$\begin{array}{c} {\rm MATHEMATICS~201} \\ {\rm SUMMER~SEMESTER,~2000\text{-}01} \\ {\rm Makeup~Quiz~II} \end{array}$

Time: 60 Minutes. Date: August 17, 2001. Instructor: Prof. A. Lyzzaik

Answer the following questions:

- 1. (a) Express in polar form the rectangular equation $x^3 + y^3 3axy = 0$. (10 points)
 - (b) Express in rectangular form the polar equation $r^2 \cos(2\theta) = 1$. (10 points)
- 2. Consider the polar equation $r^2 = 8\cos(3\theta)$.
 - (a) Indicate the possible symmetries of the graph. (10 points)
 - (b) Sketch the graph. (10 points)
- (c) Find the polar equation of the tangent line to the graph at the polar point whose $\theta = \pi/4$. (10 points)
- 3. Consider the polar equations $r = -6\cos\theta$ and $r = 2 2\cos\theta$.
 - (a) Find the points of intersection of the two graphs. (10 points)
- (b) find the area of the region lying outside the graph of $r=-6\cos\theta$ and inside the graph of $r=2-2\cos\theta$. (10 points)
- 4. Consider in rectangular form the equation $9x^2 + 4y^2 36z^2 = 1$.
 - (a) Write the equation in cylindrical and spherical coordinates. (10 points)
- (b) Sketch the graph of the equation by showing its traces with the rectangular planes. (10 points)
- 5. Identify the surfaces given in spherical and cylindrical coordinates, respectively, by $\rho = 1 \cos \phi$ and $r = 1 \cos \theta$. (10 points)