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Notre Dame University
Department of Electrical, Computer and Communication Engineering

Sample Exam

Circuit Analysis I

EEN100
R. Jabr

Name:

ID #:

Section:

Notes:

Time = 50 Minutes.

Number of Pages = 5

This exam is Closed Book and Closed Notes.

All Questions Should be Answered on the Exam Sheet.

Scratch paper will not be collected.

Write neatly and show the main steps required to reach the final answer.

Underline your final answer and include units.

Grading:

Question Number	Grade
1	25 / 25
2	25 / 25
3	25 / 25
4	25 / 25
Total	100 / 100

Question # 1 (25 points):

Determine the power that is absorbed or supplied by the elements in the circuit shown in Figure 1. Is the principle of conservation of energy satisfied? Justify your answer.

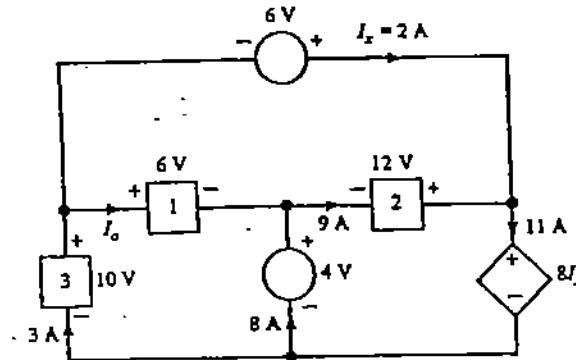


Figure 1

Solution:

$$I_o = 3 - 2 = 1 \text{ A}$$

$$P_1 = 6 \times 1 = 6 \text{ W absorbed}$$

$$P_2 = -12 \times 9 = -108 \text{ W} \quad \Rightarrow \text{delivers } 108 \text{ W}$$

$$P_3 = -3 \times 10 = -30 \text{ W} \quad \Rightarrow \text{delivers } 30 \text{ W}$$

$$P_{6V} = -6 \times 2 = -12 \text{ W} \quad \Rightarrow \text{delivers } 12 \text{ W}$$

$$P_{4V} = -4 \times 8 = -32 \text{ W} \quad \Rightarrow \text{delivers } 32 \text{ W}$$

$$P_{8\Omega} = 8 \times 2 \times 11 = 176 \text{ W}$$

$$\sum P_{abs} = 176 + 6 = 182 \text{ W}$$

$$\sum P_{del} = 108 + 30 + 12 + 32 = 182 \text{ W}$$

} \Rightarrow principle of conservation of energy is satisfied

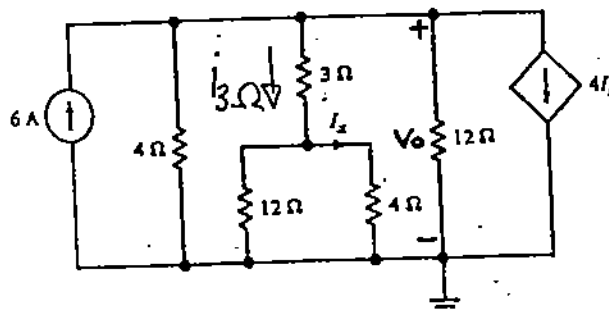
Question # 2 (25 points):Find the voltage V_o in the network in Figure 2.

Figure 2

Solution:

$$I_x = \frac{12}{12+4} I_{3\Omega} = \frac{3}{4} I_{3\Omega} \Rightarrow I_{3\Omega} = \frac{4}{3} I_x$$

$$V_o = 3 \frac{4}{3} I_x + 4 I_x = 8 I_x$$

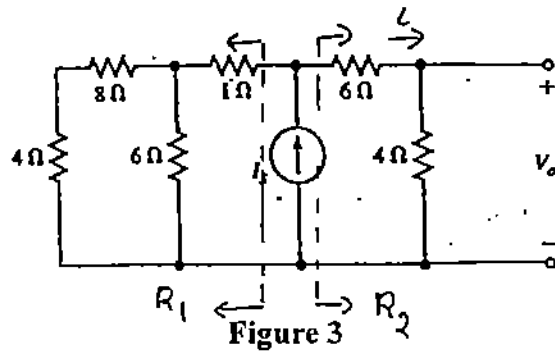
$$KCL \Rightarrow -6 + \frac{8 I_x}{4} + \frac{4}{3} I_x + \frac{8 I_x}{12} + 4 I_x = 0 \Rightarrow I_x = 0.75 A$$

$$\Rightarrow V_o = 8 I_x$$

$$V_o = \underline{\underline{6 V}}$$

Question #3 (25 points):

Given the circuit in Figure 3, if $V_o = 12V$, Find I_s .



