

## 4 - Computation of the magnified moments:

(a) For load case 1:

column is short

$$\Rightarrow \text{design for } P_u = 1128 \text{ k} \\ M_2 = M_u = 354 \text{ ft-k}$$

(b) For load case 2:

$$M_2 = M_{2ns} + \delta_s M_{2s}$$

$$M_{2ns} = 265 \text{ ft-k}$$

$$M_{2s} = 191 \text{ ft-k}$$

$$\delta_s = \frac{1}{1 - \frac{\Sigma P_u}{0.75 \Sigma P_c}} \geq 1.0$$

$$\bullet \Sigma P_u = 2 P_u (\text{int. col.}) + 2 P_u (\text{ext. col.})$$

$$P_u (\text{int. col.}) = 910 \text{ k}$$

$$P_u (\text{ext. col.}) = 0.75 (1.4 \times 160 + 1.7 \times 200 + 1.7 \times 50) \\ = 487 \text{ k}$$

$$\bullet \Sigma P_c = 2 P_c (\text{int. col.}) + 2 P_c (\text{ext. col.})$$

$$P_{c \text{ int.}} = \frac{\pi^2 EI}{(K L_u)^2} \quad K = 1.63 \quad L_u = 14 \times 12 - 30 = 138''$$

$$P_{c \text{ ext.}} = \frac{\pi^2 EI}{(K L_u)^2} \quad K = 2.1 \quad L_u = 138''$$

$$EI = \frac{0.4 E_c I_g}{(1 + \phi_d)}$$

$$\phi_d = \frac{\text{max. factored sustained shear}}{\text{total factored shear}} \\ = 0 \quad (\text{short-term wind load})$$

$$\Rightarrow EI = \frac{0.4 \times 57 \sqrt{4000} \times [18 \times (24)^3 / 12]}{(1 + 0)} \\ = 29.9 \times 10^6 \text{ k-in}^2$$

$$\Rightarrow P_{c \text{ int.}} = \frac{\pi^2 \times 29.9 \times 10^6}{(1.63 \times 138)^2} = 5832 \text{ kips}$$

$$P_{c \text{ ext.}} = \frac{\pi^2 \times 29.9 \times 10^6}{(2.1 \times 138)^2} = 3514 \text{ kips}$$