

NAME: Maha habchi ID: 20060951 Section: Hwf: 7-9

Part II. Solve the following problems

(20 points)

The electric field component of a beam of polarized light is

$$E_y = 5 \sin(10^6 z + \omega t) \text{ in V/m}$$

- What are the wavelength, the frequency, the period and the intensity of this light?
- Write an expression for the magnetic field component of the wave. Parallel to which axis does the magnetic field oscillate?

a)

$$k = 10^6 \text{ m}^{-1}; \quad \lambda = \frac{2\pi}{10^6} = 6.28 \times 10^{-6} \text{ m}$$

$$I = \frac{E_{\text{max}}^2}{2\mu_0 c} = \frac{(5)^2}{2 \times 3 \times 10^8 \times 4\pi \times 10^{-7}} = 0.033 \text{ W/m}^2$$

(12)

$$\omega = 2\pi f$$

$$f = \frac{\omega}{2\pi} \text{ (Hz)}$$

$$T = \frac{1}{f} = \frac{2\pi}{\omega} \text{ (s)}$$

Continuation of Part (a) → on 2nd page

b)

$$c B_{\text{max}} = E_{\text{max}} \Rightarrow B_{\text{max}} = \frac{E_{\text{max}}}{c} = \frac{5}{3 \times 10^8} = 1.67 \times 10^{-8} \text{ T}$$

(6)

$$B = 1.67 \times 10^{-8} \sin(10^6 z + \omega t)$$

$$B_x = 1.67 \times 10^{-8} \sin(10^6 z + 3 \times 10^{14} t) \text{ in (T)}$$

Parallel to the z -axis the Magnetic field oscillate.

In My conclusion: Direction is in $-ve$ sense
 $\vec{B} \times \vec{E}$ is in $-ve$ z direction

a)

$$v = \lambda f$$

$$\lambda = \frac{2\pi}{k} \quad ; \quad 2\pi f = \omega$$

$$v = \left(\frac{2\pi}{k}\right) \left(\frac{\omega}{2\pi}\right) = \frac{\omega}{k}$$



and since here
it is Polarized
light \Rightarrow

$$v = c = 3 \times 10^8 \text{ m/s}$$

$$3 \times 10^8 \times 10^6 = \omega = 3 \times 10^{14} \text{ rad/s}$$

$$\omega = 2\pi f \Rightarrow f = \frac{\omega}{2\pi} = \frac{3 \times 10^{14}}{2\pi} = 4.77 \times 10^{13} \text{ Hz}$$

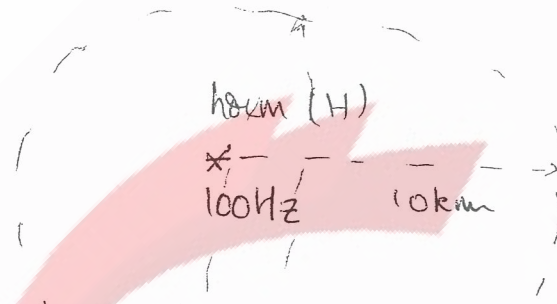
$$T = \frac{1}{f} = 2.09 \times 10^{-14} \text{ sec}$$



(17 points)

At a distance of 10 km, a 100 Hz horn, assumed to be an isotropic point source, is barely audible.

- What is the power of the horn?
- At what distance would it begin to cause pain?



$$a) \frac{\text{Power}}{A} = I \Rightarrow \text{Power} = I \cdot A = 4\pi(10 \times 10^3)^2 \times I$$
$$I = \frac{P_s}{A}$$

Since barely audible then $I = I_0 = 10^{-12} \text{ W/m}^2$
(Minimum sound the ear could hear)

$$\text{Power} = 10^{-12} \times 4\pi \times (10^4)^2 = 1.256 \times 10^{-3} \text{ W}$$

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b) It begins to cause pain at $I = 1 \text{ W/m}^2$
pain

$$\text{Power} = I \cdot A$$

$$\frac{P_s}{I} = A = \frac{1.256 \times 10^{-3}}{1} = 4\pi r^2$$

$$r^2 = 10 \times 10^{-5} \text{ m}^2$$

$$r = 10 \times 10^{-3} \text{ m}$$

$$r = 10 \text{ mm}$$