

Lecturer: Prof. Fadi N Karameh

Quiz 1, March 22, 2006

Directions:

- You will have 1.5 hrs for this quiz.
- Write down your initials *in ink* on all the pages. **DO IT NOW!**
- Enter **ALL** your work and your answers on the answer booklet. You can use the back of these pages for scratch. I will **ONLY** grade the work you neatly transfer to the assigned spaces on the booklet.
- Answers must be explained or derived. **DO NOT** just write down an answer, unless otherwise indicated.
- It is a good idea to read the whole test before you begin. Problems are divided into several parts with percentages indicated. *You might be able to solve different parts independently.*
- **DO NOT** talk to any of your colleagues under any circumstances. You will be penalized without warning.

YOUR NAME HERE:

Please space below empty for graders to use.

Problem 1

Problem 2

Problem 3

Problem 4

Problem 5

Problem 6

Total _____

PROBLEM 1 (12%)

a) Consider the CT system given by

$$y(t) = \frac{x(t)}{\sin(4t)}$$

Determine if the system is

- i- Linear
- ii- Time invariant.

For both cases, either prove the statement or give a counterexample.

b) Consider the DT system given by

$$y[n] = \text{Odd}\{x[n+1]\} = \frac{x[n+1] + x[1-n]}{2}$$

Determine whether the system is time invariant or not. That is, either prove the statement or give a counterexample.

c) **Optional (extra 5%)**: Find the steady state response of the causal CT LTI system

$$H(s) = \frac{1}{s^4 + ks^3 + s^2 + s + 1}$$

to an input $x(t) = \cos(5t + 45^\circ)$.

PROBLEM 2 (10%)

Consider the CT LTI system shown in figure 1. If the input $x_1(t)$ is given by $x_1(t) = u(t)$ (unit step function), the corresponding output is given by $y_1(t) = u(t) - 2u(t-1) + u(t-2)$.

Determine and *sketch* the output of the cascaded system $y_2(t)$ if the input $x_2(t)$ is as given in the figure.

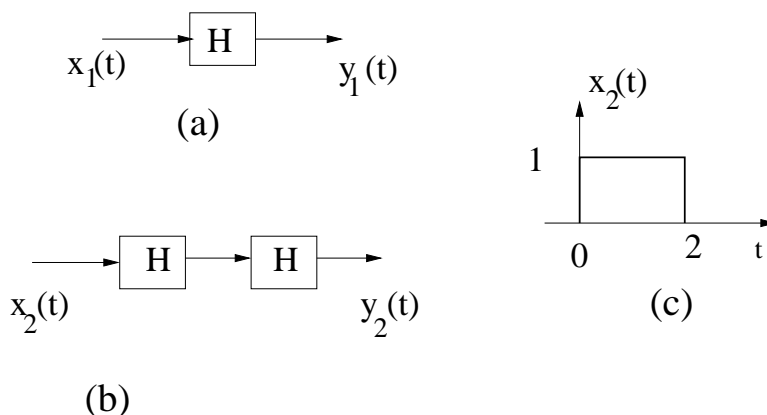


Figure 1: Problem 2

PROBLEM 3 (15%)

Consider the system shown in figure 2. This is a long ladder circuit where $x(t)$ is the input voltage and $y(t)$ is the current in the last 1Ω resistor of the circuit (note there are 100 resistors of value 2Ω).

Find the current $y(t)$ in terms of the input voltage $x(t)$.

Hint: Ladders have steps.

