## Homework \# 3 - Solution

## CIVE 646 - Water Resources Systems: Planning and Management

(Fall 2011-12)
Topics: 5) Multicriteria Decision Analysis

## Problems

5.1 The following performance matrix is for a multicriteria decision making problem related to a water resources project:

|  | $\mathbf{g}_{\mathbf{1}}$ | $\mathbf{g}_{\mathbf{2}}$ | $\mathbf{g}_{\mathbf{3}}$ | $\mathbf{g}_{\mathbf{4}}$ | $\mathbf{g}_{\mathbf{5}}$ | $\mathbf{g}_{\mathbf{6}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Min/Max | Min | Max | Min | Min | Min | Max |
| $\mathbf{a}_{\mathbf{1}}$ | 80 | 90 | 600 | 54 | 8 | 5 |
| $\mathbf{a}_{\mathbf{2}}$ | 65 | 58 | 200 | 97 | 1 | 1 |
| $\mathbf{a}_{\mathbf{3}}$ | 83 | 60 | 400 | 72 | 4 | 7 |
| $\mathbf{a}_{\mathbf{4}}$ | 40 | 80 | 1000 | 75 | 7 | 10 |
| $\mathbf{a}_{\mathbf{5}}$ | 52 | 72 | 600 | 20 | 3 | 8 |
| $\mathbf{a}_{\mathbf{6}}$ | 94 | 96 | 700 | 36 | 5 | 6 |

$\boldsymbol{A}$ is the set of alternatives and $\boldsymbol{G}$ is the set of criteria.
$\mathrm{g}_{1}$ : estimated annual maintenance cost (M US\$)
$\mathrm{g}_{2}$ : technical value (rating score out of 100 )
$\mathrm{g}_{3}$ : construction cost (M US\$)
$\mathrm{g}_{4}$ : annual operation cost (M US\$)
$\mathrm{g}_{5}$ : environmental impact (rating score out of 10 )
$\mathrm{g}_{6}$ : estimated water supply ( $10^{3} \mathrm{~m}^{3} /$ day $)$
Rank the alternatives using Promothee method. Apply the following parameters:

| Criterion | Type | Parameters | Weight |
| :---: | :---: | :---: | :---: |
| $\mathrm{g}_{1}$ |  | $\mathrm{q}=10$ | 1 |
| $\mathrm{g}_{2}$ |  | $\mathrm{p}=30$ | 1 |
| $\mathrm{g}_{3}$ | $\underset{\sigma_{q}}{\sqrt{p}}$ | $\mathrm{q}=50, \mathrm{p}=500$ | 1 |
| $\mathrm{g}_{4}$ | $\underset{q}{\sqrt{p}}$ | $\mathrm{q}=10, \mathrm{p}=60$ | 1 |
| $\mathrm{g}_{5}$ | $1$ | - | 1 |
| $\mathrm{g}_{6}$ | $p$ | $\mathrm{p}=2$ | 1 |

## Solution:

## g1(a):

Criterion to be minimized:
$\mathrm{g} 1(\mathrm{a} 1)-\mathrm{g} 1(\mathrm{a} 2)=15$
and therefore:

$\mathrm{c} 1(\mathrm{a} 1, \mathrm{a} 2)=0$
c1 $(\mathrm{a} 2, \mathrm{a} 1)=1$
g2(a):
Criterion to be maximized:
$\mathrm{g} 2(\mathrm{a} 1)-\mathrm{g} 2(\mathrm{a} 2)=32$
and therefore:
$\mathrm{c} 2(\mathrm{a} 1, \mathrm{a} 2)=1$
c2 $(a 2, a 1)=0$
g3(a):
Criterion to be minimized:
$\mathrm{g} 3(\mathrm{a} 1)-\mathrm{g} 3(\mathrm{a} 2)=32$
and therefore:
c3 3 a1, a2) $=1$
$\mathrm{c} 3(\mathrm{a} 2, \mathrm{a} 1)=0.778$
g4(a):
Criterion to be minimized:
$\mathrm{g} 4(\mathrm{a} 1)-\mathrm{g} 4(\mathrm{a} 2)=-43$
and therefore:
$\mathrm{c} 4(\mathrm{a} 1, \mathrm{a} 2)=0.5$
$c 4(\mathrm{a} 2, \mathrm{a} 1)=0$
g5(a):
Criterion to be minimized:
$\mathrm{g} 5(\mathrm{a} 1)-\mathrm{g} 5(\mathrm{a} 2)=7$
and therefore:
$c 5(\mathrm{a} 1, \mathrm{a} 2)=0$

