

**American University of Beirut**  
DEPARTMENT OF ELECTRICAL AND COMPUTER ENGINEERING  
EECE 311 – Electronic Circuits (Section 2)  
Spring 2008  
**HOMEWORK 2**

**1. Common Source Amplifier**

a)  $P = 1\text{mW}$  and  $V_{DD} = 1.8\text{V}$

$$\Rightarrow I_{DD} = \frac{P}{V_{DD}} = 0.556\text{ mA}$$

$$r_{O1} = \frac{V_{An}}{I} = 9\text{ K}\Omega, \quad r_{O2} = \frac{|V_{Ap}|}{I} = 7.2\text{ K}\Omega$$

$$|A_{V1}| = g_{m1}(r_{O1} // r_{O2}) \Rightarrow g_{m1} = 2.5\text{ mA/V}$$

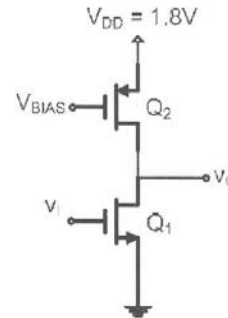
$$\text{but } g_{m1} = \frac{2I}{V_{OV1}} \Rightarrow V_{OV1} = 0.444\text{ V}$$

$$I = \frac{1}{2}k'_n \left(\frac{W}{L}\right)_1 (V_{OV1})^2 \text{ in } Q_1$$

$$\Rightarrow \left(\frac{W}{L}\right)_1 = 18.75$$

b)  $I = \frac{1}{2}k'_p \left(\frac{W}{L}\right)_2 (V_{OV2})^2 \text{ in } Q_2 \Rightarrow V_{OV2} = 0.316\text{ V}$

$$\text{but } V_{OV2} = V_{DD} - V_{bias} - |V_{tp}| \Rightarrow V_{bias} = 0.984\text{ V}$$

**2. Common Gate Amplifier**

$P = 2\text{mW}$  and  $V_{DD} = 1.8\text{V}$

$$\Rightarrow I_{DD} = I_1 = \frac{P}{V_{DD}} = 1.111\text{ mA}$$

Using the small signal model we have:

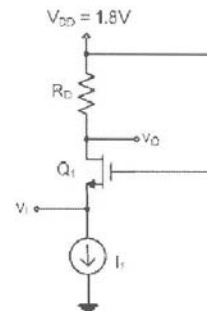
$$R_i = \frac{v_i}{i_i} = \frac{v_i}{g_m v_i} \Rightarrow g_m = \frac{1}{R_i} = 0.02\text{ A/V}$$

$$A_v = \frac{v_o}{v_i} = \frac{g_m v_i R_D}{v_i} \Rightarrow R_D = 250\text{ }\Omega$$

$$\text{but } g_m = \frac{2I_1}{V_{OV}} \Rightarrow V_{OV} = 0.111\text{ V}$$

$$I_1 = \frac{1}{2}k'_n \left(\frac{W}{L}\right) (V_{OV})^2$$

$$\Rightarrow \left(\frac{W}{L}\right) = 600.1$$



### 3. Emitter Follower

$P = 3\text{mW}$  and  $V_{CC} = 2.5\text{V}$

$$\Rightarrow I_{CC} = \frac{P}{V_{CC}} = 1.2\text{mA}$$

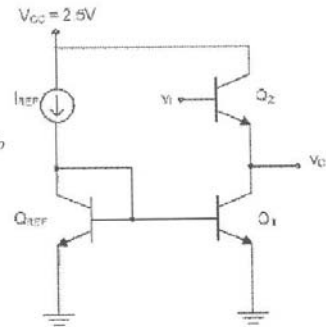
since we neglect base - width modulation no  $r_o$

$$\Rightarrow \text{in } Q_2: R_o = r_e = \frac{V_T}{I_E} \Rightarrow I_E = I_C = 0.5\text{mA}$$

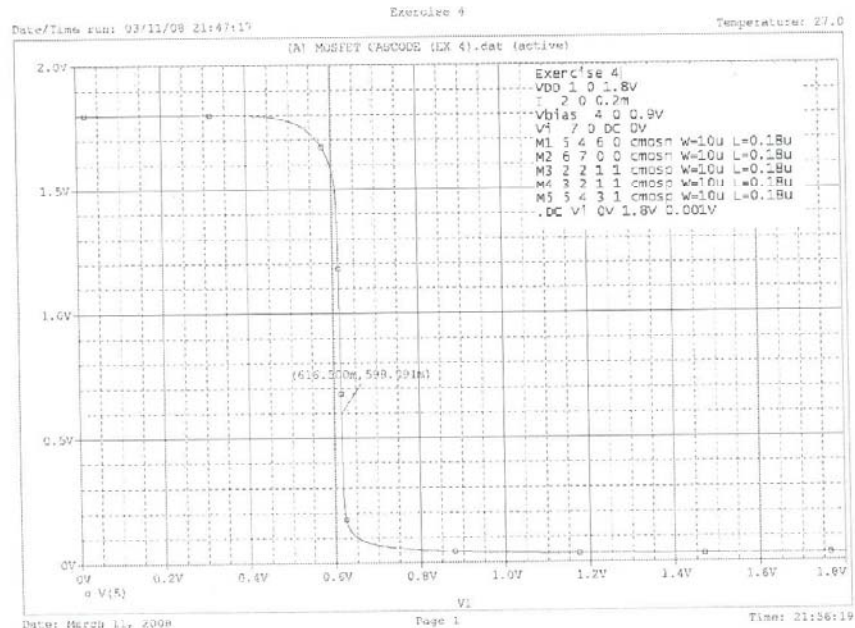
since  $B \rightarrow \infty$

$$\Rightarrow I_{REF} = I_{CC} - I_E = 0.7\text{mA}$$

$$\frac{A_{E1}}{A_{REF}} = \frac{I_E}{I_{REF}} = 0.714$$



### 4. MOSFET Cascode



The maximum gain is 129.154 according to the derivative at that point in the plot by using pspice to calculate the maximum slope of the plot.

more accurately it's 129

When the bias changes by  $\pm 20\text{mV}$ , the gain drops to less than 10.

