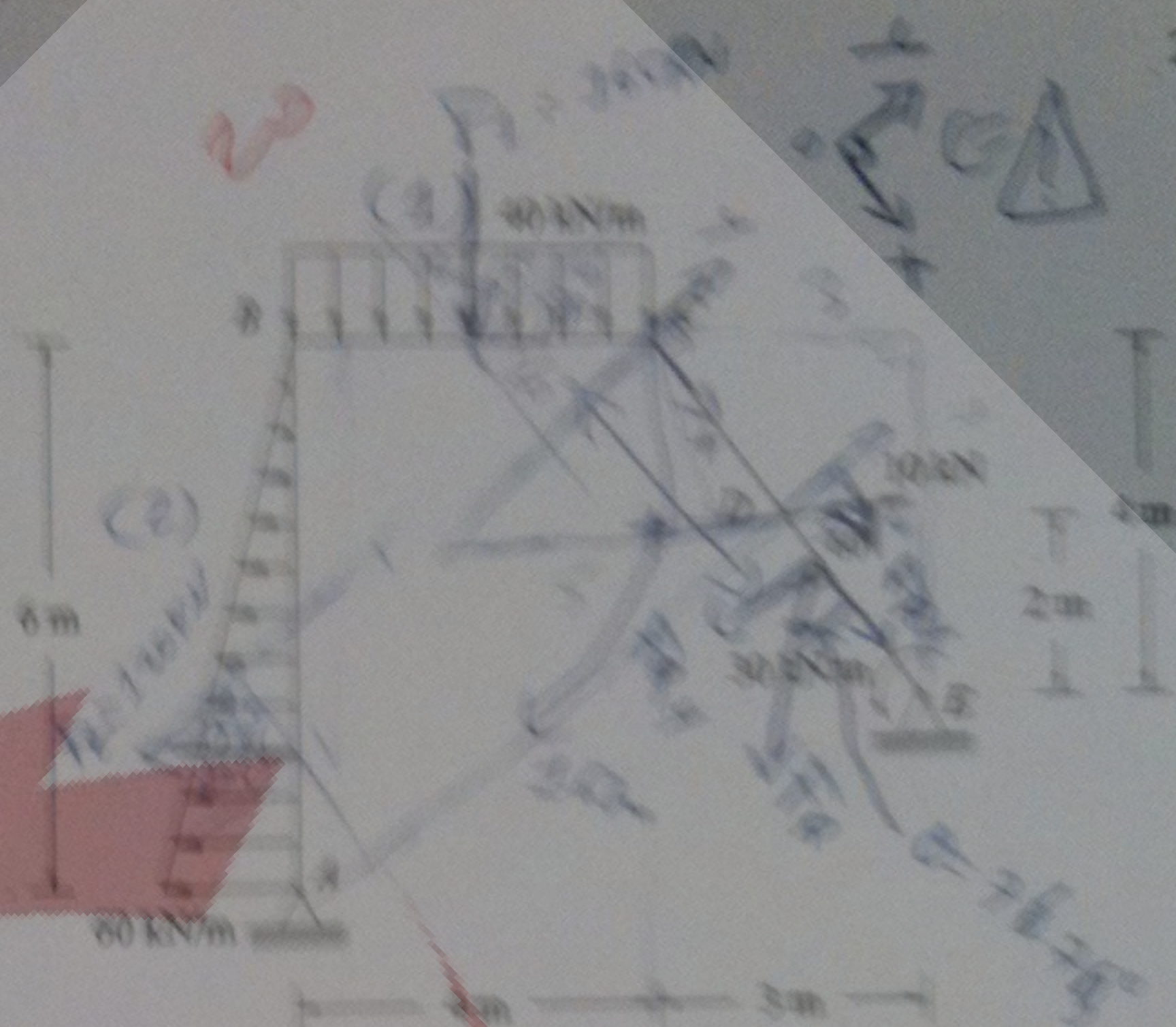


PROBLEM 1: (30 points)