Solution:

$$R_1 = 12 // 6 + 1 = 5 \Omega$$

$$R_2 = 6 + 4 = 10 \Omega$$

$$i = \frac{12}{4} = 3A = \frac{5}{5+10} I_s \Rightarrow \underline{\underline{I_s = 9A}}$$

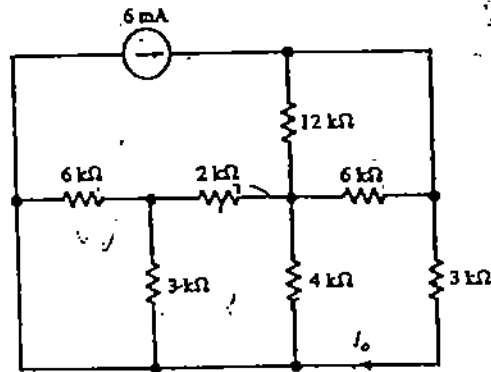
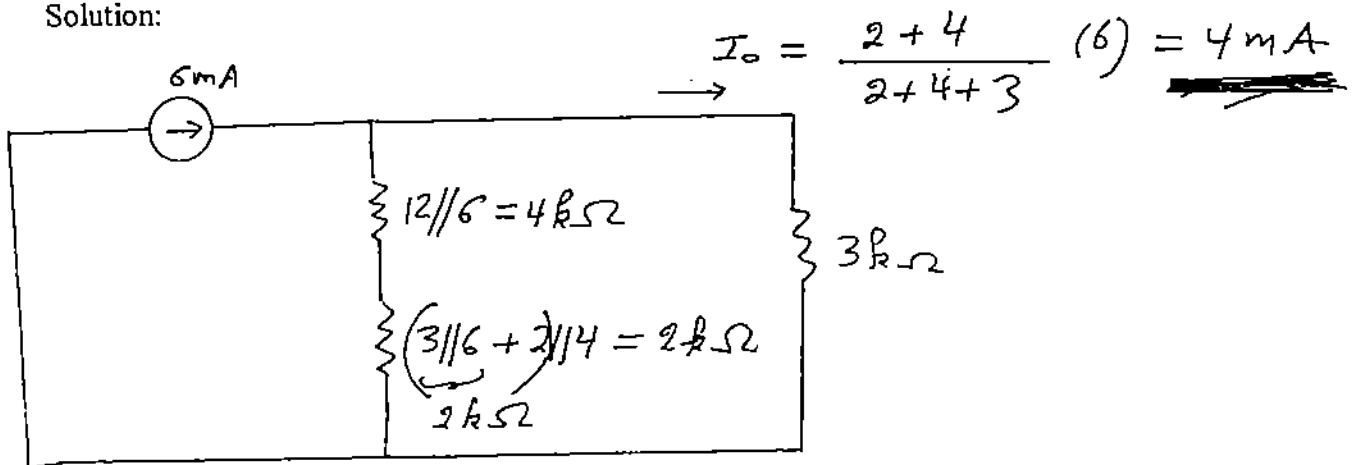
Question #4 (25 points):Find I_o in the network shown in Figure 4.

Figure 4

Solution:



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NOTE: OPEN BOOK, OPEN NOTES, CLOSED NEIGHBOURS
NOTE2: SHOW ALL WORK IN ORDER TO RECEIVE FULL CREDIT.

1. 15 Pts. In the circuit shown in Fig.P1, find the power absorbed or delivered by the circuit elements. Is the circuit valid?

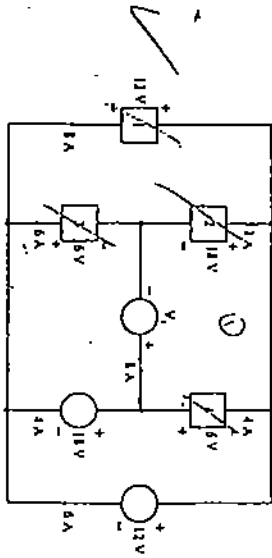


Fig.P1.

Handwritten notes:
12V source
1A source
4A source
12V source
4A source
12V source
4A source
12V source
4A source

2. 15 Pts. Find the voltage gain v_o/v_s in the circuit shown in Fig.P2.

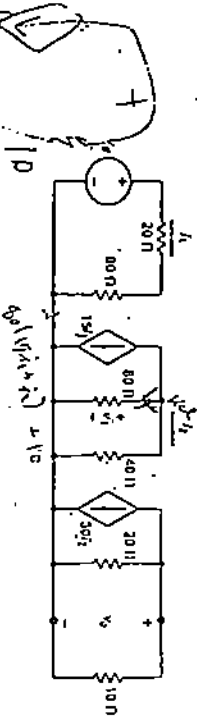


Fig.P2.

