## NDU

## MAT 235

# Ordinary Differential Equations 

## Exam \# 2

Duration: 55 minutes

Name:

Section:

## Instructor:

Grade:

1) (20 points) Solve the following differential equation for $x>0$ :
$y^{\prime \prime}-\frac{2}{x} y^{\prime}+\frac{2}{x^{2}} y=x \sin x$
2) ( $\mathbf{1 5}$ points) Find the general solution of the differential equation $\left(x^{2}-1\right) y^{\prime \prime}-2 x y^{\prime}+2 y=0(x>1)$ given that $x$ is a particular solution.
3) (20 points) Solve the initial-value-problem $y y^{\prime \prime}=\left(y^{\prime}\right)^{2}$ with $y(0)=y^{\prime}(0)=1$.
4) (20 points) Solve the differential equation $y^{\prime \prime}=x e^{x}+y$.
5) ( $\mathbf{2 5}$ points) Find a general power series solution for the differential equation $y^{\prime \prime}+x y^{\prime}+2 y=0$ near the ordinary point $x_{0}=0$.

Bonus Problem (10 points) Refer to exercise (5). Find a particular solution for $y^{\prime \prime}+x y^{\prime}+2 y=x$ near $x_{0}=0$ and deduce the general solution.