Replace all the loading by an equivalent resultant force and specify where its line of action intersects member EC measured from point C.



$$F_1 = 40 \text{ kN/m} \times 4 = 160 \text{ kN}$$

Located at: $\bar{x}_1 = \frac{4}{2} = 2 \text{ m from C}$

$$F_2 = \left(\frac{1}{2} \times 60 \text{ kN/m} \right) \times 4 = 120 \text{ kN}$$

Located at: $\bar{x}_2 = 4 - \left(\frac{1}{3} \times 4 \right) = 4 - \frac{4}{3} = 2.67 \text{ m from C}$

$$\sum F_x = 160 \times (\cos 30^\circ) - 120 \times (\cos 60^\circ) + 10 \times (\cos 60^\circ)$$

$$\sum F_x = 53.56 \text{ kN}$$

$$\sum F_y = -160 \times (\sin 30^\circ) - 120 \times (\sin 60^\circ) + 10 \times (\sin 60^\circ)$$

$$\sum F_y = -227.22 \text{ kN}$$

$$F_R = \sqrt{F_x^2 + F_y^2} = \sqrt{(53.56)^2 + (-227.22)^2} = 233.64 \text{ kN}$$

$$\theta = \tan^{-1} \left(\frac{F_y}{F_x} \right) = \tan^{-1} \left(\frac{-227.22}{53.56} \right) = 76.73^\circ$$

$$\sum M_C = 160 \times 2 - 120 \times 2.67 + 10 \times (2.5) \times (2.5)$$

$$\sum M_C = -378.35 \text{ kNm}$$

$$\sum M_C = F_R \times x = 233.64 \times x = 378.35$$

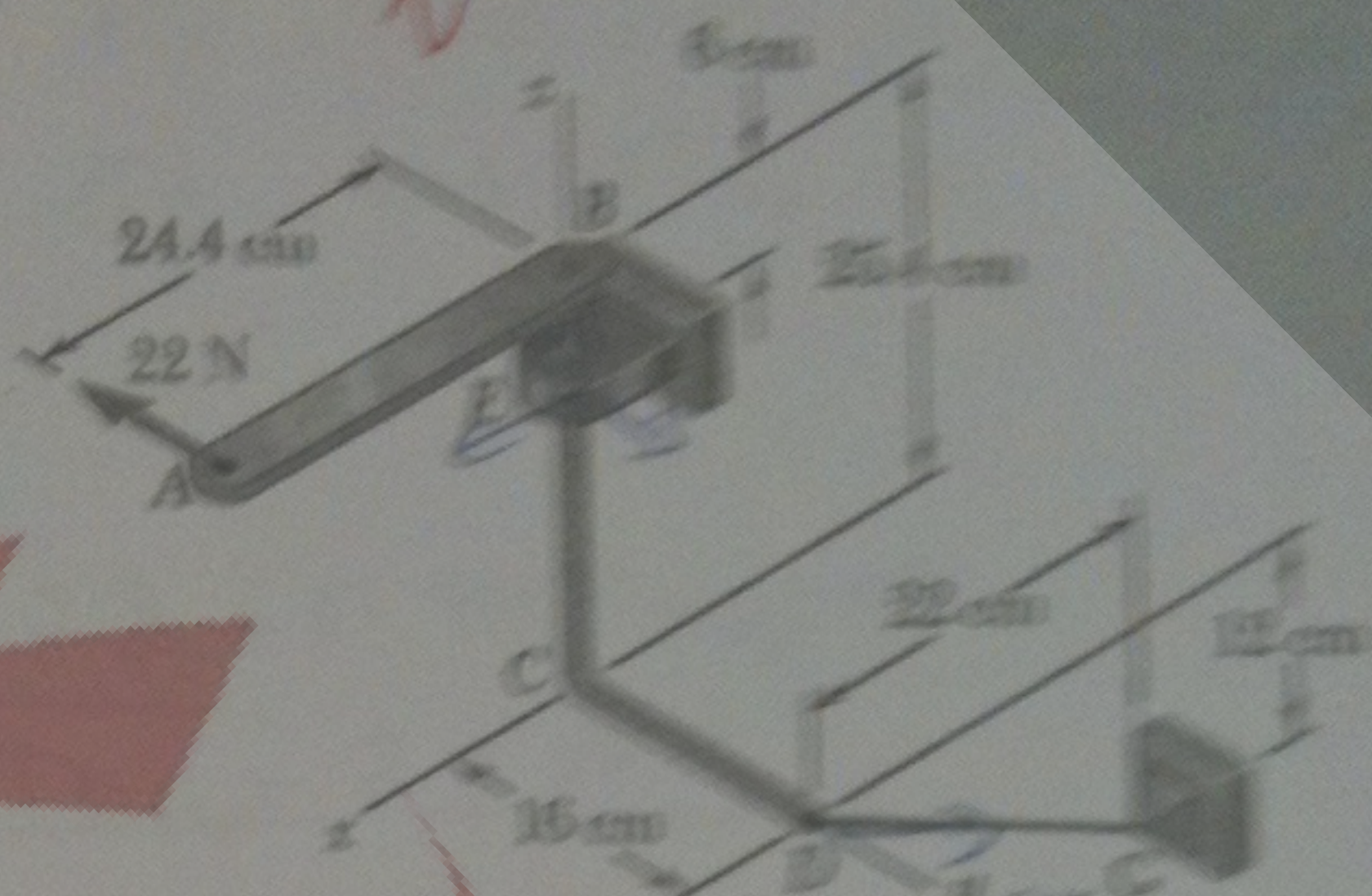
$$x = \frac{378.35}{233.64} = 1.62 \text{ m from C}$$