Handwritten notes:
10V source
20 ohm
60 ohm
40 ohm
10 ohm
0.5v_o
0.2v_o
0.1v_o

3. 20 Pts. In the network in Fig.P3, if the power generated by the 4-A source is 48W, Find V_o .

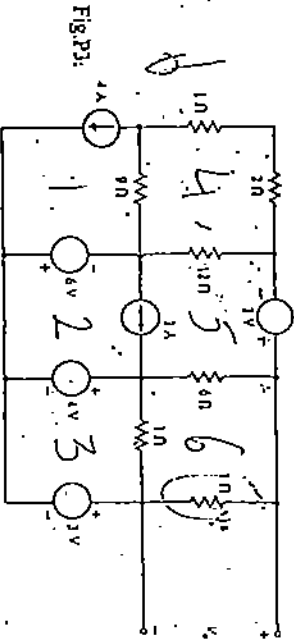


Fig.P3.

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4. 15 Pts. The network in Fig.P4 is used in digital-to-analog converters. Find an expression for I_1 , I_2 , and I_3 in terms of I_0 .

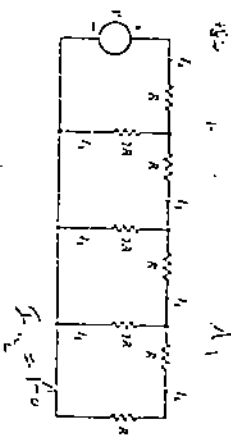


Fig.P4.

Handwritten notes:
I_1 = I_0/2
I_2 = I_0/4
I_3 = I_0/8

5. 15 Pts. Find V_o in the circuit shown in Fig.P5.

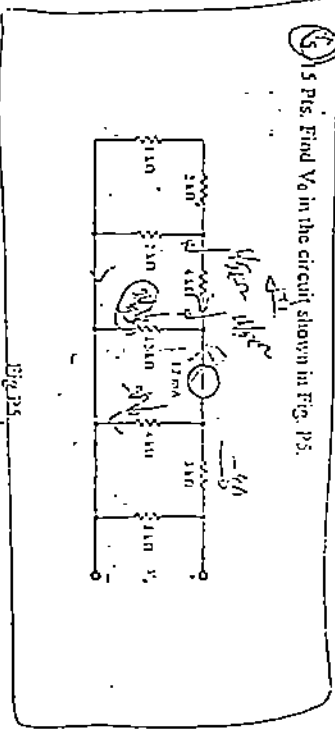


Fig.P5.

Handwritten notes:
 $V_o = R I$

6. 20 Pts. Find the power absorbed by the 12-ohm resistor in the network shown in Fig.P6.

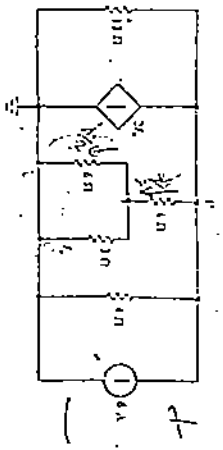


Fig.P6.

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Solution: $I_{R_{200}} = 2000$

Test 1

P_1	$2(8)$	16	ABSORBED
P_2	$8(3)$	24	ABSORBED
P_3	$4(6)$	24	ABSORBED
P_4	$6(4)$	24	ABSORBED
$P_{(200)}$	$12(2)$	24	ABSORBED
$P_{(50)}$	$18(4)$	72	DELIVERED

$P_{(18)}$	$6 + V_x = 0$	$\Rightarrow V_x = -24V$
$P_{(24)}$	$24(-8)$	$= -192W \Rightarrow 192W$ DEL
$P_{(26)}$	$-26(4)$	DELIVERED

