



Student Name : SOLUTION \_\_\_\_\_

Student I.D. : \_\_\_\_\_

## American University of Beirut

### Faculty of Arts and Sciences

<b>Course Name</b> : Introductory Physics I	<b>Course Code</b> : PHYS 101
<b>Exam</b> : Quiz-1	<b>Sections</b> : All
<b>Date</b> : March 6, 2015	<b>Time</b> : 17:00 – 18:00
<b>Semester</b> : Spring	<b>Year</b> : 2014 - 2015
<b>Instructor</b> : Dr. Hani Hamzeh	<b>Exam Weight</b> : 20%

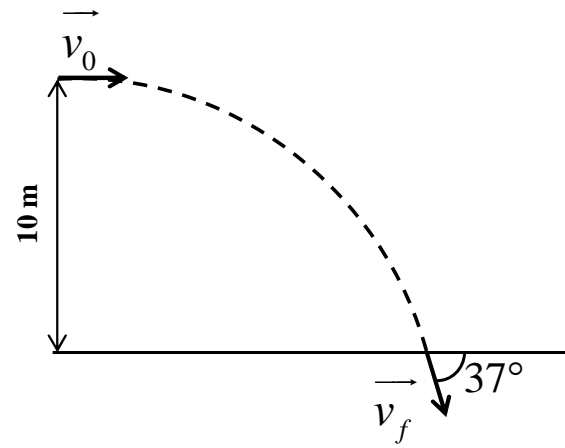
#### Instructions

- Time allowed: **60 minutes**
- Take  $g = 9.80 \text{ m/s}^2$
- Cheating in any way will result in an **F** grade
- Read each question carefully before answering
- Answer questions that you are confident about first.
- This exam consists of **7 pages** including this page
- Only standard (not programmable) calculators are allowed
- No documents are allowed
- Borrowing any instrument is forbidden

Problem #	Grade
Problem 1	/15
Problem 2	/5
Problem 3	/10
Problem 4	/10
Problem 5	/10
Problem 6	/10
<b>Total</b>	<b>/100</b>

**Problem-1** (15 points) (~ 15 min)

A ball is thrown horizontally with a speed  $v_0$  from a height of 10 m. It reaches the ground with an angle of  $37^\circ$  below the horizontal as shown in the figure. Neglect air resistance.



- (a) Find the initial speed  $v_0$  of the ball.  
 (b) How long does it take the ball to reach the ground?

$$\text{a) } v_{f_x} = v_f \cos 37 = v_{o_x} = v_0 \Rightarrow v_f = v_0 / \cos 37$$

$$v_{f_y} = -v_f \sin 37 = -v_0 \tan 37$$

constant acceleration, projectile motion  $\Rightarrow$

$$v_{f_y}^2 = v_{i_y}^2 + 2a_y \Delta y = 0 + 2(-9.80)(-10) = 196 \Rightarrow v_{f_y} = -14 \text{ m/s}$$

$$v_0 = \frac{-v_{f_y}}{\tan 37} = \frac{14}{\tan 37} = 18.6 \text{ m/s}$$

$$\text{b) } t = \frac{v_{f_y} - v_{i_y}}{a} = \frac{-14 - 0}{-9.80} = 1.43 \text{ s}$$

If the ball were thrown instead with an initial velocity of 9 m/s at an angle of  $30^\circ$  above the horizontal, from the same initial height:

- (c) What would then be the maximum height reached by the ball with respect to the ground?  
 (d) How far from the initial horizontal position would it reach the ground?

$$\text{c) } v_{i_y} = v_i \sin 30 = 9 \sin 30 = 4.5 \text{ m/s}$$

$$v_{f_y}^2 = v_{i_y}^2 + 2a_y \Delta y \Rightarrow \Delta y = y_{\max} - y_i = \frac{v_{f_y}^2 - v_{i_y}^2}{2a_y} = \frac{0 - 4.5^2}{2(-9.80)} = 1.03 \text{ m} \Rightarrow y_{\max} = 11.03 \text{ m}$$

$$\text{d) } \Delta y = v_{i_y} t - \frac{1}{2} g t^2 \text{ the total time of the flight can be found:}$$

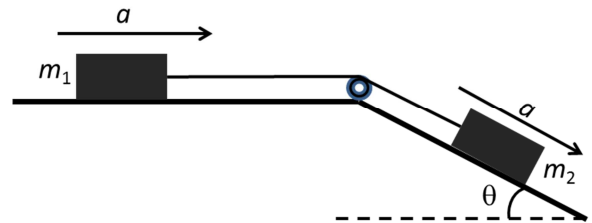
$$-10 = 4.5t - 4.9t^2 \Rightarrow 4.9t^2 - 4.5t - 10 = 0 \Rightarrow t = 1.96 \text{ s (only the positive solution is possible)}$$

$$\Delta x = v_{i_x} t = (v_i \cos 30)t = (9 \cos 30)1.96 = 15.3 \text{ m}$$

**Problem-2** (5 points) (~ 5 min)

Two blocks of masses  $m_1 = 3$  kg and  $m_2 = 5$  kg are connected by a string of negligible mass that passes over a frictionless mass-less pulley. Block  $m_1$  moves on a horizontal frictionless surface, while block  $m_2$  moves on a frictionless inclined plane making an angle  $\theta = 30^\circ$  with the horizontal.

