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Mechanics of Materials 2: 2000

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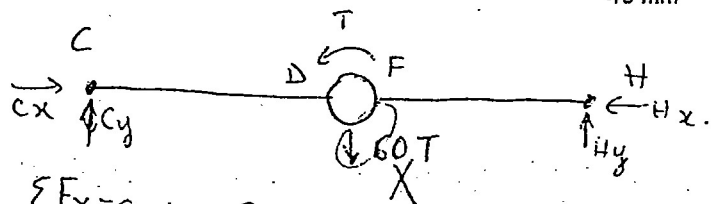
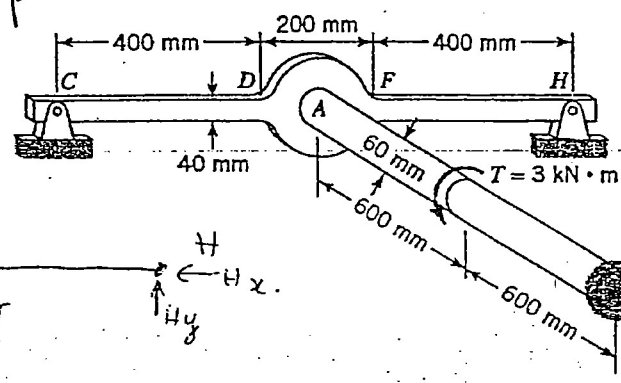
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MEN 302
EXAM 2
SPRING 2004

1) (20 pts) A shaft AB is attached to member $CDFH$ at A and fixed to a wall at B . The shaft has a diameter of 60 mm and the parts CD and FH have square cross sections of 40 mm by 40 mm . The massive hub DF may be considered rigid. A torque of magnitude $3\text{ kN}\cdot\text{m}$ is applied to the midsection of the shaft. All members are made of steel ($E = 200\text{ GPa}$ and $G = 77.5\text{ GPa}$). Determine the maximum shear stress in the shaft.

old edition
p. 184

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$$\sum F_x = 0 \Rightarrow C_x = H_x$$

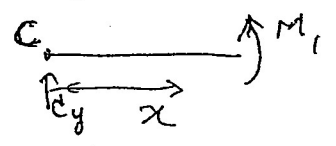
$$\sum F_y = 0 \Rightarrow C_y + H_y = 60T$$

$$\sum M_C = 0 \Rightarrow H_y \times 1000 + T + 60T \times 500 = 0 \Rightarrow H_y = 30.001 Q$$

$$\Rightarrow C_y = 60Q - H_y = 60Q - 30Q \Rightarrow C_y = 30Q$$

let $T = Q$
 $T_B = Y$

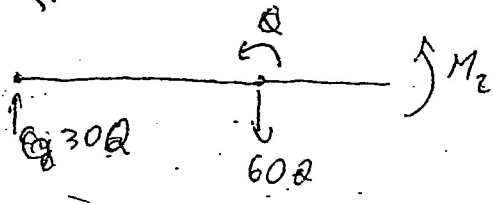
cut: $0 \leq x < 400$



$$M_1 = C_y x \Rightarrow M_1 = 30Qx$$

$$\frac{\partial M_1}{\partial Q} = 30x$$

cut: $600 \leq x \leq 1000$



$$M_2 = 30Qx - 61Q$$

$$\frac{\partial M_2}{\partial Q} = 30x - 61$$

$$M_2 = -Q - 60Q + 30Qx = -61Q + 30Qx$$

X

$$\frac{1}{EI} \left[\int_0^{0.4} (30Qx)(30x) dx + \int_{0.6}^1 (30Qx - 61Q)(30x - 61) dx \right]$$

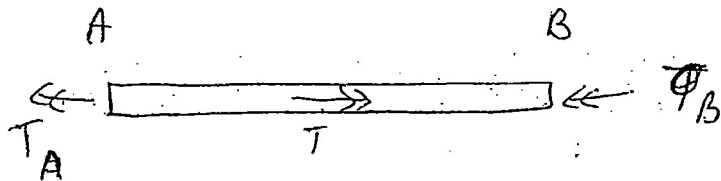
$$= \frac{1}{EI} \left[\left(900Q \frac{x^3}{3} \right)_0^{0.4} + \left(\frac{30Qx^3}{3} - \frac{1830Qx^3}{3} - \frac{1830Qx^2}{2} + 37216 \right) \right]$$

$$= \frac{1}{EI} [19.2Q + 432.4Q] = \frac{1}{EI} [451.6Q]$$

$$= \frac{1}{200 \times 10^9 \times \frac{1}{12} \times 0.04^4} [451.6 \times 3000]$$

$$= \boxed{31.753125} \quad (1)$$

Stab

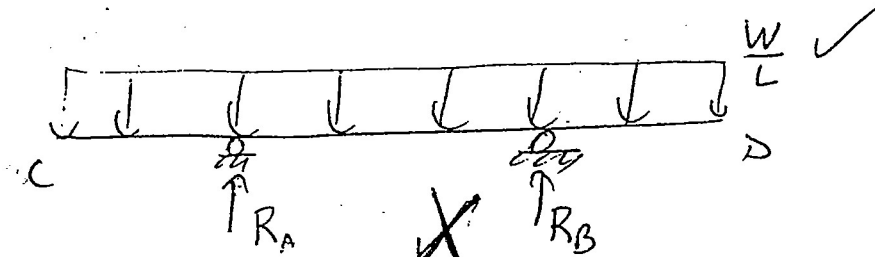
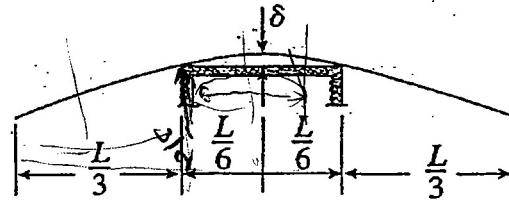


let $Q = T_A$

\Rightarrow

X

2) (15 pts) A thin metal strip of total weight W and length L is placed across the top of a flat table of width $\frac{L}{3}$ as shown in the figure. What is the clearance δ between the strip and the middle of the table. The strip of metal has a flexural rigidity EI .

