

4.18 This problem asks that we determine, for a hypothetical alloy that is composed of 25 wt% of metal A and 75 wt% of metal B, whether the crystal structure is simple cubic, face-centered cubic, or body-centered cubic. We are given the densities of these metals ( $\rho_A = 6.17 \text{ g/cm}^3$  and  $\rho_B = 8.00 \text{ g/cm}^3$  for B), their atomic weights ( $A_A = 171.3 \text{ g/mol}$  and  $A_B = 162.0 \text{ g/mol}$ ), and that the unit cell edge length is 0.332 nm (i.e.,  $3.32 \times 10^{-8} \text{ cm}$ ). In order to solve this problem it is necessary to employ Equation 3.5; in this expression density and atomic weight will be averages for the alloy—that is

$$\rho_{\text{ave}} = \frac{nA_{\text{ave}}}{V_C N_A}$$

Inasmuch as for each of the possible crystal structures, the unit cell is cubic, then  $V_C = a^3$ , or

$$\rho_{\text{ave}} = \frac{nA_{\text{ave}}}{a^3 N_A}$$

And, in order to determine the crystal structure it is necessary to solve for  $n$ , the number of atoms per unit cell. For  $n = 1$ , the crystal structure is simple cubic, whereas for  $n$  values of 2 and 4, the crystal structure will be either BCC or FCC, respectively. When we solve the above expression for  $n$  the result is as follows:

$$n = \frac{\rho_{\text{ave}} a^3 N_A}{A_{\text{ave}}}$$

Expressions for  $A_{\text{ave}}$  and  $\rho_{\text{ave}}$  are found in Equations 4.11a and 4.10a, respectively, which, when incorporated into the above expression yields

$$n = \frac{\left( \frac{100}{\frac{C_A}{\rho_A} + \frac{C_B}{\rho_B}} \right) a^3 N_A}{\left( \frac{100}{\frac{C_A}{A_A} + \frac{C_B}{A_B}} \right)}$$

Substitution of the concentration values (i.e.,  $C_A = 25 \text{ wt\%}$  and  $C_B = 75 \text{ wt\%}$ ) as well as values for the other parameters given in the problem statement, into the above equation gives