

Chapter 04 Solved Problems

**Problem 4.20**

$$W = \int F dx = F \Delta x = 1500 \text{ N} \times 100 \text{ m} = 150\,000 \text{ J} = \mathbf{150 \text{ kJ}}$$

$$W = \int F dz = \int mg dz = mg \Delta Z = 500 \text{ kg} \times 9.807 \text{ m/s}^2 \times 3 \text{ m} = 14\,710 \text{ J} = \mathbf{14.7 \text{ kJ}}$$

$$W_{\text{total}} = 150 \text{ kJ} + 14.7 \text{ kJ} = \mathbf{164.7 \text{ kJ}}$$

**Problem 4.22**

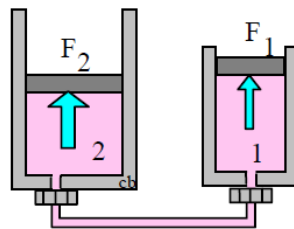
$$W = \int F dx = \int P dV = \int PA dx = PAx H = P\Delta V$$

$$\Delta V = W/P = 1 \text{ kJ} / 1200 \text{ kPa} = \mathbf{0.000\,833 \text{ m}^3}$$

Both cases the height is  $H = \Delta V/A$

$$H_1 = 0.000833 / 0.01 = \mathbf{0.0833 \text{ m}}$$

$$H_2 = 0.000833 / 0.03 = \mathbf{0.0278 \text{ m}}$$



**Problem 4.27**

Control volume radiator.

After the valve is closed no more flow, constant volume and mass.

$$1: x_1 = 1, P_1 = 110 \text{ kPa} \Rightarrow v_1 = v_g = 1.566 \text{ m}^3/\text{kg} \text{ from Table B.1.2}$$

$$2: T_2 = 25^\circ\text{C}$$

$$\text{Process: } v_2 = v_1 = 1.566 \text{ m}^3/\text{kg} = [0.001003 + x_2 \times 43.359] \text{ m}^3/\text{kg}$$

$$x_2 = 1.566 - 0.001003 / 43.359 = \mathbf{0.0361}$$

$$\text{State 2 : } T_2, x_2 \text{ From Table B.1.1 } P_2 = P_{\text{sat}} = \mathbf{3.169 \text{ kPa}}$$

**Work is 0 since constant volume process**

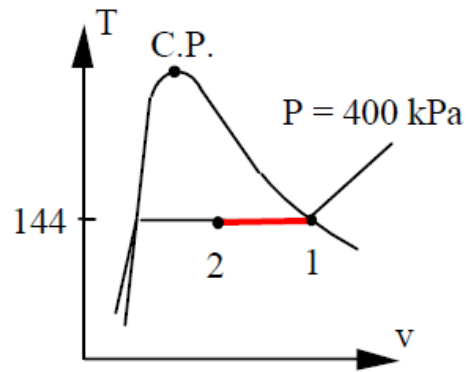
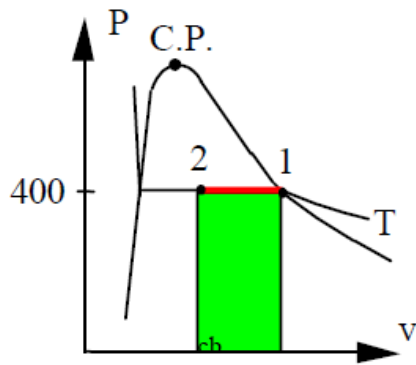
**Problem 4.28**

$$\text{Table B.1.2 } v_1 = 0.4625 \text{ m}^3/\text{kg} \quad V_1 = mv_1 = 0.0925 \text{ m}^3$$

