

3.15 In order to determine the APF for U, we need to compute both the unit cell volume (V_C) which is just the product of the three unit cell parameters, as well as the total sphere volume (V_S) which is just the product of the volume of a single sphere and the number of spheres in the unit cell (n). The value of n may be calculated from Equation 3.5 as

$$\begin{aligned}
 n &= \frac{\rho V_C N_A}{A_U} \\
 &= \frac{(19.05 \text{ g/cm}^3)(2.86)(5.87)(4.95)(\times 10^{-24} \text{ cm}^3)(6.023 \times 10^{23} \text{ atoms/mol})}{238.03 \text{ g/mol}} \\
 &= 4.01 \text{ atoms/unit cell}
 \end{aligned}$$

Therefore

$$\begin{aligned}
 \text{APF} &= \frac{V_S}{V_C} = \frac{(4)\left(\frac{4}{3}\pi R^3\right)}{(a)(b)(c)} \\
 &= \frac{(4)\left[\frac{4}{3}(\pi)(1.385 \times 10^{-8} \text{ cm})^3\right]}{(2.86)(5.87)(4.95)(\times 10^{-24} \text{ cm}^3)} \\
 &= 0.536
 \end{aligned}$$