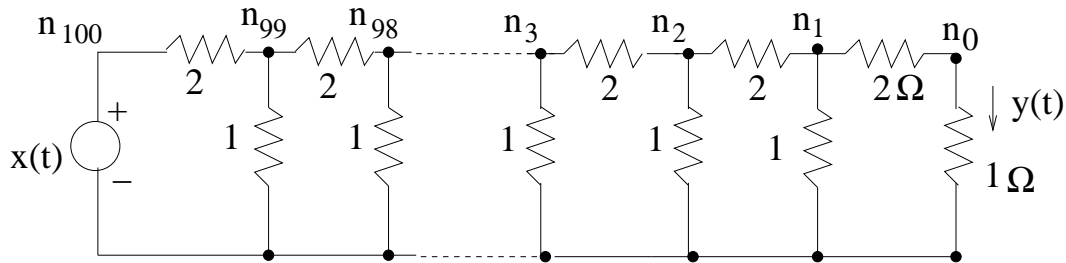


Figure 2: Problem 3

PROBLEM 4 (15%)

Consider the CT LTI system described by:

$$\frac{d^2y}{dt^2} + 4\frac{dy}{dt} = \frac{dx}{dt} + x$$

- a) Draw a block diagram description of the above system, using integrators, adders and gains.
- b) Write the state space description of this system in matrix form.
- c) Find the zero state response (ZSR) if the input is $x(t) = e^{-2t}u(t)$.

PROBLEM 5 (30%)

Consider the causal CT LTI system shown in figure 3.

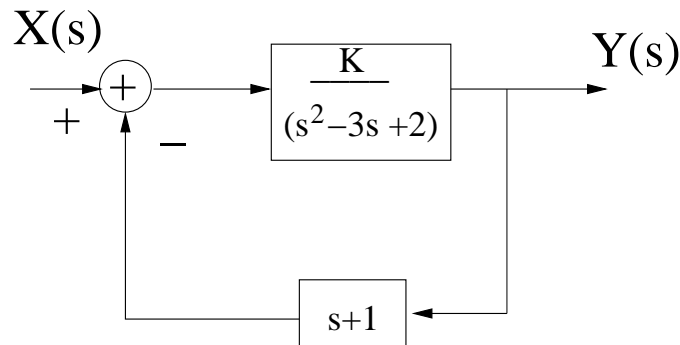


Figure 3: Problem 5

- a) Find the closed loop transfer function from the input to the output $H(s) = \frac{Y(s)}{X(s)}$.
- b) For what values of K is this system BIBO stable? explain.

- c) If the input to the system is $x(t) = \cos(2t)$, $-\infty < t < \infty$, you are told that the corresponding output is $y(t) = A \sin(\alpha t)$. (i) Find the value of K that makes this possible. (ii) Find also α and A .
- d) If sensor noise affects the system as shown in figure 4, find the *maximum* steady state attenuation of the noise effect at the output $y(t)$ that can be achieved for a unit step noise $n(t) = u(t)$.
- e) Can you suggest a controller $F(s)$ to be placed in cascade with the $(s+1)$ term in the feedback loop such that the noise effect $n(t) = u(t)$ is *completely blocked* at the output $y(t)$ at steady state?

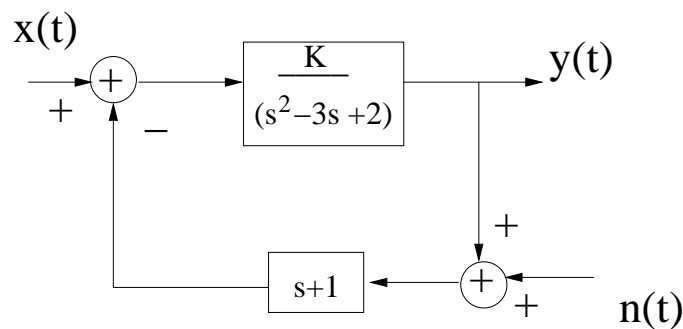


Figure 4: Problem 5 (e)

PROBLEM 6 (18%)

A pole zero plot is a schematic for the location of the poles and zeros in the s -plane. A pole is represented with an "x" while a zero is represented by a "o".

For each pole-zero plot shown in Figure 5 below, find the frequency response, among those given in the same figure, that could result from the pole-zero plot.

- Explain the reasoning of your choices.
- *NO GRADE* will be given without a clear justification that I am convinced of.
- Note that the bode plots DO NOT change their asymptotic behavior outside the given range of frequencies.

