



Notre Dame University, Department of Mechanical Engineering
Test #2-MEN210 (Thermodynamic I) Open book: 1hr
Dr. Gabi Nehme, PhD Spring-2006

Problem # 1 (25pts)

A rigid tank is electrically wired and contains ideal gas. The energy going into the tank is at a rate 75 W and energy leaves the system at a rate of 20 W. If the mass of the gas is 2 kg and the temperature changes over 10 minutes is 40 K. Find C_v in kJ/kg.K.

Problem # 2 (15pts)

Temperature, Pressure and Heat are state functions. True or false? Explain in details.

Problem # 3 (30pts)

Consider a piston weighing 990 g which contains 10 g or 0.347 mole of air at 1 atm and 25° C. Calculate the effects of performing 100 J of work on the air-containing piston for the following situations. State any assumptions and show all units.

- Find the maximum possible elevation if all the work is used to raise the cylinder and its contents vertically.
- Find the maximum possible final velocity if all the work is used to accelerate the cylinder and its contents.
- Find the maximum possible pressure of air if the piston is compressed isothermally.

Problem # 4 (30pts)

A heat exchanger is insulated and has two inlets and one outlet. At inlet one, water vapor enters at 5 MPa and 430°C. At inlet two, Liquid water enters at 10 MPa with an internal energy of 416.11 kJ/kg. The mass flow rate is 15kg/s at each inlet. A mixer of streams put 5 KW into the system. Exit pressure is 10 MPa.

Locate the states on P-V diagram and find the exit temperature of the stream.





problem 1

$$\dot{E} = \dot{E}_{in} - \dot{E}_{out} = 75 - 20 = 55 \text{ W} = 55 \text{ J/s}$$

$$\begin{aligned} \Delta E &= \dot{E} \times 10 \text{ min} \times \frac{60 \text{ sec}}{\text{min}} \\ &= 33 \text{ kJ} \end{aligned}$$

$$\Delta E = \Delta U + \Delta KE + \Delta PE$$

$$\Delta E = \Delta U \quad 0 \quad 0$$

$$\Delta U = 33 \text{ kJ}$$

$$du = \frac{33}{2} = 16.5 \text{ kJ}$$

$$du = C_v dT$$

$$C_v = \frac{du}{dT} = \frac{16.5}{40} = 0.4125$$

problem # 2

Temperature and pressure are state functions because they define the state. If you know the Temp. & the press. ~~of the~~ you can know its phase (solid, liquid, gas) but heat is not a state function thus it doesn't define the state. If we know the heat loss & gained, we can't know the phase & the state. Heat is a function of work & int. dy, KE, PE, etc. so it doesn't define state. no statement is false.



Problem 3

Control mass: All air in piston

Initial state: P_1, T_1, V_1, m

Final state: P_2, T_2, V_2, m

Process: mass is constant

Model: A-Z.1 prop. air

piston	$m = 0.0994$
air	$m = 0.01 \text{ kg}$
	$P = 100 \text{ kPa}$
	$T = 25 \text{ K}$

a) analysis: First law of thermodynamics

$$Q_{1-2} - W_{1-2} = m(u_2 - u_1) + \frac{1}{2} m (V_2^2 - V_1^2) + mg(z_2 - z_1)$$

a) max. elevation: no work ^{done to increase} ~~done to increase~~ $W = 0$
 no work for initial energy $du = 0$

~~0 (0.1 kg)~~

$$Q_{1-2} - W_{1-2} = mg(z_2 - z_1)$$

$$0 - 0 = (0.1 \text{ kg}) = \frac{(0.994 + 0.01) \times 9.80665}{1000} (z_2 - z_1)$$

$$\boxed{\Delta z = 10.19 \text{ m}}$$

$$z_1 = 0 \text{ so } z_2 = 10.19 \text{ m}$$

b) max velocity no work to elevatn. $P_1 = 0$

no work to energy $du = 0$

$$Q_{1-2} - W_{1-2} = \frac{1}{2} m (V_2^2 - V_1^2)$$

$$(-0.1 \text{ kJ}) = \frac{1}{2} (0.994 + 0.01) (V_2^2 - V_1^2)$$

$$V_2^2 - V_1^2 = 200 \quad V_1 = 0$$

$$\boxed{V_2 = 14.14 \text{ m/s}}$$

c) max pressure: For maximum pressure we have the max U

$$W = \int_{V_1}^{V_2} P dV \quad P = \frac{nRT}{V}$$

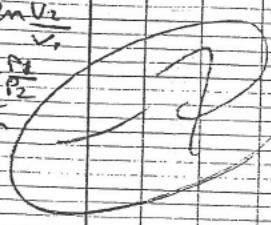
$$= \int_{V_1}^{V_2} \frac{nRT}{V} dV \quad \text{do facts}$$

$$W = nRT \int_{V_1}^{V_2} \frac{1}{V} dV$$

$$= nRT \ln \frac{V_2}{V_1}$$

$$= nRT \ln \frac{P_1}{P_2}$$

$$= 1.12 \text{ kJ}$$



$$Q_{1-2} = W_{1-2} = m_{H_2O} (u_2 - u_1)$$

From table A.7.1 at $T_1 = T_2 = 298 \text{ K}$

$$2 \text{ kg} \cdot 0.1 \text{ MPa} \quad u = 213.04 \text{ kJ/kg}$$

$$u_1 = 213.04$$

$$0.1 = 0.01 (u_2 - 213.04)$$

$$10 = u_2 - 213.04$$

$$u_2 = 223.04 \text{ kJ/kg}$$

The temperature is the same 298 K but u is increased
so the pressure must increase.

