

7.28 In order for these two cylindrical specimens to have the same deformed hardness, they must be deformed to the same percent cold work. For the first specimen

$$\begin{aligned} \%CW &= \frac{A_0 - A_d}{A_0} \times 100 = \frac{\pi r_0^2 - \pi r_d^2}{\pi r_0^2} \times 100 \\ &= \frac{\pi (15 \text{ mm})^2 - \pi (12 \text{ mm})^2}{\pi (15 \text{ mm})^2} \times 100 = 36\%CW \end{aligned}$$

For the second specimen, the deformed radius is computed using the above equation and solving for r_d as

$$\begin{aligned} r_d &= r_0 \sqrt{1 - \frac{\%CW}{100}} \\ &= (11 \text{ mm}) \sqrt{1 - \frac{36\%CW}{100}} = 8.80 \text{ mm} \end{aligned}$$