

1 2nd order system

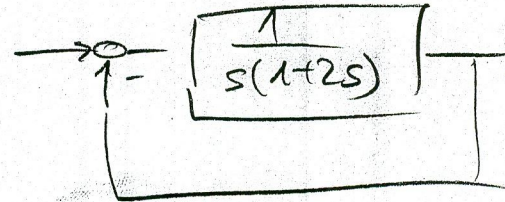
b

The open loop transfer function of a unity feedback system is

$$G(s) = \frac{1}{s(1+2s)}$$

The desired performance specifications are:

- peak time $t_p = 1$ sec
- Overshoot $M_p \approx 5\%$



$$G_o(s) = \frac{K}{2s^2 + s + K}$$

Can those requirements be met?

a) yes

b) no

$$s^2 + \frac{1}{2}s + \frac{k}{2} \Rightarrow \omega_n = \frac{k}{2}$$

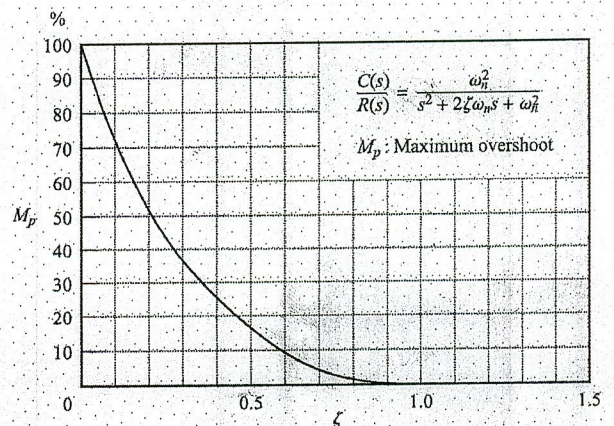
$$2\zeta\omega_n = \frac{1}{2}$$

$$\Rightarrow \zeta = \frac{1}{2\omega_n \cdot 2} = \frac{1}{4\omega_n}$$

$$M_p \approx 5\% \Rightarrow \zeta = 0,7$$

$$\Rightarrow 0,7 = \frac{1}{4\omega_n} \Rightarrow \omega_n = 0,357$$

$$t_p = \frac{\pi}{\omega_d} = \frac{\pi}{\omega_n \sqrt{1-\zeta^2}} = 12,3 \text{ s}$$



2 Routh

Suppose that unity feedback is to be applied around the open loop system:

$$G_{ol} = \frac{2(s+2)}{s^2(s+1)}$$

Then the closed loop has

- a) no poles in RHP (right half plane)
- b) 1 pole in RHP
- c) 2 poles in RHP

$$1 + G_o(s) =$$

$$s^3 + s^2 + 2s + 4 = 0$$

$$\begin{array}{r} s^3 \\ s^2 \\ s \\ 1 \end{array} \begin{array}{r} 1 \\ 1 \\ -2 \\ 4 \end{array} \begin{array}{r} 2 \\ 4 \\ \\ 4 \end{array}$$

3 System type

Two feedback systems are shown below:

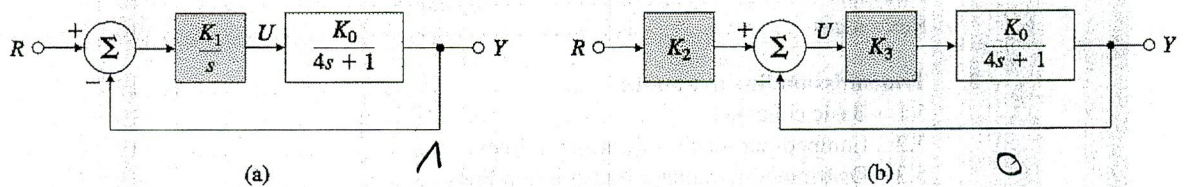


Figure 1: Two feedback systems

The system types are:

- a) system a: type 2, system b: type 1
- b) system a: type 1, system b: type 1
- c) system a: type 1, system b: type 0**
- d) system a: type 2, system b: type 0

4 Steady state error

Consider the system below:

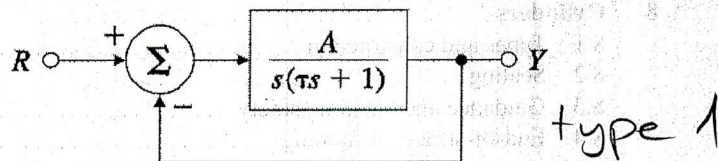


Figure 2: Feedback system

The steady state error due to ramp input $R(s) = \frac{r_0}{s}$ is

- a) $e_\infty = \frac{r_0}{A}$**
- b) $e_\infty = \frac{A}{r_0}$
- c) none of the above

$$e_\infty = \frac{r_0}{K_v}$$

$$K_v = \lim_{s \rightarrow 0} s G(s)$$

$$= A$$

$$\Rightarrow e_\infty = \frac{r_0}{A}$$



5 True or false

The final value theorem is only applicable for stable systems

- a) True
- b) False

6 True or false

Stability of a system does not depend on the kind of system input

- a) True
- b) False

7 True or false

Overshoot of a second order system depends mainly on the system damping ratio but also on the natural undamped frequency

- a) True
- b) False