pages 1,2,3,4 of the booklet)**

Evaluate the following integrals:

(5 pts each)

- a.  $\int \frac{xe^x}{(x+1)^2} dx$       b.  $\int \frac{x^3}{\sqrt{1+x^2}} dx$       c.  $\int \frac{x^2 + x - 2}{(3x-1)(x^2+1)} dx$
- d.  $\int_1^{\infty} \frac{4}{(x^9+100)^{5/3}} dx$  (Test for convergence or divergence only). Explain

**Problem 2. (Answer on page 5 of the booklet)**

Find the following limits:

(5 pts each)

1)  $\lim_{x \rightarrow \infty} \left( \frac{x}{3^{\ln x}} \right)$       2)  $\lim_{x \rightarrow \infty} \left( \frac{x-2}{x} \right)^{3x}$

**Problem 3. (Answer on page 6 of the booklet)**

(5 pts) Find the length of the curve

$$x = 5 \cos t - \cos 5t \quad y = 5 \sin t - \sin 5t \quad 0 \leq t \leq 2\pi$$

**Problem 4 (Answer on pages 7, 8, 9, 10 of the booklet)**

- a. (5 pts) Find the distance from the point S(1,1,3) to the plane  $3x + 2y + 6z = 6$
- b. (5 pts) Find the distance from the point S(1,1,5) to the line  
L:  $x = 1 + t, \quad y = 3 - t, \quad z = 2t$
- c. (5 pts) Find an equation for the plane through the point (2,1,-1) and perpendicular to the line of intersection of the planes  
 $2x + y - z = 3, \quad x + 2y + z = 2$
- d. (5 pts) Find an equation for the plane through the point (2,4,5) perpendicular to the line  
L:  $x = 5 + t, \quad y = 1 + 3t, \quad z = 4t$

**Problem 5. (Answer on pages 11, 12 of the booklet).**

- a. (5 pts) Find the area of a parallelogram determined by the vectors  $\mathbf{u} = -3\mathbf{i} - 2\mathbf{j} + 2\mathbf{k}$  and  $\mathbf{v} = -2\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$
- b. (5 pts) Write  $\mathbf{u} = 2\mathbf{i} - \mathbf{j} + 3\mathbf{k}$  as a sum of a vector parallel to  $\mathbf{v} = 4\mathbf{i} - \mathbf{j} + 2\mathbf{k}$  and a vector orthogonal to  $\mathbf{v}$ .

**Problem 6. (Answer on pages 13, 14, 15 of the booklet)**

(25 pts) Determine the unit tangent vector  $\mathbf{T}$ , the principal unit normal vector  $\mathbf{N}$ , the binormal vector  $\mathbf{B}$ , the curvature  $\kappa$ , and the torsion  $\tau$  for the curve

$$\mathbf{r}(t) = (3 \sin t) \mathbf{i} + (3 \cos t) \mathbf{j} + 4t \mathbf{k}$$

**Problem 7. (Answer on page 16 of the booklet)**

(10 pts) Without finding  $\mathbf{T}$  and  $\mathbf{N}$ , write the acceleration of the curve

$$\mathbf{r}(t) = (a \cos t) \mathbf{i} + (a \sin t) \mathbf{j} + bt \mathbf{k} \quad \text{in the form } \mathbf{a} = a_T \mathbf{T} + a_N \mathbf{N}$$