### 5. Miller's Theorem

The two BJT's in this circuit are cascaded, so the total gain is the product of the gain of each BJT independently.

$$\Rightarrow K = -g_{m1}R_C \times 1$$

by Miller's theorem we can separate  $C_F$  in to 2 different capacitors, one on the side of the input and one on the input.

At the input:  $C_{in} = C_F(1 - K)$   
 At the output:  $C_{out} = C_F(1 - \frac{1}{K})$

The resistance seen by  $C_{in}$  is:

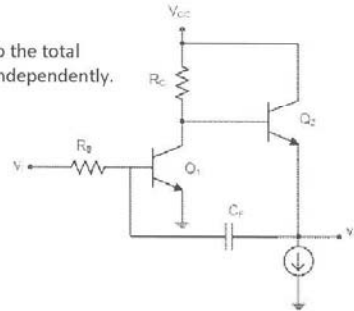
$$R_{Cin} = (R_B // r_{\pi 1})$$

The resistance seen by  $C_{out}$ : Replace  $C_{out}$  by a current source  $I_x$  having voltage  $V_x$

$$R_{Cout} = \frac{V_x}{I_x} = \frac{r_{\pi 2} + R_C}{1 + g_m r_{\pi 2}}$$

$$\Rightarrow \text{the pole at the input is: } \frac{1}{R_{Cin} C_{in}} = \frac{1}{(R_B // r_{\pi 1}) C_F (1 + g_{m1} R_C)}$$

$$\Rightarrow \text{the pole at the output is: } \frac{1}{R_{Cout} C_{out}} = \frac{1}{(r_{\pi 2} + R_C) C_F (1 + \frac{1}{g_{m1} R_C})}$$



### 6. Active Inductor

To find  $Z_{in}$  we add a voltage source  $V_x$  with a current  $I_x$ , and then:  $Z_{in} = \frac{V_x}{I_x}$ , in small signal analysis the MOSFET becomes a dependent current source  $= g_m V_{gs}$  with  $V_{gs}$  being the voltage across the capacitor  $C$ .

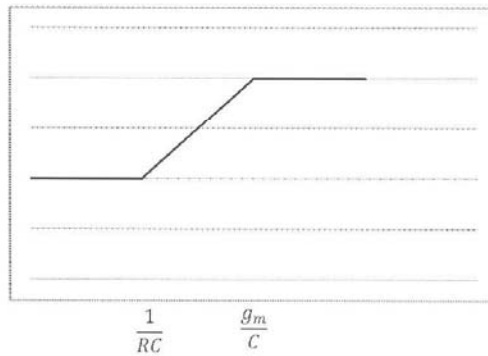
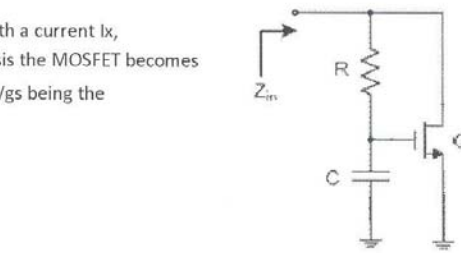
$$V_{gs} = \frac{V_x}{sC(R + \frac{1}{sC})} = \frac{V_x}{1 + sRC}$$

$$I_x = \frac{V_x}{(R + \frac{1}{sC})} + g_m V_{gs} = \frac{g_m + sC}{1 + sRC} V_x$$

$$\Rightarrow \frac{V_x}{I_x} = \frac{1}{g_m} \times \frac{1 + sRC}{1 + \frac{sC}{g_m}}$$

Between  $\omega = \frac{1}{RC}$  and  $\omega = \frac{g_m}{C}$  } - The Bode Plot of  $Z_{in}$  represents the Bode plot of an inductor.   
*approximates*

$$\frac{1}{g_m}$$



### 7. Cascode Frequency Response

$$I_D = \frac{1}{2} k_n' \left( \frac{W}{L} \right) (V_{OV})^2$$

$$\Rightarrow \left( \frac{W}{L} \right) = 250 \Rightarrow W = 45 \mu\text{m}$$

$$\Rightarrow C_{gs} = 64.8 \text{ fF} \Rightarrow C_{gd} = 9 \text{ fF}$$

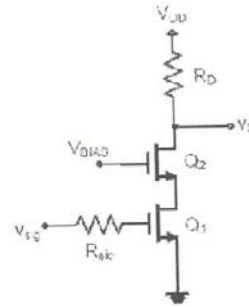
$$g_m = \frac{2I_D}{V_{OV}} = 5 \frac{\text{mA}}{\text{V}}$$

The gain of Q1 is -1

So by Miller's we can approximate Cgd1 in to 2 capacitors

On the side of the input:  $C_{gdin} = 9 \text{ fF} \times 2 = 18 \text{ fF}$

$$\omega_{in} = \frac{1}{R_{sig}(C_{gdin} + C_{gs})}, \Rightarrow R_{sig} = 384.43 \Omega$$



At the output :

$$f_{P_{out}} = \frac{1}{2\pi C_{gd} R_D} \Rightarrow R_D = 1.768 \text{ k}\Omega$$

$$\text{Voltage Gain} = -g_{m2} R_D \quad \text{since gain of } Q_1 \text{ is } -1$$

$$= -5 \text{ m} \times 1.768 = -8.84 \text{ V/V}$$