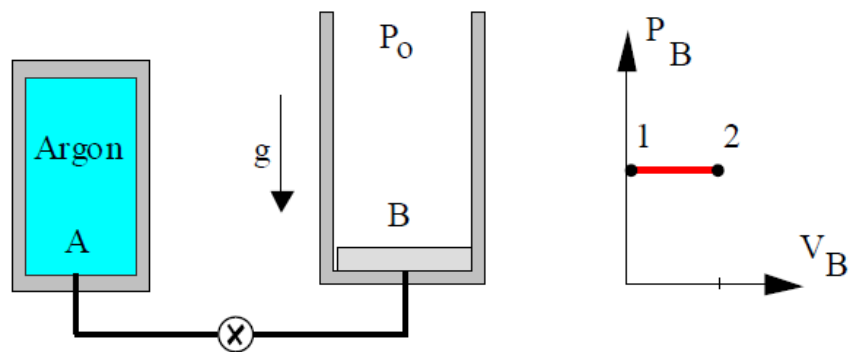
$$v_2 = v_1 / 2 = 0.23125 \text{ m}^3/\text{kg} \quad V_2 = V_1 / 2 = 0.04625 \text{ m}^3$$

Process:  $P = \text{Cst}$  so the work term integral is

$$W = \int PdV = P(V_2 - V_1) = 400 \text{ kPa} \times (0.04625 - 0.0925) \text{ m}^3 = \mathbf{-18.5 \text{ kJ}}$$



### Problem 4.30



Taking a control volume enclosing all the argon in both A and B.

The boundary movement work done in cylinder B against constant external pressure of 150 kPa. Argon is an ideal gas, so writing out that the mass and temperature at state 1 and 2 are the same:

$$P_1 V_A = m_A R T_{A1} = m_A R T_2 = P_2 (V_A + V_{B2})$$

$$\Rightarrow V_{B2} = 250 \times 0.4 / 150 - 0.4 = 0.2667 \text{ m}^3$$

$$W_{12} = \int P_{\text{ext}} dV = P_{\text{ext}} (V_{B2} - V_{B1}) = 150 \text{ kPa} (0.2667 - 0) \text{ m}^3 = \mathbf{40 \text{ kJ}}$$

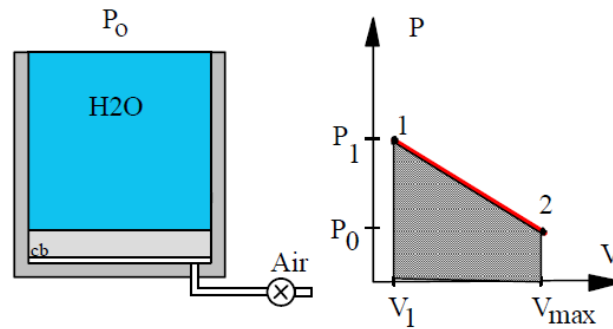
### Problem 4.33

$$P_1 = P_0 + \rho g H$$

$$= 101.32 + 997 \times 9.807 \times 5 / 1000 = 150.2 \text{ kPa}$$

$$\Delta V = H \times A = 5 \times 0.1 = 0.5 \text{ m}^3$$

$$W_{12} = \text{AREA} = \int P dV = \frac{1}{2} (P_1 + P_0) (V_{\text{max}} - V_1) = \frac{1}{2} (150.2 + 101.32) \text{ kPa} \times 0.5 \text{ m}^3 = \mathbf{62.88 \text{ kJ}}$$



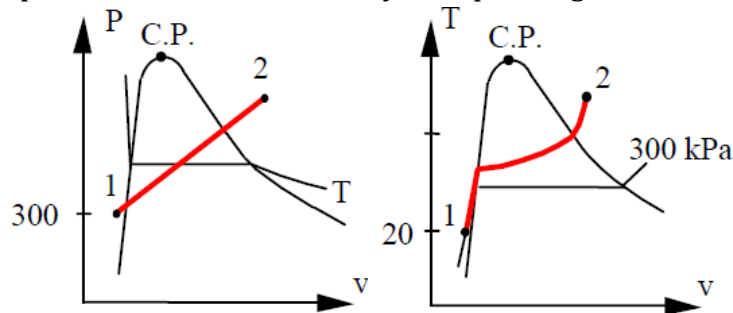
### Problem 4.35

a. State 1: Compressed liquid, saturated liquid at same temperature.