$\mathrm{c} 5(\mathrm{a} 2, \mathrm{a} 1)=1$

## g6(a):

Criterion to be maximized:

$\mathrm{c} 6(\mathrm{a} 1, \mathrm{a} 2)=1$
$\mathrm{c} 6(\mathrm{a} 2, \mathrm{a} 1)=0$

|  | g 1 | g 2 | g 3 | g 4 | g 5 | g 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{c}(\mathrm{a} 1, \mathrm{a} 2)$ | 0 | 1 | 0 | 0.5 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 1, \mathrm{a} 3)$ | 0 | 1 | 0 | 0.5 | 0 | 0 |
| $\mathrm{c}(\mathrm{a} 1, \mathrm{a} 4)$ | 0 | 0.33 | 0.78 | 0.5 | 0 | 0 |
| $\mathrm{c}(\mathrm{a} 1, \mathrm{a} 5)$ | 0 | 0.6 | 0 | 0 | 0 | 0 |
| $\mathrm{c}(\mathrm{a} 1, \mathrm{a} 6)$ | 1 | 0 | 0.11 | 0 | 0 | 0 |
| $\mathrm{c}(\mathrm{a} 2, \mathrm{a} 1)$ | 1 | 0 | 0.78 | 0 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 2, \mathrm{a} 3)$ | 1 | 0 | 0.33 | 0 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 2, \mathrm{a} 4)$ | 0 | 0 | 1 | 0 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 2, \mathrm{a} 5)$ | 0 | 0 | 0.78 | 0 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 2, \mathrm{a} 6)$ | 1 | 0 | 1 | 0 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 3, \mathrm{a} 1)$ | 0 | 0 | 0.33 | 0 | 1 | 1 |
| $\mathrm{c}(\mathrm{a} 3, \mathrm{a} 2)$ | 0 | 0.067 | 0 | 0.5 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 3, \mathrm{a} 4)$ | 0 | 0 | 1 | 0 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 3, \mathrm{a} 5)$ | 0 | 0 | 0.33 | 0 | 0 | 0 |
| $\mathrm{c}(\mathrm{a} 3, \mathrm{a} 6)$ | 1 | 0 | 0.55 | 0 | 1 | 0.5 |
| $\mathrm{c}(\mathrm{a} 4, \mathrm{a} 1)$ | 1 | 0 | 0 | 0 | 1 | 1 |
| $\mathrm{c}(\mathrm{a} 4, \mathrm{a} 2)$ | 1 | 0.73 | 0 | 0.5 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 4, \mathrm{a} 3)$ | 1 | 0.67 | 0 | 0 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 4, \mathrm{a} 5)$ | 1 | 0.267 | 0 | 0 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 4, \mathrm{a} 6)$ | 1 | 0 | 0 | 0 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 5, \mathrm{a} 1)$ | 1 | 0 | 0 | 0.5 | 1 | 1 |
| $\mathrm{c}(\mathrm{a} 5, \mathrm{a} 2)$ | 1 | 0.47 | 0 | 1 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 5, \mathrm{a} 3)$ | 1 | 0.4 | 0 | 0.5 | 1 | 0.5 |
| $\mathrm{c}(\mathrm{a} 5, \mathrm{a} 4)$ | 0 | 0 | 0.78 | 0.5 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 5, \mathrm{a} 6)$ | 1 | 0 | 0.11 | 0.5 | 1 | 1 |
| $\mathrm{c}(\mathrm{a} 6, \mathrm{a} 1)$ | 0 | 0.2 | 0 | 0.5 | 1 | 0.5 |
| $\mathrm{c}(\mathrm{a} 6, \mathrm{a} 2)$ | 0 | 1 | 0 | 1 | 0 | 1 |
| $\mathrm{c}(\mathrm{a} 6, \mathrm{a} 3)$ | 0 | 1 | 0 | 0.5 | 0 | 0 |
| $\mathrm{c}(\mathrm{a} 6, \mathrm{a} 4)$ | 0 | 0.53 | 0.55 | 0.5 | 1 | 0 |
| $\mathrm{c}(\mathrm{a} 6, \mathrm{a} 5)$ | 0 | 0.8 | 0 | 0 | 0 | 0 |