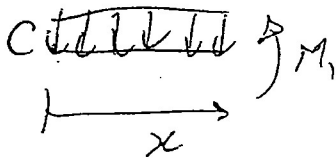


$$R_A + R_B = \frac{W}{L}$$

$$R_A = R_B = \frac{W}{2L}$$

cut

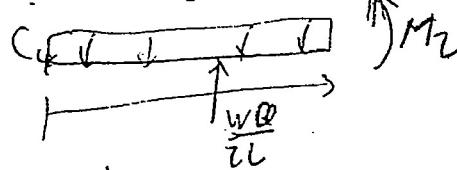
$$0 \leq x < \frac{L}{3}$$



$$M_1 = -\frac{W}{L} x^2$$

cut

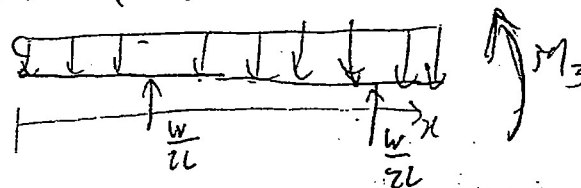
$$\frac{L}{3} < x < \frac{2L}{3}$$



$$M_2 = -\frac{W}{L} x + \frac{W}{2L} \left(x - \frac{L}{3} \right)$$

cut

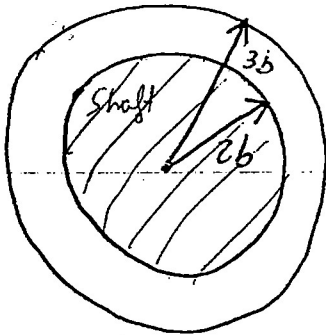
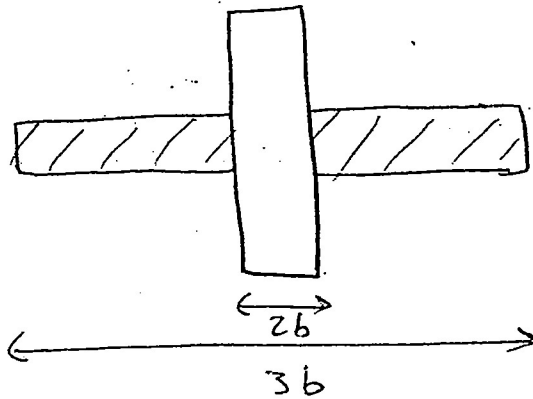
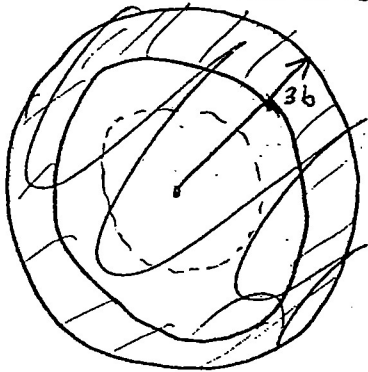
$$\frac{2L}{3} < x \leq L$$



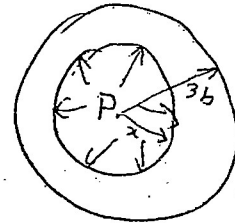
$$M_3 = -\frac{W}{L} x + \frac{W}{2L} \left(x - \frac{L}{3} \right) + \frac{W}{2L} \left(x - \frac{2L}{3} \right)$$

3) (15 pts) A steel tube of external diameter $3b$ is shrunk onto a solid steel shaft of diameter $2b$. The internal diameter of the tube is increased by an amount δ_0 .

Assuming that $\nu = \frac{1}{3}$, determine the reduction of the diameter of the shaft.



internal d of the tube increased by δ_0



$\Rightarrow \delta_0 = 2u$ & let x be the initial internal radius of the tube

~~$u = \frac{P x^2}{E} \left(\frac{1}{2} + \frac{1}{2} \frac{3b^2 + 2b^2}{3b^2 - 2b^2} \right)$~~

we have $U_{\text{tube}} - U_{\text{shaft}} = \delta_{\text{allowance}}$

but $\delta_0 = 2u_t \Rightarrow u_t = \frac{\delta_0}{2}$

$\Rightarrow U_s = \frac{\delta_0}{2} = \delta$

~~$\delta = \frac{2bP}{E} \left(\frac{4b^2 + 9b^2}{9b^2 - 4b^2} + 1 \right) + \frac{2bP}{E} \left(\frac{0 + 4b^2}{4b^2 - 0} - 1 \right)$~~

$= \frac{2bP}{E} \left[\left(\frac{13}{5} + \frac{1}{3} \right) + \left(1 - \frac{1}{3} \right) \right] = \frac{2bP}{E} \cdot \frac{52}{15}$

$\Rightarrow \delta = \frac{104 b P}{15 E} \quad P = ?$