- (a) Draw a free body diagram for each block.  
 (b) Find the tension in the string.



$$\text{Newton's second law on block } m_1 : \vec{T}_1 + m_1 \vec{g} + \vec{n}_1 = m_1 \vec{a}_1$$

$$\text{Newton's second law on block } m_2 : \vec{T}_2 + m_2 \vec{g} + \vec{n}_2 = m_2 \vec{a}_2$$

Since the two blocks are connected by a taut string and the pulley is frictionless and mass-less  $\Rightarrow a_1 = a_2$   
 since the string is also of negligible mass  $\Rightarrow T_1 = T_2$

Considering the system comprised of the two blocks and the string connecting them and using the "system approach" we first find  $a$

$$\text{Newton's second law for the system is } m_1 \vec{g} + m_2 \vec{g} + \vec{n}_1 + \vec{n}_2 = (m_1 + m_2) \vec{a}$$

If we take the projection along the direction of motion, with rightward as the positive direction:

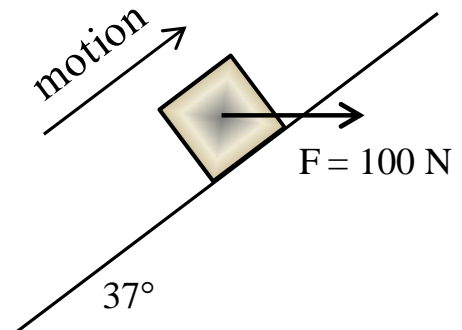
$$m_2 g \sin 30 = (m_1 + m_2) a \Rightarrow a = \frac{m_2 g \sin 30}{(m_1 + m_2)} = \frac{5 \times 9.80 \times \sin 30}{8} = 3.06 \text{ m/s}^2$$

If we isolate the block of mass  $m_1$  and project Newton's second law along the horizontal direction:

$$T = m_1 a = 3 \times 3.06$$

**Problem-3** (10 points) (~ 10 min)

A 4 kg block is pushed upward over a  $37^\circ$  rough incline by a constant horizontal force of 100 N (see figure). The block moves up the incline with a constant acceleration  $a = 3 \text{ m/s}^2$ . Find the magnitude of the coefficient of kinetic friction between the incline and the object ( $\mu_k = ?$ ).



Newton's second law

$$\sum \vec{F} = \vec{F} + \vec{n} + m\vec{g} + \vec{f}_k = m\vec{a}$$

Projection along  $x$  ( $x$  axis taken parallel to the incline and positive upwards)

$$F \cos 37 + 0 - mg \sin 37 - f_k = ma \quad (1)$$

$$\text{and } f_k = \mu_k n$$

Projection along  $y$

$$-F \sin 37 + n - mg \cos 37 + 0 = 0 \Rightarrow n = F \sin 37 + mg \cos 37 = 91.5 \text{ N}$$

$$\Rightarrow f_k = \mu_k (F \sin 37 + mg \cos 37)$$

if we replace in equation (1)

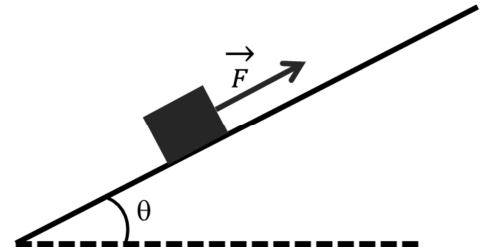
$$F \cos 37 - mg \sin 37 - \mu_k (F \sin 37 + mg \cos 37) = ma$$

$$\Rightarrow \mu_k = \frac{F \cos 37 - mg \sin 37 - ma}{F \sin 37 + mg \cos 37} = 0.48$$

**Problem-4** (10 points) (~ 10 min)

An object of weight 80 N is on an inclined plane that makes an angle  $\theta = 20^\circ$  with the horizontal. An upward force  $\vec{F}$  is applied on the object parallel to the inclined plane (see figure). The coefficient of static friction between the object and the inclined plane is  $\mu_s = 0.25$ .

