NDU

## Notre Dame University

## MAT 235

# Ordinary Differential Equations 

## Exam 2

## Duration: 55 minutes

## Name:

## Section:

## Instructor:

## Grade:

1) (25 points) Solve the following differential equation for $x>0$ :

$$
y^{\prime \prime}-\frac{2}{x} y^{\prime}+\frac{2}{x^{2}} y=x \sin x
$$

2) ( $\mathbf{1 5}$ points) Find the general solution of the differential equation

$$
\left(x^{2}-1\right) y^{\prime \prime}-2 x y^{\prime}+2 y=0 \quad(\mathrm{x}>1)
$$

given that $x$ is a particular solution.
3) (20 points) Solve the initial-value problem $y y^{\prime \prime}=\left(y^{\prime}\right)^{2}$ with $y(0)=y^{\prime}(0)=1$.
4) (40 points) By using two different methods, solve the differential equation

$$
y^{\prime \prime}=x e^{x}+y
$$