$\Rightarrow -26(4) \Rightarrow$ Current is valid

$26(4) = 104$
 $\Rightarrow -104 + 204 = 80A = 0$

$\Rightarrow \frac{I_{R_{200}}}{V_g} = \frac{1}{100}$

$15A_1 + I_1 + 12A_2 = 0 \Rightarrow I_1 = -15A_1$

$80I_1 + 40A_2 = 0$
 $-80(-15A_1) + 40A_2 = 0$

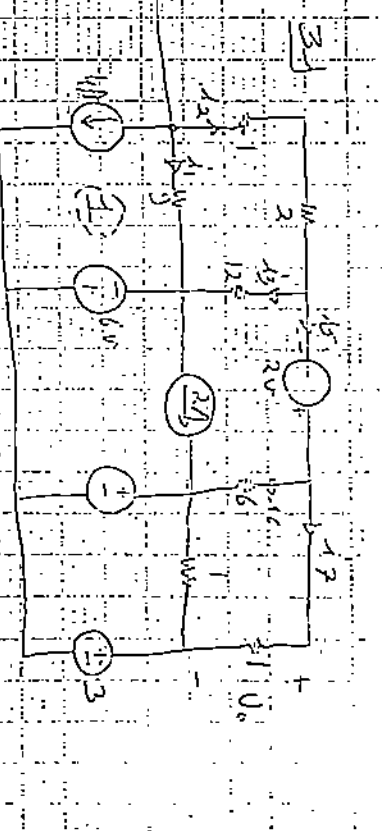
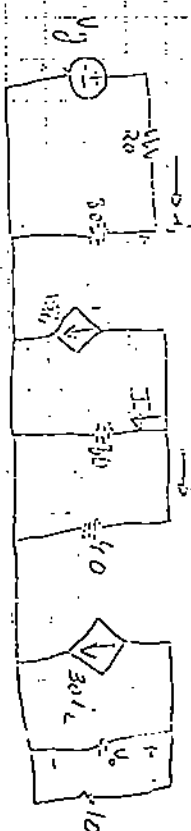
$\Rightarrow \frac{A_2}{A_1} = -10$

$\Rightarrow 80 \Omega$ and 10Ω are in $\parallel \Rightarrow R_{eq} = \frac{80 \times 10}{80 + 10} = \frac{200}{9} = \frac{20}{0.9}$

$V_g = 24A \Rightarrow V_g = \left(\frac{20}{3}\right)(-30A_1)$

$\Rightarrow \frac{V_g}{A_1} = 200$

$$\frac{V_o}{V_g} = \left(\frac{V_o}{I_2}\right) \left(\frac{I_2}{I_1}\right) \left(\frac{I_1}{V_g}\right) = 200(-10) \frac{1}{100} = -20$$



generator is ideal $\Rightarrow P = 1.8W$

$P = 0.1 \Rightarrow V = \frac{P}{I} = \frac{1.8}{4} = 0.45V$

$\Rightarrow V = 1.8V$

$9A_1 - 6 + 12 = 0 \Rightarrow \frac{I_1}{A_1} = \frac{2}{3}$

$12A_2 - 4 = 0 \Rightarrow \frac{I_2}{A_2} = \frac{1}{3}$

Current is not the cause of the error. Also, the KVL is not applied correctly. The current is not the cause of the error.

ENEN 100 Circuit Analysis I Test #1

- 20 Pts. The voltage and current at the terminals of an element are given by:
 $v = 100 e^{-100t}$ V, $i = 10 e^{-100t}$ mA.
- Calculate the power received by this element at $t = 1$ ms.
- Calculate the total energy delivered to this element.

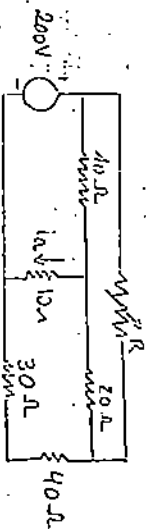
- 20 Pts.

Find the voltage v_x in the following circuit.
Calculate the power delivered or absorbed by each element.
Verify that the total of absorbed powers is equal to the total c delivered powers.



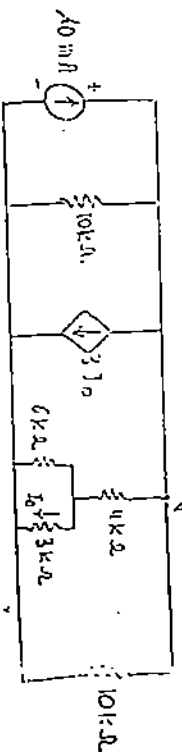
- 20 Pts.

The variable resistor R is adjusted until $i_x = 1$ A. Find the value of R .



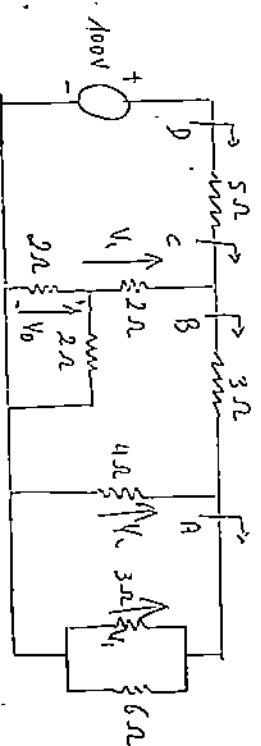
- 20 Pts.

