

## key solution

CHEN 490 – Fundamentals of Petroleum Engineering  
HW 5 (continued) – Due 28/11/2013

- ✓ 1. If the bore hole is  $8\frac{3}{4}$ " and using  $4\frac{1}{2}$ " OD drill pipe, what is the required flow rate if the minimum upward velocity is 195 ft/min?
- ✓ 2. Calculate the pressure drop in psi in 1500 ft of  $4\frac{1}{2}$ " ID pipe carrying oil ( sp. gr. = 0.825 and viscosity = 12 cp) at a rate of 1550 gal/min.
- ✓ 3. What is the total weight of 20 bbl. Of material whose sp.gr. is 4.3?
- ✓ 4. Calculate the density in all common units ( $\text{lb}_m/\text{ft}^3$ ,  $\text{lb}_m/\text{bbl}$ ,  $\text{gm}/\text{cm}^3$ ) of a fluid weighs 500 lbs?

1. Given : A drill pipe of  $4\frac{1}{2}$ " OD in  
A bore hole of  $8\frac{3}{4}$ " = 8.75"

Find : Flow rate of mud if  $v = 195$  ft/min. ?

Solution :

$$q = AV$$

Where  $q = \text{ft}^3/\text{sec}$

$$A = \text{ft}^2$$

$$v = \text{ft}/\text{sec}$$

then,

$$A = \frac{\pi}{4} \frac{(8.75)^2}{12} - \frac{\pi}{4} \frac{(4.5)^2}{12} = 0.307 \text{ ft}^2$$

$$v = \frac{195 \text{ ft}/\text{min}}{60 \text{ sec}/\text{min}} = 3.25 \text{ ft}/\text{sec}$$

and

$$q = (0.307)(3.25) = 1 \text{ ft}^3/\text{sec} = \underline{\underline{449 \text{ gal}/\text{min}}}$$

or

$$q = 2.45 (d_{\text{hole}}^2 - d_{\text{OD pipe}}^2) v$$

$$= 2.45 (8.75^2 - 4.5^2) \left(\frac{195}{60}\right) = \underline{\underline{448 \text{ gal}/\text{min}}}$$

2. Given: 1500' of 4" ID pipe of ~~air~~ oil flowing  
 (sp. gr. = 0.825) +  $\mu = 12 \text{ cp}$  @  
 a rate = 1550 gal/min

Find:  $\Delta P_f$  in psi?

Solution:

$$N_R = \frac{928 d \rho v}{\mu}, \quad d = 4''$$

$$\rho = (0.825)(8.34) = 6.88 \text{ lbm/gal}$$

$$v = \frac{Q}{A} = \frac{1550}{(2.45)(4)^2} = 39.5 \text{ ft/sec}$$

$$\mu = 12 \text{ cp}$$

then,

$$N_R = \frac{(928)(6.88)(4)(39.5)}{12} = 84064 > 2000 \rightarrow \text{turbulent flow}$$

then,

$$\Delta P_f = \frac{f \rho L v^2}{25.8(d)}, \quad f \approx 0.0055 \text{ (from curve II)}$$

$$\Delta P_f = \frac{(0.0055)(6.88)(1500)(39.5)^2}{(25.8)(4)}$$

$$= 858 \text{ psi}$$

858

3. Given: 20 bbl of material (sp. gr. = 4.3)  
Find: total weight

Solution:

$$T. wt. = (\rho)(Vol)$$

$$lb_m = \frac{lb_m}{bbl} (bbl) = (4.3) \left( 350 \frac{lb_m}{bbl} \right) (20 bbl)$$

$$= \underline{\underline{30100 lb_m}}$$

4. Given: <sup>Volume</sup> a fluid =  $3 ft^3$ , Weights = 500 lbs  
Find:  $\rho$  ? in  $lb_m/ft^3$ ,  $lb_m/bbl$ ,  $gm/cm^3$  ?

Solution:

$$\rho = \frac{500 lb_m}{3 ft^3} = 166.7 lb_m/ft^3$$

$$\rho = \frac{166.7 lb_m/ft^3}{7.48 gal/ft^3} = 22.3 lb_m/gal$$

$$\rho = (166.7 lb_m/ft^3) (5.615 ft^3/bbl) = 935.0 \frac{lb_m}{bbl}$$

$$\rho = \frac{(166.7 lb_m/ft^3) (454 gm/lb_m)}{(28320 cm^3/ft^3)}$$

$$= \underline{\underline{2.67 gm/cm^3}}$$