

**AMERICAN UNIVERSITY OF BEIRUT
FACULTY OF ENGINEERING AND ARCHITECTURE
ELECTRICAL AND COMPUTER ENGINEERING DEPARTMENT
EECE 442 – Communications Systems**

QUIZ # 1

Closed book exam

**TWO SHEETS OF FORMULAS WITH NO PROBLEM SOLUTIONS ARE
ALLOWED**

TIME: 1 Hour and 15 minutes

Monday, April 4, 2005

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PROBLEM # 1

Consider the probability space $S = \{S_1, S_2, S_3, S_4, S_5, S_6\}$ corresponding to some random experiment. Let $P\{S_i\} = P_i, i=1, 2, 3, 4, 5, 6$.

- (a) Partition S into 3 mutually exclusive events subsets of S in such a way that each event contains at least one element of S . Let these events be denoted by A, B and C .
- (b) Use the axioms of probability and determine the probability of each of the events you specified in Part (a).
- (c) Determine $[P(A)+P(B)+P(C)]$ in terms of $P_i, i=1, 2, 3, 4, 5, 6$ and determine the numerical value of this probability sum. Justify your answer.

PROBLEM # 2

Consider a Gaussian random variable, X , having a mean equal to zero and variance equal to 1.

- (a) Express the cumulative distribution function of $X, F_X(x)$, using the integral of the probability density function of X .
- (b) Use the approximate plot of $f_X(x)$ and obtain the approximate plot of $F_X(x)$. What are the values of $F_X(x)$ at $-\infty, 0, \infty$.

PROBLEM # 3

Consider a zero-mean stationary random process $X(t)$ with autocorrelation function $R_X(\tau) = E[X(t+\tau)X(t)] = \exp\{-a|\tau|\}$, with $a > 0$ and $-\infty < \tau < \infty$.

- (a) Describe how the correlation between any two samples of $X(t)$ varies as the time difference between them increases.
- (b) Determine the time difference between any two samples of $X(t)$ that makes these samples uncorrelated.
- (c) Determine the value of the integral $\int_{-\infty}^{\infty} S_X(\omega) d\omega$, where $S_X(\omega)$ is the PSD of $X(t)$. You do not need to find $S_X(\omega)$.

PROBLEM # 4

Consider the following modulated signal:

$$s(t) = A_c \cos(\omega_c t) + A_c k_a m(t) \sin(\omega_c t).$$

- Determine the spectrum of $s(t)$, denoted $S(\omega)$, and plot its magnitude.
- Determine the bandwidth needed for the transmission of $s(t)$. The message signal $m(t)$ has a bandwidth equal to W .
- Suggest and describe the blocks that need to be used in the demodulation of $s(t)$.

PROBLEM # 5

DSB-LC has an inferior performance compared to DSB-SC under the presence of noise. This requires an increase in the transmission power of DSB-LC to achieve comparable performance with DSB-SC. Despite this fact, AM stations prefer to use DSB-LC signals. Consider the issue of receiver structure and explain the reason(s) for which DSB-LC signal transmission is preferable commercially.

PROBLEM # 6

Consider the establishment of an FM radio transmission system involving different FM stations. Each radio station is supposed to generate first a stereo signal occupying a bandwidth $W=52$ KHz. This stereo signal is then modulated using FM modulation and transmitted. Assume that due to technical reasons, the least modulation index β that can be generated is equal to 2.

- Determine the least separation between the transmission frequencies of the adjacent FM signals.
- Let the generation of each FM signal be done by generating first a NBFM signal with $\beta=0.1$. What is the frequency multiplication factor needed to obtain the WBFM signals transmitted by the radio stations?

PROBLEM # 7

Consider the following DSB-SC signal in the presence of narrow-band noise at the input of an envelope detector.

$$s(t) = A_c m(t) \sin(\omega_c t).$$

- Determine the signal and noise components at the output of the envelope detector. Assume large carrier-to-noise ratio.
- Repeat Part (a) when $s(t) = A_c m(t) \cos(\omega_c t)$.
- In Parts (a) and (b) determine the signal-to-noise ratios at the output of the envelope detector.