MAT 235 Make Up Exam I

1) Solve the following differential equations.

a)
$$-\frac{x}{2} \frac{dy}{dx} + y = \sqrt{y}$$
 (18 points)

b)
$$\frac{dy}{dx} = \frac{4x + 3y^2}{2xy}$$
 (18 points)

c)
$$x \frac{dy}{dx} - y = x^2 + y^2$$
 (18 points)

2) Solve the initial value problem.

$$\frac{dy}{dx} = \frac{x^3 - xy^2}{y^3 - x^2y}, y(1) = \sqrt{3}$$
 (23 points)

3) Find the family of orthogonal trajectories to the given family of curves

$$x^2 + y^2 + 2cy - 1 = 0$$
 (23 points)