

$$\text{mol\% Al}_2\text{O}_3 = \left[ \frac{\frac{100 - 2y}{2}}{\frac{100 - 2y}{2} + (50 + 2y)} \right] \times 100$$

If we solve for  $y$  when the mol% of  $\text{Al}_2\text{O}_3 = 39$ , then  $y = 7.91$ . Thus, 7.91  $\text{O}^{2-}$  vacancies are produced in the original material that had 200  $\text{O}^{2-}$  ions. Therefore, the percentage of vacancies is just

$$\% \text{ vacancies} = \frac{7.91}{200} \times 100 = 3.96\%$$