B.1.1:  $v_1 = v_f(20^\circ\text{C}) = 0.001002 \text{ m}^3/\text{kg}$ ,

State 2:  $v_2 = V_2/m = 0.1/1 = 0.1 \text{ m}^3/\text{kg}$  and  $P = 3000 \text{ kPa}$  from B.1.3

=> Superheated vapor close to  $T = 400^\circ\text{C}$  so by interpolating:  $T_2 = 404^\circ\text{C}$



c. Work is done while piston moves at linearly varying pressure, so we get:

$$W_{12} = \int P \, dV = P_{\text{ave}}(V_2 - V_1) = 1/2(P_1 + P_2)(V_2 - V_1) = 0.5 (300 + 3000)(0.1 - 0.001) = 163.35 \text{ kJ}$$

### Problem 4.47

Process:  $Pv^n = \text{Const} = P_1v_1^n = P_2v_2^n$

Ideal gas so :  $Pv = RT$

$$v_1 = RT/P = 0.287 \times 325/125 = 0.7462 \text{ m}^3/\text{kg}$$

$$v_2 = RT/P = 0.287 \times 500/300 = 0.47833 \text{ m}^3/\text{kg}$$

From the process equation

$$(P_2/P_1) = (v_1/v_2)^n \Rightarrow \ln(P_2/P_1) = n \ln(v_1/v_2)$$

$$n = \ln(P_2/P_1) / \ln(v_1/v_2) = \ln 2.4 / \ln 1.56 = 1.969$$

The work per unit mass (specific work) is:

$$w_{12} = \frac{P_2v_2 - P_1v_1}{1 - n} = \frac{R(T_2 - T_1)}{1 - n} = \frac{0.287(500 - 325)}{-0.969} = -51.8 \text{ kJ}$$

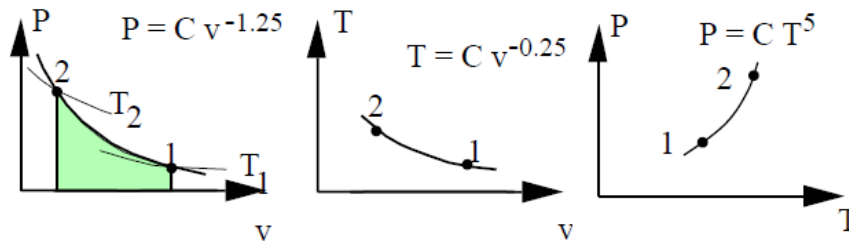
### Problem 4.50

Process:  $Pv^n = \text{Const} = P_1v_1^n = P_2v_2^n$

$$T_2 = T_1 \left( \frac{P_1}{P_2} \right)^{\frac{n-1}{n}} = 300.15 \left( \frac{100}{250} \right)^{\frac{0.25}{1.25}} = 360.5 \text{ K}$$

To evaluate the work:

$$W_{12} = \frac{P_2 V_2 - P_1 V_1}{1 - n} = m \cdot \frac{P_2 v_2 - P_1 v_1}{1 - n} = m \cdot \frac{R(T_2 - T_1)}{1 - n} = 0.1 \frac{0.2968(360.5 - 300.15)}{-0.25} = -7.165 \text{ kJ}$$



### Problem 4.59

a) From Table B.4.2:  $v_1 = 0.17732 \text{ m}^3/\text{kg}$ ,  
 $m = V/v = 0.010/0.17732 = 0.056395 \text{ kg}$

For the final state, if the piston were at the final stop, then  $V_{1a}$  would have been of 11 L  
 Then  $v_{1a} = V/m = 0.011/0.056395 = 0.19505 \text{ m}^3/\text{kg}$   
 $\Rightarrow T_{1a} = -9.4^\circ\text{C}$  but  $T_2 = 15^\circ\text{C}$  so  $T_2 > T_{1a}$   
 $\Rightarrow P_2 > P_1$

If the piston didn't reach the stops yet, the pressure would have remained constant at 150 kPa and by using 150 kPa and  $15^\circ\text{C}$ , we would have obtained the right specific volume

### Problem 4.86

Process:  $P = \text{constant}$

Boundary work:  $\delta W = P dV \Rightarrow W = P \Delta V$

Assuming ideal gas behavior for air

$$V_2 = V_1 \times (T_2/T_1) = 0.1 \times (600/300) = 0.2 \text{ m}^3$$

$$\dot{W} = P \Delta V / \Delta t = 300 \times (0.2 - 0.1) / 30 \text{ kPa m}^3/\text{s} = \mathbf{1 \text{ kW}}$$

### Problem 4.90

Steady conduction through the bottom of the steel pot.