| S | a1 | a2 | a3 | a4 | a5 | a6 | $\phi^{+}$ | $\phi=\phi^{+}-\phi^{-}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a1 |  | 0.417 | 0.25 | 0.268 | 0.1 | 0.185 | 1.22 | -1.081 |
| a 2 | 0.463 |  | 0.388 | 0.33 | 0.297 | 0.5 | 1.978 | - 0.308 |
| a3 | 0.388 | 0.261 |  | 0.33 | 0.055 | 0.508 | 1.542 | -0.358 |
| a4 | 0.5 | 0.538 | 0.445 |  | 0.378 | 0.33 | 2.191 | 0.453 |
| a5 | 0.583 | 0.57 | 0.567 | 0.38 |  | 0.6 | 2.71 | 1.74 |
| a6 | 0.367 | 0.5 | 0.25 | 0.43 | 0.133 |  | 1.68 | -0.443 |


| $\phi^{-}$ | 2.301 | 2.286 | 1.9 | 1.738 | 0.962 | 2.123 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |

## Ranking of alternatives:


5.2 The Lebanese government intends to construct a treatment plant for wastewater disposal in the Sour drainage Zone (South Lebanon). Four alternatives were identified as follows:

Alternative 1 (A1): Treatment of all wastewater generated in the area at a single WWTP located on the coast.
Alternative 2 (A2): Coastal WWTP plus four smaller inland WWTPs
Alternative 3 (A3): Coastal WWTP plus a WWTP for each interior village
Alternative 4 (A4): Coastal WWTP and upgrading of the existing septic tanks in the interior villages

The decision matrix is as follows:

|  | Cost (Million \$) | Technical rating | Environmental rating |
| :---: | :---: | :---: | :---: |
| Max/Min | Min | Min | Max |
| A1 | 124 | 16 | 16 |
| A2 | 140 | 26 | 21 |
| A3 | 142 | 24 | 20 |
| A4 | 122 | 15 | 16 |

Rank the four alternative using Promothee method using the following parameters:

|  | Cost (Million \$) | Technical rating | Environmental rating |
| :---: | :---: | :---: | :---: |
| Weight | 0.8 | 0.5 | 0.5 |
| Preference | $\mathrm{Q}=2, \mathrm{p}=10$ | $\mathrm{q}=2, \mathrm{p}=5$ | $\mathrm{q}=2, \mathrm{p}=6$ |
| $\overbrace{\mathrm{q}}^{\mathrm{P}}$ |  |  |  |

## Solution:

|  | Cost | Technical | Environment |
| :---: | :---: | :---: | :---: |
| weights | 0.8 | 0.5 | 0.5 |
| c(A1,A2) | 1 | 1 | 0 |
| c(A1,A3) | 1 | 1 | 0 |
| c(A1,A4) | 0 | 0 | 0 |
| c(A2,A1) | 0 | 0 | 0.75 |
| c(A2,A3) | 0 | 0 | 0 |
| c(A2,A4) | 0 | 0 | 0.75 |
| c(A3,A1) | 0 | 0 | 0.5 |
| c(A3,A2) | 0 | 0 | 0 |


| $\mathrm{c}(\mathrm{A} 3, \mathrm{~A} 4)$ | 0 | 0 | 0.5 |
| :---: | :---: | :---: | :---: |
| $\mathrm{c}(\mathrm{A} 4, \mathrm{~A} 1)$ | 0 | 0 | 0 |
| $\mathrm{c}(\mathrm{A} 4, \mathrm{~A} 2)$ | 1 | 1 | 0 |
| $\mathrm{c}(\mathrm{A} 4, \mathrm{~A} 3)$ | 1 | 1 | 0 |


| $\mathbf{S}$ | $\mathbf{A 1}$ | $\mathbf{A 2}$ | $\mathbf{A 3}$ | $\mathbf{A 4}$ |
| :---: | :---: | :---: | :---: | :---: |
| A1 |  | 0.722 | 0.722 | 0 |
| A2 | 0.208 |  | 0 | 0.208 |
| A3 | 0.139 | 0 |  | 0.139 |
| A4 | 0 | 0.722 | 0.722 |  |
| A4 |  |  |  |  |$\quad$| $\phi^{+}$ |
| :---: |
| $\mathbf{1 . 4 4 4}$ |
| $\mathbf{0 . 4 1 6}$ |
| $\mathbf{0 . 2 7 8}$ |
| $\mathbf{1 . 4 4 4}$ |$\quad$| $\phi=\phi^{+}-\phi^{-}$ |
| :---: | :---: |
| $\mathbf{1 . 0 9 7}$ |
| $\mathbf{- 1 . 0 2 8}$ |
| $\mathbf{- 1 . 1 6 6}$ |
| $\mathbf{1 . 0 9 7}$ |


| $\phi^{-}$ | 0.347 | 1.444 | 1.444 | 0.347 |
| :---: | :--- | :--- | :--- | :--- |

