

16.D6 (a) This portion of the problem calls for a determination of which of the four fiber types is suitable for a tubular shaft, given that the fibers are to be continuous and oriented with a volume fraction of 0.40. Using Equation 16.10 it is possible to solve for the elastic modulus of the shaft for each of the fiber types. For example, for glass (using moduli data in Table 16.6)

$$\begin{aligned}
 E_{cs} &= E_m(1 - V_f) + E_f V_f \\
 &= (2.4 \text{ GPa})(1.00 - 0.40) + (72.5 \text{ GPa})(0.40) = 30.4 \text{ GPa}
 \end{aligned}$$

This value for  $E_{cs}$  as well as those computed in a like manner for the three carbon fibers are listed in Table 16.D1.

Table 16.D1 Composite Elastic Modulus for Each of Glass and Three Carbon Fiber Types for  $V_f = 0.40$

Fiber Type	$E_{cs}$ (GPa)
Glass	30.4
Carbon—standard modulus	93.4
Carbon—intermediate modulus	115
Carbon—high modulus	161

It now becomes necessary to determine, for each fiber type, the inside diameter  $d_i$ . Rearrangement of Equation 16.23 such that  $d_i$  is the dependent variable leads to

$$d_i = \left[ d_0^4 - \frac{4FL^3}{3\pi E \Delta y} \right]^{1/4}$$

The  $d_i$  values may be computed by substitution into this expression for  $E$  the  $E_{cs}$  data in Table 16.D1 and the following

$$F = 1700 \text{ N}$$

$$L = 1.25 \text{ m}$$

$$\Delta y = 0.20 \text{ mm}$$