Assume the inside surface is at the liquid water temperature.

$$\dot{Q} = k A \Delta T / \Delta x \Rightarrow \Delta T = \dot{Q} \Delta x / k A$$

$$\Delta T = 250 \text{ W} \times 0.005 \text{ m} / (50 \text{ W/m-K} \times \pi/4 \times 0.22 \text{ m}^2) = 0.796 \text{ K}$$

$$T = 15 + 0.796 \cong \mathbf{15.8^\circ\text{C}}$$

### Problem 4.103

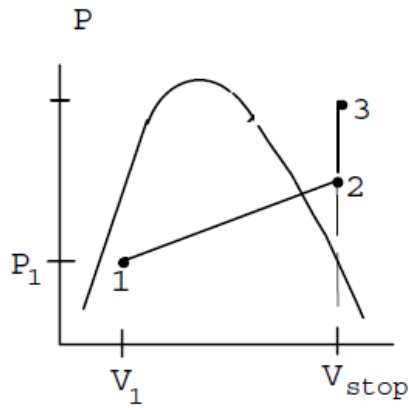
State 1:  $v_1 = V/m = 0.2 / 2 = 0.1 \text{ m}^3/\text{kg}$

Process:  $1 \rightarrow 2 \rightarrow 3$  or  $1 \rightarrow 3'$

State at stops: 2 or 2'

$$v_2 = V_{\text{stop}}/m = 0.4 \text{ m}^3/\text{kg} \text{ \& } T_2 = 600^\circ\text{C}$$

Table B.1.3  $\Rightarrow P_{\text{stop}} = 1 \text{ MPa} < P_3$  since  $P_{\text{stop}} < P$  then the process is as  $1 \rightarrow 2 \rightarrow 3$



State 3:  $P_3 = 1.2 \text{ MPa}$ ,  $v_3 = v_2 = 0.4 \text{ m}^3/\text{kg} \Rightarrow T_3 \cong 770^\circ\text{C}$

$$W_{13} = W_{12} + W_{23} =$$

$W_{12} = 0.5(P_1 + P_2)(V_2 - V_1) = 0.5(100 + 1000) \text{ kPa} \times (0.8 - 0.2) \text{ m}^3$  (this is only possible because the spring is linear and the force it applies, induces a pressure that varies linearly with the displacement and hence the swept volume)

$W_{23} = 0$  (constant volume)

Hence  $W_{13} = 330 \text{ kJ}$

#### Problem 4.109

The process equation and  $T$  determines state 2. Use ideal gas law to say

$$P_2 = P_1 \left( \frac{T_1}{T_2} \right)^{\frac{n}{n-1}} = 100 \left( \frac{340}{300} \right)^{\frac{1.1}{0.1}} = 396 \text{ kPa}$$

$$V_2 = V_1 \left( \frac{P_1}{P_2} \right)^{\frac{1}{n}} = 0.2 \left( \frac{100}{396} \right)^{1/1.1} = 0.0572 \text{ m}^3$$

For propane Table A.2:  $T_c = 370 \text{ K}$ ,  $P_c = 4260 \text{ kPa}$ , Figure D.1 gives  $Z$ .

$$Tr_1 = 0.81, Pr_1 = 0.023 \Rightarrow Z_1 = 0.98$$

$$Tr_2 = 0.92, Pr_2 = 0.093 \Rightarrow Z_2 = 0.95$$

Ideal gas model OK for both states, work is integrated to give:

$${}_1W_2 = \int P dV = \frac{P_2 V_2 - P_1 V_1}{1-n} = \frac{(396 \times 0.0572) - (100 \times 0.2)}{1 - 1.1} \text{ kPa m}^3$$

$$W_{12} = -26.7 \text{ kJ}$$