

4.3 This problem calls for the computation of the activation energy for vacancy formation in silver. Upon examination of Equation 4.1, all parameters besides Q_v are given except N , the total number of atomic sites. However, N is related to the density, (ρ), Avogadro's number (N_A), and the atomic weight (A) according to Equation 4.2 as

$$\begin{aligned} N &= \frac{N_A \rho_{\text{Pb}}}{A_{\text{Pb}}} \\ &= \frac{(6.023 \times 10^{23} \text{ atoms/mol})(9.5 \text{ g/cm}^3)}{107.9 \text{ g/mol}} \\ &= 5.30 \times 10^{22} \text{ atoms/cm}^3 = 5.30 \times 10^{28} \text{ atoms/m}^3 \end{aligned}$$

Now, taking natural logarithms of both sides of Equation 4.1,

$$\ln N_v = \ln N - \frac{Q_v}{kT}$$

and, after some algebraic manipulation

$$\begin{aligned} Q_v &= -kT \ln \left(\frac{N_v}{N} \right) \\ &= - (8.62 \times 10^{-5} \text{ eV/atom} \cdot \text{K})(800^\circ\text{C} + 273 \text{ K}) \ln \left[\frac{3.60 \times 10^{23} \text{ m}^{-3}}{5.30 \times 10^{28} \text{ m}^{-3}} \right] \\ &= 1.10 \text{ eV/atom} \end{aligned}$$