

Hamad

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2. Select preliminary sizes:

To use same cross-section for both columns:

$$A_g \approx 152.8 / 0.85 \approx 179.8 \text{ in}^2 \quad \text{Try } (14 \times 14)$$

3. Are the columns slender?

$$\frac{Kl_u}{r} < 34-12 \frac{M_1}{M_2}$$

- column CD: $\ell_u = 20-2 = 18 \text{ ft}$
 $r \leq 0.3h = 0.3 \times 14 = 4.2 \text{ in.}$

$$\begin{aligned} \gamma_{top} &= \frac{\sum (EI/l_c)_{col.}}{\sum (EI/l)_{beams}} & I_c &= 0.7 I_g = 0.7 \times \frac{14 \times (4)^3}{12} = 2240.93 \text{ in}^4 \\ && I_b &= 0.35 I_g = 0.35 \times \frac{16 \times (24)^3}{12} = 6451.2 \text{ in}^4 \\ && l_c &= 24 \times 12 = 288 \text{ in} \\ && l_{c2} &= 19 \times 12 = 228 \text{ in} \end{aligned}$$

$$\gamma_{top} = \frac{2240.93/288 + 2240.93/228}{6451.2/360} = 0.98 \quad 57000 \sqrt{5000}$$

$$\begin{aligned} \gamma_{bot} &= \frac{4E_c I_c/l_c}{f(E_s) \text{subgrade modulus}} = \frac{4 \times 3.12 \times 10^6 \times 2240.93/228}{48(48)^3 \times 150 \text{ lb/in}^3} \\ &= 1.073 \end{aligned}$$

from nomograph $K = 0.806 \approx 0.81$

$$\text{So } \frac{Kl_u}{r} = \frac{0.81 \times 18 \times 12}{4.2} = 41.7 > 34-12 (-0.4) = 38.8$$

 \Rightarrow slender

- column DE: $\ell_u = 24-2 = 22 \text{ ft}$
 $r \leq 4.2 \text{ in.}$

$$\gamma_{top} = \frac{2240.93/288}{6451.2/25 \times 12} = 0.36$$

$$\gamma_{bot} = 0.98$$

from nomograph $K = 0.71$

$$\text{so } \frac{Kl_u}{r} = \frac{0.71 \times 22 \times 12}{4.2} = 24.6 > 34-12 (0.75) = 25$$

 \Rightarrow slender.

$\frac{Kl_u}{r} < 100$ for both cases \Rightarrow or use ACI moment magnification method