PROBLEM 2: (35 points)

The lever AB is welded to the bent rod BCD which is supported by a thrust bearing E and by cable DG . Determine:

- The tension in the cable DG ,
- The reactions at E .

N.B.: the order by which the tension in the cable DG and the reactions at E are calculated is not important.



$$A (0.244; 0; 0.254)$$

$$B (0; 0; 0.254)$$

$$C (0, 0, 0)$$

$$D (0, 0.16, 0)$$

$$G (-0.22; 0.16; 0.12)$$

$$E (0, 0, 0.194)$$

$$\vec{F}_A = -22\vec{j}$$

$$\vec{F}_E = E_x\vec{i} + E_y\vec{j} + E_z\vec{k}$$

$$\vec{T}_{DG} = T_{DG} \cdot \vec{u}_{DG}$$

$$\vec{u}_{DG} = \frac{\vec{T}_{DG}}{T_{DG}} = \frac{-0.22\vec{i} + 0.16\vec{j} - 0.12\vec{k}}{0.25} = -0.88\vec{i} + 0.64\vec{j} - 0.48\vec{k}$$

$$\Rightarrow \vec{T}_{DG} = -0.22T_{DG}\vec{i} + 0.64T_{DG}\vec{j} - 0.48T_{DG}\vec{k}$$