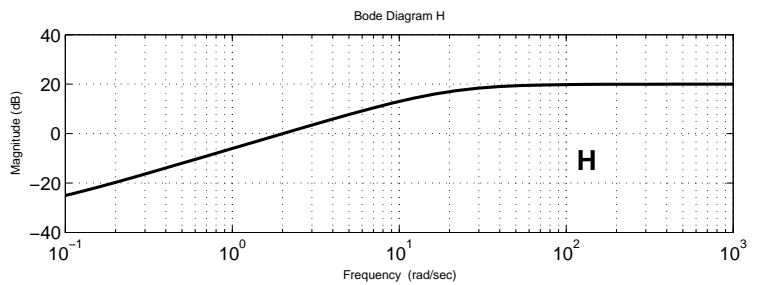
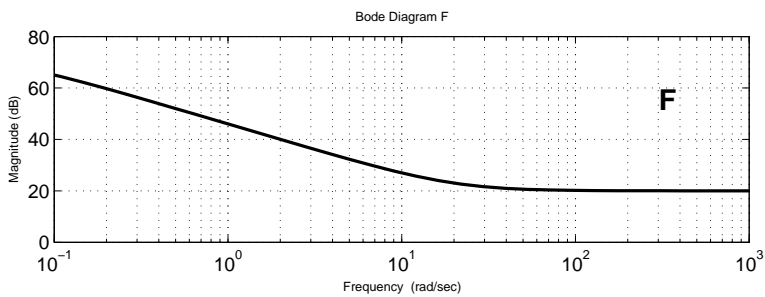
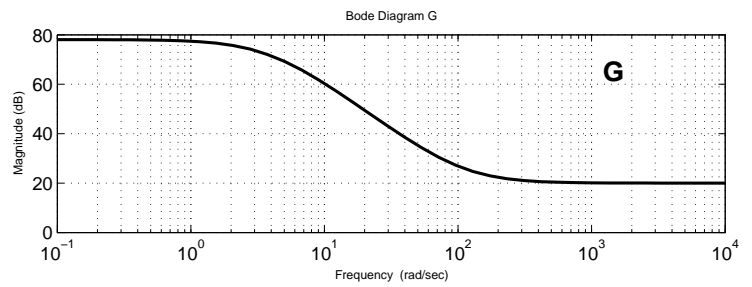
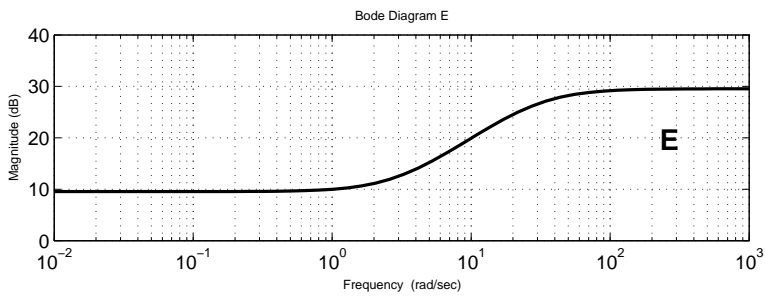
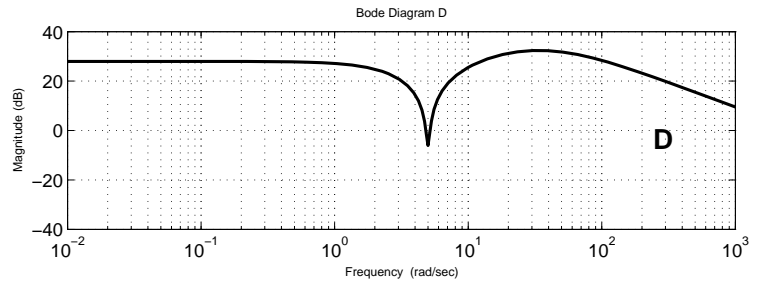
