

American University of Beirut

Faculty of Engineering and Architecture

Department of Electrical and Computer Engineering

EECE 200-Introduction to Engineering – Fall 2014

Homework 2

Homework2 consists of two parts:

- Part 1 is questions related to topics covered during the lectures.
- Part 2 is based on LabVIEW, and the concepts covered will help you with the project later on.

Part 1:

Problem 1 (Circuits and Electronics): [15 points]

Apple recently (September 2014) released the iPhone 6 smart phone. It has an A8 processor which has several powerful properties.

- a. Find out some properties of the A8 processor in terms of number of transistors and technology used, size, clock speed. [3points]

2 billion transistors using a 20-nanometer manufacturing process , size of 89 mm² , clock speed of 1.4 gigahertz [1 point each]

- b. If the A8 processor now has 2 billion transistors. Suppose after few years, Apple will announce its new smart phone whose processor has 13 billion transistors. What year would that be? [6points]

The number of transistors in a chip in year Y_2 is given by:

$N_2 = 2^{(Y_2 - Y_1)/2} * N_1$ where N_1 is the number of transistors in a chip in year Y_1 ($Y_1 < Y_2$).

So $\ln(N_2) = (Y_2 - Y_1)/2 * \ln(2) + \ln(N_1)$

$Y_2 = 2\ln(N_2/N_1) / \ln(2) + Y_1$

$$Y_2 = 2[\ln(13/2)] / \ln(2) + 2014$$

$$Y_2 = 2019.4$$

- c. Suppose Moore's Law said that the number of transistors would triple every two years, how many transistors would be on this chip in the year 2025? [6points]

$$N_2 = 3^{(Y_2 - Y_1)/2} * N_1$$

$$Y_2 - Y_1 = 2025 - 2014 = 11, \text{ then } N_2 = 3^{5.5} * 2 \text{ billion}$$

In 2025 we will have about 841.7 billion transistors on a single chip.

Problem 2 (Computer Hardware): [16 points]

Consider the following expression:

$$O = [(A.B)' + C] \oplus [(A+C) + (B \oplus C)']$$

- a. Find the truth table of the following expression (output O in terms of three inputs A, B, and C). [10 points]

A	B	C	A.B	(A.B)'	(A.B)' + C	(A+C)	(B ⊕ C)	(B ⊕ C)'	(A+C) + (B ⊕ C)'	[(A.B)' + C] ⊕ [(A+C) + (B ⊕ C)']
0	0	0	0	1	1	0	0	1	1	0
0	0	1	0	1	1	1	1	0	1	0
0	1	0	0	1	1	0	1	0	0	1
0	1	1	0	1	1	1	0	1	1	0
1	0	0	0	1	1	1	0	1	1	0
1	0	1	0	1	1	1	1	0	1	0
1	1	0	1	0	0	1	1	0	1	1
1	1	1	1	0	1	1	0	1	1	0

- b. Write the following expression in terms of AND, OR, NAND, NOR, NOT and XOR gates. [6points]

$$O = [(A \text{ NAND } B) \text{ OR } C] \text{ XOR } [(A \text{ OR } C) \text{ OR } \text{NOT}(B \text{ XOR } C)]$$

Problem 3 (Communications and Signals): [19 points]

The following audio signal $X(t) = 1.5 \cos(1250t)$ Volts is to be transmitted via a communication link using digital communication system.

(In the following exercises, make sure to indicate units whenever necessary).

- a. What are the two main steps in Analog to Digital conversion? [2 points]

Sampling, Quantization

- b. What is the minimum sampling rate required to sample this signal? Why? [2 point]

According to Nyquist rule:

$$\text{minimum sampling rate} = 2 * F_{\text{max}} = 2 * (1250/2 * \pi) = 397.8 \text{ Sample/sec}$$

- c. If the signal is sampled at a rate of 500 samples/sec. Find the values of the first five samples, starting with $t=0$. Show all your calculations. [5 points]

$$t_1=0; X(t_1) = 1.5\cos(0) = 1.5V$$

$$t_2=1/\text{sampling rate}=1/500 \text{ s}; X(t_2) = 1.5\cos(1250*(1/500)) = -1.2V$$

$$t_3=2/500 \text{ s}; X(t_3) = 1.5\cos(1250*(2/500)) = 0.425V$$

$$t_4=3/500 \text{ s}; X(t_4) = 1.5\cos(1250*(3/500)) = 0.519V$$

$$t_5=4/500 \text{ s}; X(t_5) = 1.5\cos(1250*(4/500)) = -1.26V$$

(Angle is in radians)

The samples are quantized to 256 discrete levels that correspond to full range of +/- 1.5Volts (All zeros is -1.5V and all ones is +1.5V).

