

B-8-15. Note that $G(s)$ has two open-loop poles in the right-half s plane, as seen from the following MATLAB output.

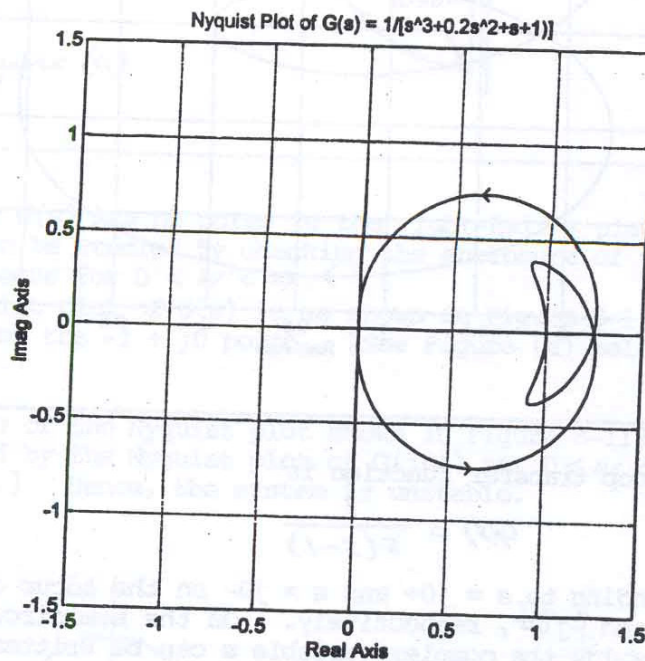
```
p = [1 0.2 1 1];
roots(p)

ans =

    0.2623 + 1.1451i
    0.2623 - 1.1451i
   -0.7246
```

The following MATLAB program produces the Nyquist plot shown below.

```
% ***** Nyquist plot *****
num = [0 0 0 1];
den = [1 0.2 1 1];
nyquist(num,den)
v = [-1.5 1.5 -1.5 1.5]; axis(v); axis('square')
grid
title('Nyquist Plot of G(s) = 1/[s^3+0.2s^2+s+1]')
```

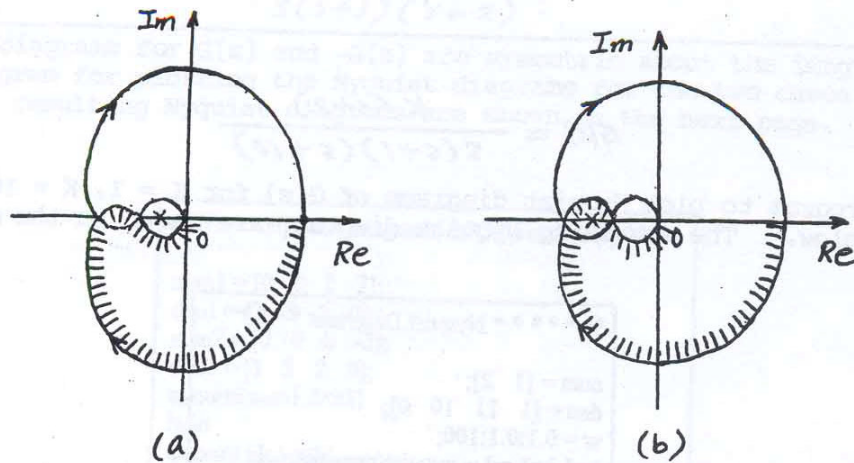


From the plot notice that the critical point $(-1+j0)$ is not encircled. Because there are two open-loop poles in the right-half s plane and no encirclement of the critical point, the closed-loop system is unstable.

B-8-18. Since $G(s)$ has no poles in the right-half s plane, the stability of the system can be studied by checking the enclosure of the $-1 + j0$ point by the Nyquist locus for $0 < \omega < \infty$.

If the Nyquist plot of $G(s)$ is as shown in Figure 8-119(a), then there is no enclosure of the $-1 + j0$ point. [See Figure (a) below.] Hence, the system is stable.

For the case of the Nyquist plot shown in Figure 8-119(b), the $-1 + j0$ point is enclosed by the Nyquist plot of $G(j\omega)$ for $0 < \omega < \infty$. [See Figure (b) below.] Hence, the system is unstable.