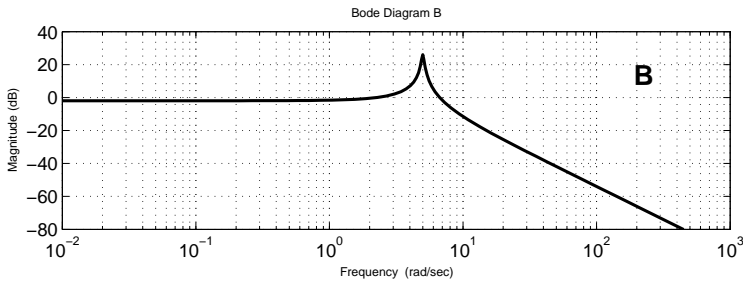
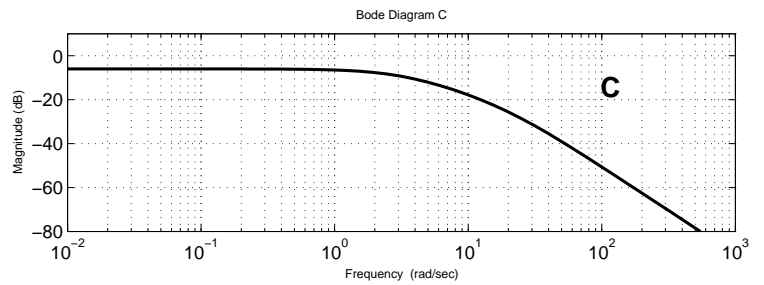
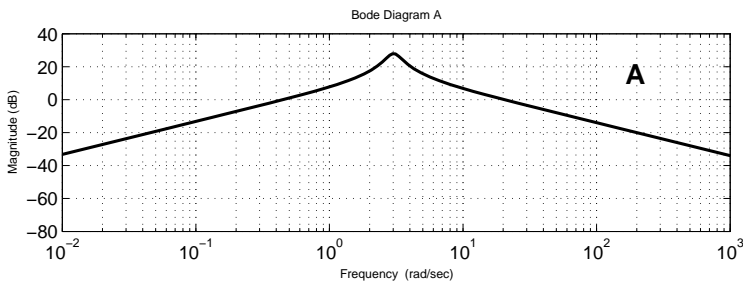
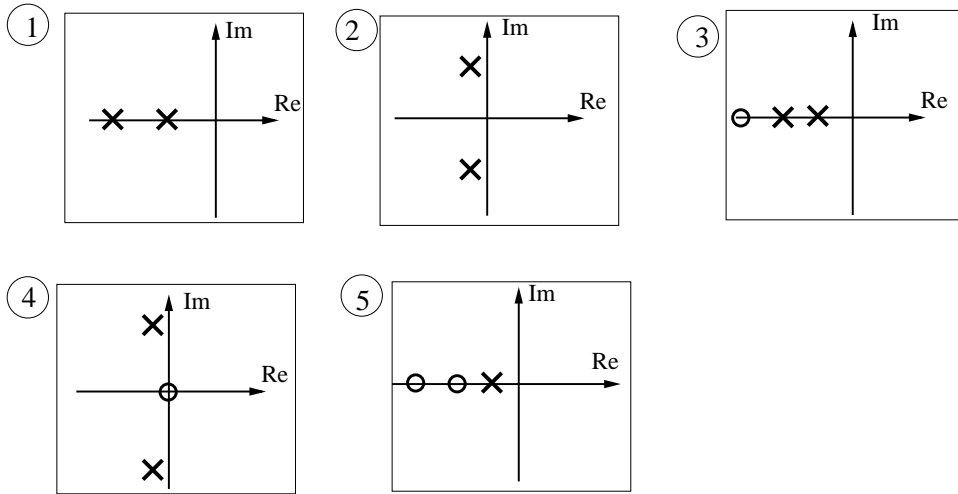


Figure 5: Problem 6