- d. If 256 quantization levels are used, what is the required bits/sample of the A/D converter? [1 point]

8 bits/ sample

- e. Find the binary representation of the first five samples starting at $t=0$. Show all your calculations. [5 points]

Total range is 3 V => $\Delta = 3/256 \text{ levels} = 0.0117$.

At $t_1=0, v=1.5 \Rightarrow 1.5+1.5=3, 3/0.0117=256 \Rightarrow 256^{\text{th}}$ interval, level number: 255 (because 256 intervals start from level 0 to level 255), binary representation of 255 is 1111 1111

At $t_2, v=-1.2 \Rightarrow -1.2+1.5=0.3; 0.3/0.0117=25.6 \Rightarrow 26^{\text{th}}$ interval. level number=25, its binary representation is 0001 1001

T	Value of the sample(V)	interval	Level number	Binary representation of the level
t1=0	1.5	256 th	255	1111 1111
t2=1/500	-1.2	26 th	25	0001 1001
t3=2/500	0.425	165 th	164	1010 0100
t4=3/500	0.519	173 nd	172	1010 1100
t5=4/500	-1.26	21 st	20	0001 0100

f. How can we improve sampling of a signal? Does it have any drawbacks? [2 points]

Increase the sampling rate which will give us a better quality of the digital signal. [1 point] Drawback: a larger size of the file or needs more memory (due to a larger number of samples with the same number of bits) [1 point]

g. How can quantization be improved? What is the disadvantage of this improvement? [2 points]

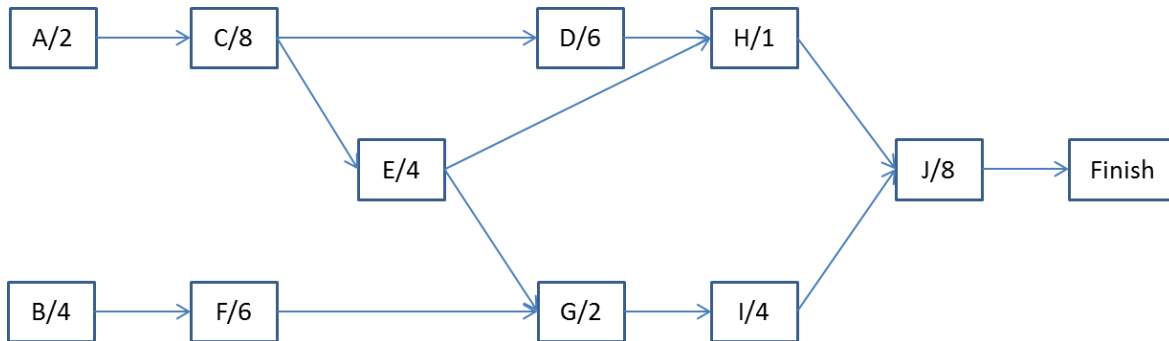
Increase the number of quantized levels or the number of bits. [1 point] Disadvantage: will also make the file larger or needs more memory (due to an increase in the number of bits used to store the data digitally, while the number of samples remains the same). [1 point]

Problem 4 (Project Management): [35 points]

Consider the following list of activities for an engineering project along with the expected duration in days. The activities are shown in the table below:

Activity	Predecessor	Duration in days
A	None	2
B	None	4
C	A	8
D	C	6
E	C	4
F	B	6
G	E,F	2
H	D,E	1
I	G	4
J	H,I	8

a. Show the network diagram representation of this project. [4 points]



b. Identify the paths from start to end of the project and the duration of each path. [4 points]

PATH	Duration in days
A C D H J	$2+8+6+1+8 = 25$
A C E H J	$2+8+4+1+8=23$
A C E G I J	$2+8+4+2+4+8 = 28$
B F G I J	$4+6+2+4+8 = 24$

c. Indicate the critical path based on observations from part (b). Justify. [1.5points]

A C E G I J, since it has the longest duration of 28 days.

d. Find the earliest start and the earliest finish of each task. [10 points: 0.5 point for each]

e. Find the latest start and latest finish of each task. [10 points: 0.5 point for each]

f. Find the float time (slack time= $LS-ES=LF-EF$). [2.5 points: 0.25 Point for each]

TASK	Earliest Start (ES)	Earliest Finish (EF)	LS	LF	Float time =LS-ES
A	0	2	0	2	0
B	0	4	4	8	4
C	2	10	2	10	0
D	10	16	13	19	3
E	10	14	10	14	0
F	4	10	8	14	4
G	14	16	14	16	0
H	16	17	19	20	3
I	16	20	16	20	0
J	20	28	20	28	0

- g. Indicate the critical path based on observations from part (f). Justify.
[2 points]

The tasks that have 0 float time belong to the critical path, so the critical path is: A C E G I J

- h. Find the minimum project completion time. [1 point]

The minimum project completion time is the duration of the critical path:
28 days