Find the power absorbed by the 3 kΩ resistor in the following circuit.



- 20 Pts.

Find the equivalent resistance at points A, B, C, and D.
By the voltage division method find V_o .
By the current division method find V_o .



Handwritten student work on graph paper. The table below summarizes the visible calculations and results.

Problem	Method	Result
1	Power	$P = 100 \times 10 = 1000$ W
2	Voltage	$V_x = 100 e^{-100 \times 10^{-3}} = 100 e^{-0.1} \approx 90.48$ V
3	Resistor R	$R = 100 \Omega$
4	Power	$P = 3 \times 10^3 \times 1^2 = 3000$ W
5	Equivalent Resistance	$R_{eq} = 10 \Omega$

6. 15 Pts. Find the power absorbed by the $12\text{-}\Omega$ resistor in the network in Fig. P6. 5.75 W

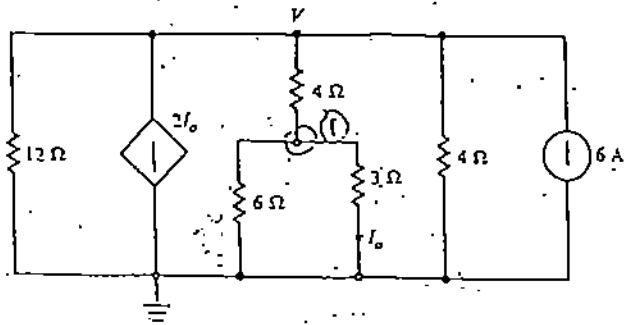


Fig P6

7. 25 Pts. Use Nodal analysis to find I_o in the network in Fig. P7.

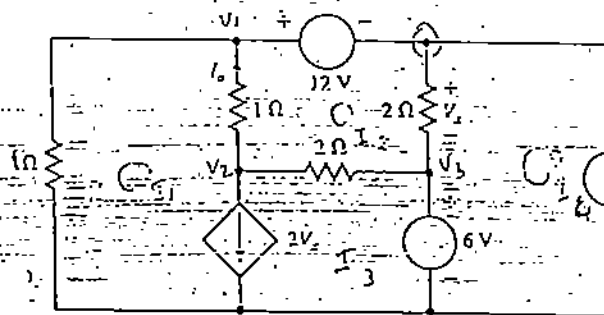


Fig P7

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Test 1

$P_1 = 2(6) = 12W$

$P_2 = 2(6) = 12W$

$P_3 = 4(2) = 8W$

$P_{av} = 3(4) = 12W$

$P_o = 7(VI) = 7(8) = 56W$

$68W$ ABS } available power

$68W$ DEL } available power

$3 + 4 = 7$

$4 // 2 = 3$

$4 // 4 = 2$

$2 + 3 = 5$

$5 // 5 = 2.5$

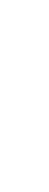
$R_{eq} = 5 + 2.5 + 5 = 12.5 \Omega$

$34 \quad 10 + 2 = 12 \Omega$

$12 // 6 = 4 \Omega \quad 4 + 2 = 6 \Omega$

$2 + 1 = 3 \Omega$

$3 // 6 = 2 \Omega = R_{eq}$



$V_4 = \frac{36 \times 4}{6} = 24V$ (with sign convention)

$6A - 36 = 0 \Rightarrow I = 6$

$\Rightarrow V_r = 6(4) = 24V$

$36 - 24 = 12 \Rightarrow 3I_o = 0$
 $\Rightarrow I_o = -4A$

$2 + 1 = 3 \Omega, 3 // 6 = 2 \Omega$
 $1 + 2 + 3 = 6$



current division
 $I = 4$
 $I = 8$

current division
 $I = \frac{16}{3} \Rightarrow I_o = 3.2V$



$KVL \text{ at } 6 \quad V_4 = 4I_1 + 2I_2 = 4I_1 + 2I_2$

$KVL \text{ at } 4 \quad 2 = 9I_1 - 6I_2 \Rightarrow 3I_1 - 2I_2 = 2A$

$KVL \text{ at } 2 \quad 4A - 2I_1 + 2I_2 = 2$

$KVL \text{ at } 1 \quad 6I_1 - 2I_2 = 6$

$KVL \text{ at } 3 \quad 6I_1 - 2I_2 = 6$

$KVL \text{ at } 4 \quad 6I_1 - 2I_2 = 6$

$KVL \text{ at } 2 \quad 6I_1 - 2I_2 = 6$

$KVL \text{ at } 1 \quad 6I_1 - 2I_2 = 6$

we consider the same way
 on #3 in Fall 2000
 (But beware of the claims of the sign of the voltage)