$$\sum \vec{F} = 0;$$

$$\vec{F}_A + \vec{F}_E + \vec{T}_{DG} = 0$$

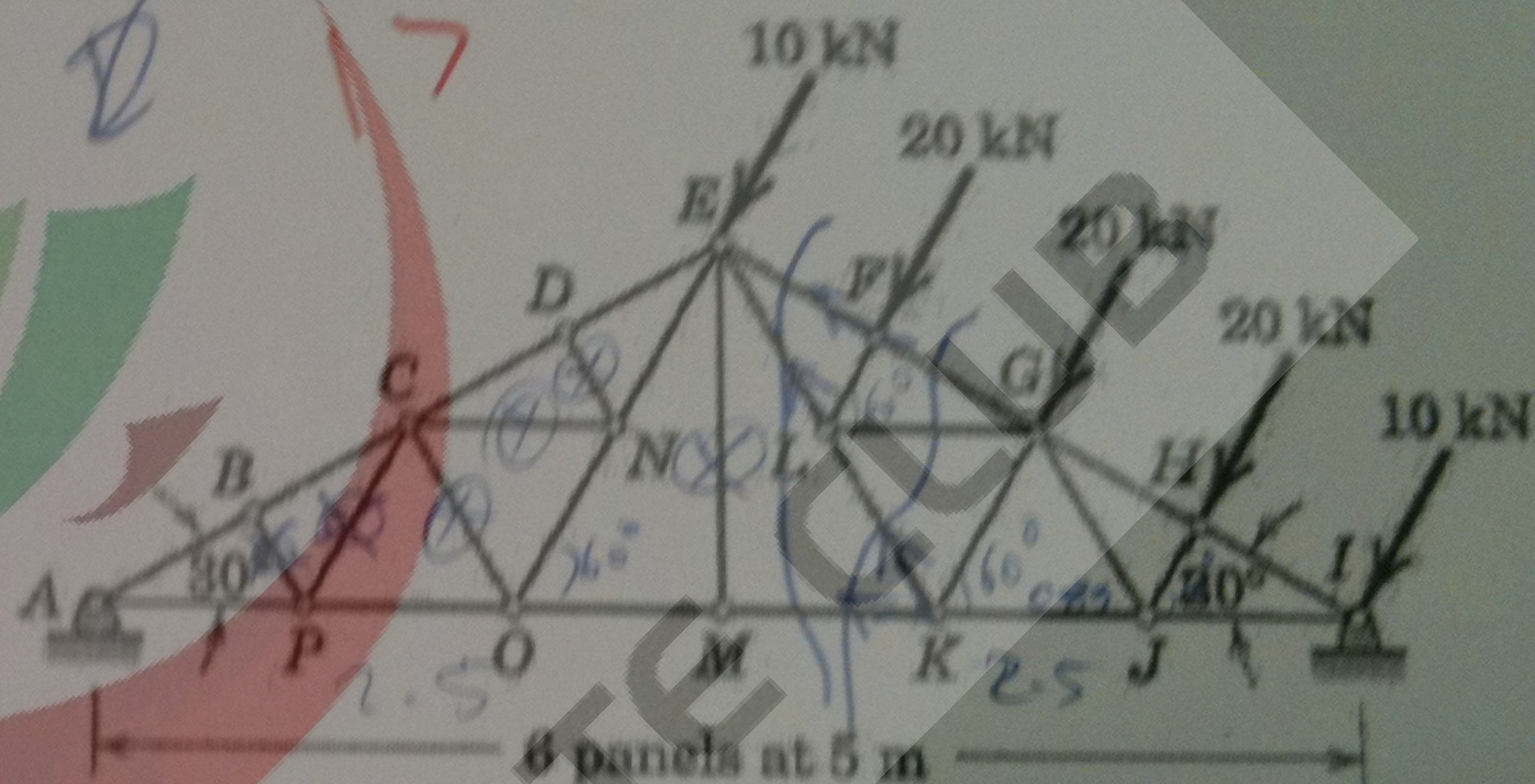
$$\Rightarrow -22\vec{j} + E_x\vec{i} + E_y\vec{j} + E_z\vec{k} - 0.22T_{DG}\vec{i} + 0.64T_{DG}\vec{j} - 0.48T_{DG}\vec{k} = 0$$

$$\Rightarrow (E_x - 0.22T_{DG})^2 + (E_y - 22)^2 + (E_z - 0.48T_{DG})^2 = 0$$

For the Fink truss shown in figure:

Determine the reactions at the roller-support A and the pin-support I .

Using the method of sections, determine the forces in members EF , KL , and GL .



$$\rightarrow \sum F_x = -10 \times \cos 60^\circ - 20 \times \cos 60^\circ - 20 \times \cos 60^\circ - 20 \times \cos 60^\circ$$

$$+ \rightarrow \sum F_x = -40 \text{ kN} = 40 \text{ kN} \leftarrow$$

$$\sum F_y = -10 \times \sin 60^\circ - 20 \times \sin 60^\circ - 20 \times \sin 60^\circ$$