what if

problem 4

- control volume: heat exchanger
- inlet: vapor, liquid
- outlet: fixed me,
- ~~inlet, fixed~~
- ~~inlet, fixed~~



Process - steady state process

model: steam table

Analysis: 1st law of Thermodynamics

$$Q + \sum m_i (h_i + \frac{1}{2} V_i^2 + gz_i) = \sum m_e (h_e + \frac{1}{2} V_e^2 + gz_e) + \dot{W}$$

solution: ~~5 MPa~~ inlet @ \Rightarrow 5 MPa, 430°C superheated

Table B.3 interpolating $\frac{450 - 430}{450 - 400} = \frac{3316.15 - h}{3316.15 - 3155.64}$

$$h_v = 3268.43 \text{ kJ/kg}$$





inlet @ 10 MPa $u = 416.11$ water subcooled $T = 100^\circ\text{C}$

$$h_f = 426.47 \text{ kJ/kg}$$

Assumption: heat exchanger: $W = 0$

No KE, No PE
 $m_{in} = m_{out} = 2 \text{ mi}$

$$m_1(h_1) + m_2(h_2) = m_e h_e + W$$

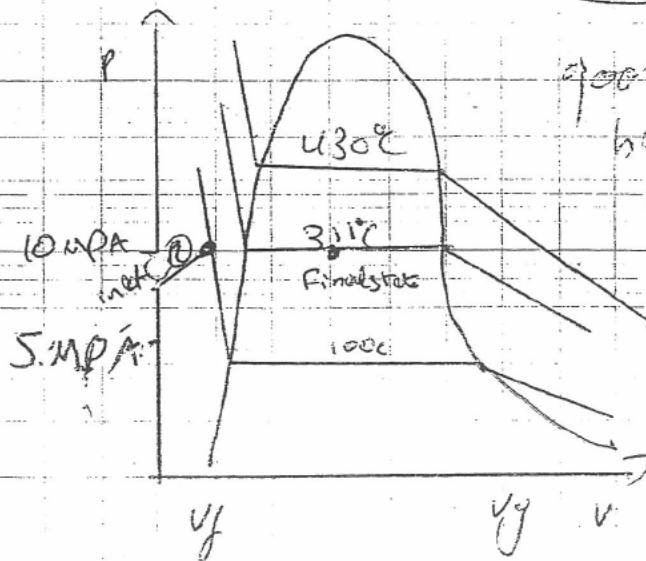
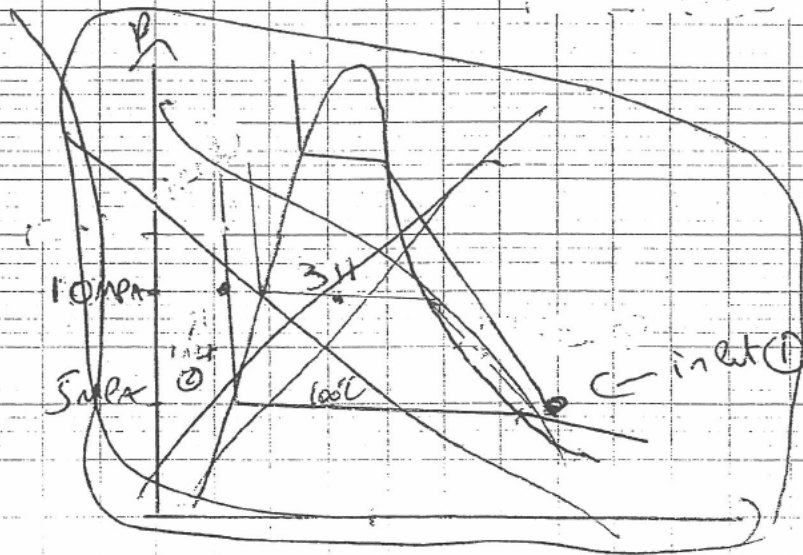
$$m_1(h_1 + h_2) = 2m_1 h \quad -5$$

$$2m_1 h = 15(2 \times 426.48 + 3268) + 15$$

$$h = 1847 \text{ kJ/kg}$$

From B.2 @ 10 MPa $h_f = 1407, h_g = 2729$

$h_f < h < h_g$ so it is sat. @ 311.06°C



good but little explanation needed

-2