- (a) If the object is not moving and if the force of static friction  $f_s$  is not equal to its maximum value, find an expression for  $f_s$ .
- (b) Calculate the minimum magnitude of the applied force  $\vec{F}$  that will start the object to move up the incline.



a) Newton along the incline:

$$F - f_s - mg \sin \theta = 0$$

$$f_s = F - mg \sin \theta$$

b) the minimum magnitude of the force  $F$  that will start the object moving up the incline is the one which causes the static friction force to reach its maximum value  $f_{s,\max} = \mu_s n$

$$F_{\min} - mg \sin \theta = f_{s,\max} = \mu_s n$$

Newton along the perpendicular to the incline:

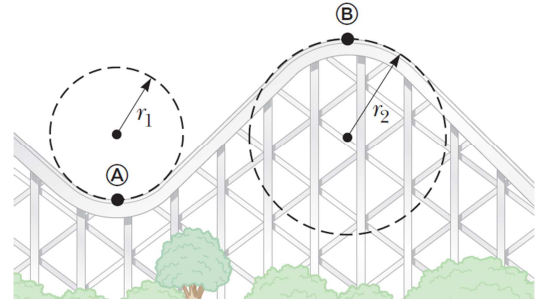
$$n - mg \cos \theta = 0 \Rightarrow n = mg \cos \theta \text{ and we replace this value in the equation giving us } F_{\min}$$

$$\Rightarrow F_{\min} = \mu_s mg \cos \theta + mg \sin \theta = 0.25 \times 80 \times \cos 20^\circ + 80 \times \sin 20^\circ = 46.16 \text{ N}$$

**Problem-5** (10 points) (~ 10 min)

A roller-coaster car has a mass of 500 kg when fully loaded with passengers. Assume the roller-coaster tracks at points A and B are parts of vertical circles of radius  $r_1 = 10.0$  m and  $r_2 = 15.0$  m, respectively.

- (a) If the vehicle has a speed of 20.0 m/s at point A, what is the force exerted by the track on the car at this point?  
 (b) What is the maximum speed the vehicle can have at point B and still remain on the track?



- a) We apply Newton's second law at point A, with  $v = 20.0$  m/s,  
 $n =$  force of track on roller coaster, and  $R = 10.0$  m:

$$\sum F = \frac{Mv^2}{R} = n - Mg$$

From this we find

$$n = Mg + \frac{Mv^2}{R} = 2.49 \times 10^4 \text{ N}$$

- b) At point B, the centripetal acceleration is now downward and Newton's second law now gives

$$\sum F = n - Mg = -\frac{Mv^2}{R}$$

The maximum speed at B corresponds to the case where the rollercoaster begins to fly off the track, or when  $n = 0$ . Then,

$$-Mg = -\frac{Mv_{\max}^2}{R} \Rightarrow v_{\max} = \sqrt{Rg} = 12.1 \text{ m/s}$$

**Problem-6** (10 points) (~ 10 min)

A skydiver of mass 80.0 kg jumps from a slow-moving aircraft and reaches a terminal speed of 50.0 m/s.

- (a) What is her acceleration when her speed is 30.0 m/s?  
 (b) What is the drag force on the skydiver when her speed is  
 i. 50.0 m/s?  
 ii. 30.0 m/s?

Given  $m = 80.0$  kg,  $v_T = 50.0$  m/s, we can write

If we apply Newton's second law along the vertical direction to the skydiver we have:

$$D - mg = -ma \Rightarrow \frac{1}{2} C \rho A v^2 - mg = -ma$$

When the skydiver reaches her terminal speed,  $a = 0$

$$\Rightarrow mg = \frac{C \rho A v_T^2}{2} \Rightarrow \frac{C \rho A}{2} = \frac{mg}{v_T^2} = 0.314 \text{ kg/m}$$

a) At  $v = 30.0$  m/s

$$a = g - \frac{C \rho A v^2 / 2}{m} = 9.80 \text{ m/s}^2 - \frac{(0.314 \text{ kg/m})(30.0 \text{ m/s})^2}{80.0 \text{ kg}} = 6.27 \text{ m/s}^2 \text{ downward}$$

b) i) At  $v = 50.0$  m/s, terminal velocity has been reached

$$\sum F_y = 0 = mg - D \Rightarrow D = mg = (80.0 \text{ kg})(9.80 \text{ m/s}^2) = 785 \text{ N directed upward}$$

ii) At  $v = 30.0$  m/s

$$\frac{C \rho A v^2}{2} = (0.314 \text{ kg/m})(30.0 \text{ m/s})^2 = 283 \text{ N directed upward}$$