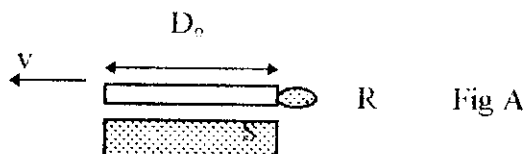




N.B. Write your name and ID number on the top of your booklet.

1)- 20 points

An observer  $S$  is standing on a platform of length  $D_0 = 65 \text{ m}$  on a space station. A rocket  $R$  passes at a speed  $v = 0.80c$  moving parallel to the edge of the platform. The observer  $S$  notes that the front and back of the rocket simultaneously line up with the ends of the platform at a particular instant (fig. A)



- According to  $S$ , what is the time necessary for the rocket to pass a particular point on the platform?
- What is the rest length  $L_0$  of the rocket?
- According to an observer  $S'$  on the rocket, what is the length  $D$  of the platform?
- According to  $S'$ , how long does it take for observer  $S$  to pass the entire length of the rocket?
- According to  $S$ , the ends of the rocket simultaneously line up with the ends of the platform. Are these events simultaneous to  $S'$ ?

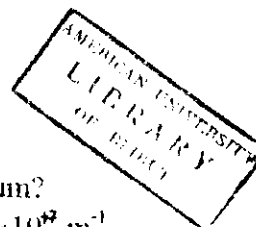
2)- 20 points

A certain accelerator produces a beam of neutral kaons ( $m_K c^2 = 498 \text{ MeV}$ ) with kinetic energy  $325 \text{ MeV}$ . Consider a kaon that decays in flight into two pions ( $m_\pi c^2 = 140 \text{ MeV}$ ). Find the kinetic energy of each pion in the special case in which the pions travel parallel or antiparallel to the direction of the kaon beam.

3)- 20 points

The discovery of the antiproton  $\bar{p}$  took place in 1956 at Berkeley through the following reaction:  $p + p \rightarrow p + p + p + \bar{p}$ , in which accelerated protons were incident on a target of protons at rest in the laboratory. When the product particles in the laboratory frame  $S$  move together as if they were a single unit, find

- the magnitude  $v'$  of the velocity of either reacting proton in the center-of-mass reference frame  $S'$ ,
- the velocity  $v$  of the incident protons in the laboratory frame.



4)- 20 points

What is the wavelength of the least energetic photon in the Balmer spectrum?

What is the wavelength of the series limit for the Balmer series?  $R = 1.097 \times 10^7 \text{ m}^{-1}$ .

5)- 20 points

X rays with  $\lambda = 100 \text{ pm}$  are scattered from a carbon target. The scattered radiation is viewed at  $90^\circ$  to the incident beam.

- What is the Compton shift  $\Delta\lambda$  ?
- What kinetic energy is imparted to the recoiling electron?

6)- 15 points

- For  $n=4$ , what is the largest allowed value of  $l$  ?
- What is the magnitude of the corresponding angular momentum ?
- How many different components on the z axis may this angular momentum vector have?
- What is the magnitude of the largest projected component ?
- What is the smallest angle that the angular momentum vector can make with the z-axis?

7)- 30 points

The wave function for the ground state of the hydrogen atom is given by

$$\psi(r) = \frac{1}{\sqrt{\pi a_0^3}} e^{-r/a_0}, \text{ in which } a_0 \text{ is the Bohr radius.}$$

- Show that the probability that an electron lies within a sphere of radius  $r$  is given by:  $P = 1 - e^{-2x} (1 + 2x + 2x^2)$ , in which  $x = r/a_0$ .
- Evaluate the probability that the electron, in the ground state, will be found between the spheres  $r = a_0$  and  $r = 2a_0$ .

8)- 15 points

The nuclide  $^{120}\text{Sn}$  ( $Z = 50$ ) has a filled proton shell, 50 being one of the magic nucleon numbers. The nuclide  $^{121}\text{Sb}$  ( $Z = 51$ ) has an extra proton outside this shell. According to the shell concept, this extra proton should be easier or harder to remove than a proton from the filled shell. ( $1u = 931.5 \text{ MeV}$ )

Nuclide	Z	N	Atomic Mass(u)
$^{121}\text{Sb}$	50+1	70	120.903821
$^{120}\text{Sn}$	50	70	119.902199
$^{119}\text{In}$	50-1	70	118.905819

9)- 30 points

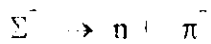
The  $\Omega^-$  baryon has  $S = -3$ .  $K^+$  and  $K^0$  have  $S = 1$ .  $\Xi^0$  and  $\Xi^-$  have  $S = -2$ .

While  $\Sigma^+$ ,  $\Sigma^0$ ,  $\Sigma^-$ ,  $\Lambda^0$  all have  $S = -1$ . All non strange particles such as  $p$ ,  $n$ , pions and  $\eta$ ,  $\eta'$  have  $S = 0$ . Each baryon is assigned a baryon number  $B = +1$ .

- a) It is desired to produce the  $\Omega^-$  using a beam of  $K^-$  incident on protons. What other particles are produced in this reaction? ( Use the three conservation laws for  $B$ ,  $S$  and  $Q$  ).
- b) How might the  $\Omega^-$  decay? ( knowing that the product particles can be  $\Lambda^0$ ,  $\Xi^0$ ,  $K^-$  and  $\pi^-$  ).

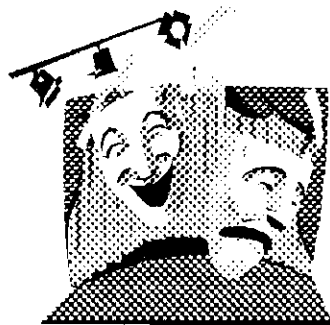
10)- 10 points

Analyze this process in terms of its quark content (  $u$ ,  $d$ , and  $s$  ).



Use data given in problem number 8 with the following table:

quark	charge ( unit e)	Baryon number	strangeness
u	2/3	+1/3	0
d	-1/3	+1/3	0
s	-1/3	+1/3	-1



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