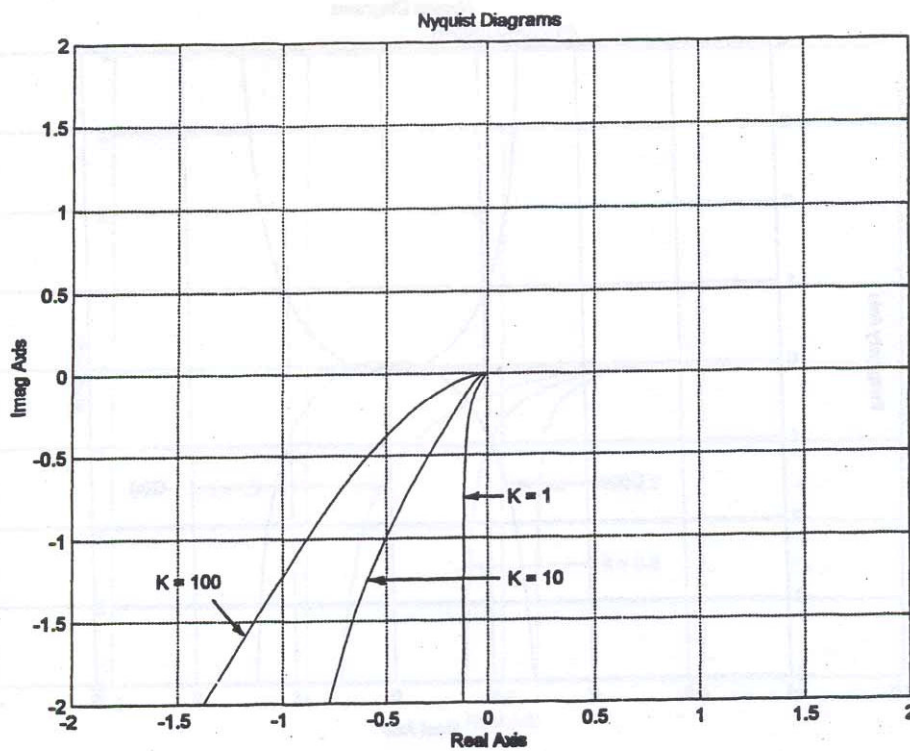


B-8-20.

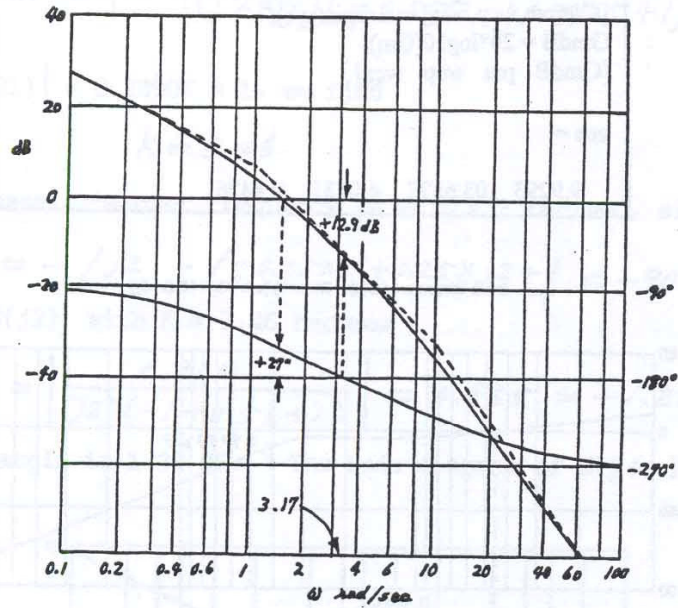
$$G(s) = \frac{K(s+2)}{s(s+1)(s+10)}$$

A MATLAB program to plot Nyquist diagrams of $G(s)$ for $K = 1$, $K = 10$, and $K = 100$ is shown below. The resulting Nyquist diagrams are shown on the next page.

```
%***** Nyquist Diagrams *****  
num = [1 2];  
den = [1 11 10 0];  
w = 0.1:0.1:100;  
[re1,im1,w] = nyquist(num,den,w);  
[re2,im2,w] = nyquist(10*num,den,w);  
[re3,im3,w] = nyquist(100*num,den,w);  
plot(re1,im1,re2,im2,re3,im3)  
v = [-2 2 -2 2]; axis(v)  
grid  
title('Nyquist Diagrams')  
xlabel('Real Axis')  
ylabel('Imag Axis')  
text(0.1,-0.75,'K = 1')  
text(0.1,-1.25,'K = 10')  
text(-1.6,-1.25,'K = 100')
```



B-8-27. A Bode diagram of the system is shown below.



From this Bode diagram, we find the phase margin and gain margin to be 27° and 13 dB, respectively.

The phase margin, gain margin, phase crossover frequency, and gain crossover frequency can be obtained easily with MATLAB. Use the command

```
[Gm, pm, wcp, wcg] = margin(sys)
```

See Problem B-8-28.
