

NDU

MAT 235

Ordinary Differential Equations

Exam # 1

Duration: 55 minutes

Name: _____

Section: _____

Instructor: _____

Grade: _____

1) (18 points) Solve the differential equation $3\frac{dy}{dx} + y = (1 - 2x)y^4$.

2) (18 points) Solve the differential equation $\frac{dy}{dx} = \frac{-2x}{x^2 + e^y}$.

3) (23 points) Solve the initial value problem

$$xy \frac{dy}{dx} = 2y^2 + 4x^2 \quad \text{with} \quad y(2) = 4, \quad x > 0 \quad \text{and} \quad y > 0$$

4) (23 points) Solve the differential equation

$$x \frac{dy}{dx} = 1 - x^2 y^2 - y, \quad \text{with } y(0) = 1 \quad (\text{Hint: You can use the substitution } v = xy)$$

- 5) (18 points)** Find the family of orthogonal trajectories to the given family of curves
 $c^2x^2 + y^2 = c^2$.