## Ranking of alternatives:


5.3 Reformulate and solve the problem 5.2 by introducing the following environmental concerns:

- Minimize discharge into Mediterranean
- Minimize discharge to surface waters
- Minimize discharge into groundwater
- Highest potential source of irrigation water for interior areas
- Minimize sludge production
- Minimize space requirement
- Minimize impact to areas of high protection value because of rareness of environment
- Minimize impairment of historical or cultural monuments
- Not creating mosquito breeding areas
- Not causing diseases by use of effluent for irrigation

Use a Maximization rating scale between 1 and 4 to evaluate the above mentioned environmental concerns.

## Solution:

|  | A1 | A2 | A3 | A4 |
| :--- | :---: | :---: | :---: | :---: |
| Minimize discharge into Mediterranean | 4 | 2 | 1 | 1 |
| Minimize discharge to surface waters | 1 | 4 | 4 | 2 |
| Minimize discharge into groundwater | 1 | 2 | 2 | 4 |
| Highest potential source of irrigation water for interior areas | 3 | 2 | 2 | 3 |
| Minimize sludge production | 2 | 2 | 2 | 1 |
| Minimize space requirement | 1 | 1 | 1 | 1 |
| Minimize impact to areas of high protection value because of <br> rareness of environment | 1 | 1 | 1 | 1 |
| Minimize impairment of historical or cultural monuments | 1 | 1 | 1 | 1 |
| Not creating mosquito breeding areas | 1 | 3 | 3 | 1 |
| Not causing diseases by use of effluent for irrigation | 1 | 3 | 3 | 1 |
| Total Environmental rating | $\mathbf{1 6}$ | $\mathbf{2 1}$ | $\mathbf{2 0}$ | $\mathbf{1 6}$ |

The total Environmental rating of each alternative is the same as problem 5.2

## Ranking of alternatives: same as problem 5.2

5.4 A water supply project consists of identifying the most suitable development scenario for water supply in the Sour region. Of necessity the choice of alternatives must consider various criteria; cost (investment, operation and maintenance costs), water quality, water quantity, ...

## Present water sources:

The existing water supply in Sour area is provided from:

| Source | Capacity $\left(\mathrm{m}^{3} / \mathrm{day}\right)$ |
| :--- | :---: |
| Ras el Ain source | 15,000 |
| Er Rachidiye spring | 10,000 |
| Ouadi Jilo artesian wells | 10,000 |
|  | Total |

The water demand for the area in the year 2015 is estimated to $90,000 \mathrm{~m}^{3} / \mathrm{day}$.
Two alternatives were identified:
Alternative 1: The concept of alternative 1 is to concentrate the majority of the official water supply at Ras el Ain in order to make maximum use of the good quality water which comes naturally from these springs. The total development for this alternative consists of:

- Extension of WTP for Ras el Ain source to provide an additional capacity of $50,000 \mathrm{~m}^{3} / \mathrm{day}$
- Construction of new pumping station at Ras el Ain
- Construction of new transmission pipelines from Ras el Ain to Hanaouay and Saddiqine regional reservoirs
- Construction of new distribution pipelines

The detailed construction cost of this alternative is as follows:

| Construction Works | Cost Million \$ |
| :--- | :---: |
|  <br> pumping station | 4,1 |
| Transmission networks | 8,9 |
| Distribution networks | 4,6 |

Alternative 2: The concept of this alternative is to provide more dispersed sources of supply rather than concentrating on the major source of Ras el Ain. It consists of:

- Extension of WTP for Ras el Ain source to provide an additional capacity of $20,000 \mathrm{~m}^{3} / \mathrm{day}$
- Drilling new artesian wells in different locations in the region of a capacity of $20,000 \mathrm{~m}^{3} /$ day
- Construction of new transmission pipelines
- Construction of new distribution pipelines

The detailed construction cost of this alternative is as follows:

| Construction Works | Cost Million \$ |
| :--- | :---: |
|  <br> drilling new wells | 3,6 |
| Transmission networks | 9,9 |


| Distribution networks | 4,6 |
| :--- | :---: |
| Land | 0,2 |

1- Propose criteria to perform multicriteria decision analysis.
2- Propose methods to evaluate the identified criteria.
3- Construct the performance matrix.
4- Rank the alternatives using Promothee method.

## Solution:

Solution depends on criteria and methods of evaluation selected by students

